

Proposal

to perform an experiment at MAMI

High Precision Measurement of the ep elastic cross section at small Q^2

Contact person for the Experiment:

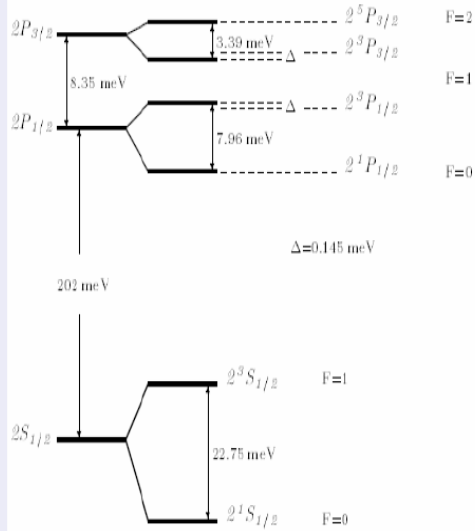
Alexey Vorobyev, Petersburg Nuclear Physics Institute

Mainz contact person: Achim Denig,
Institute for Nuclear Physics, JGU Mainz

Motivation

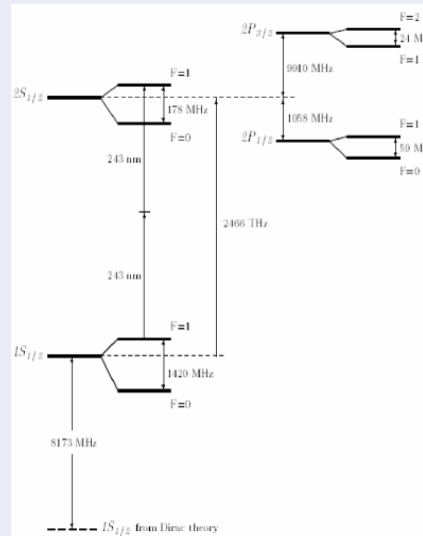
Proton radius puzzle

μp atom



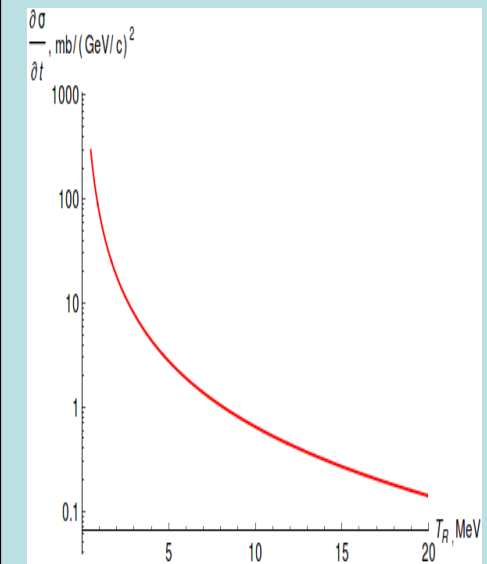
$$R_p = 0.8409(4)\text{fm}$$

$e p$ atom



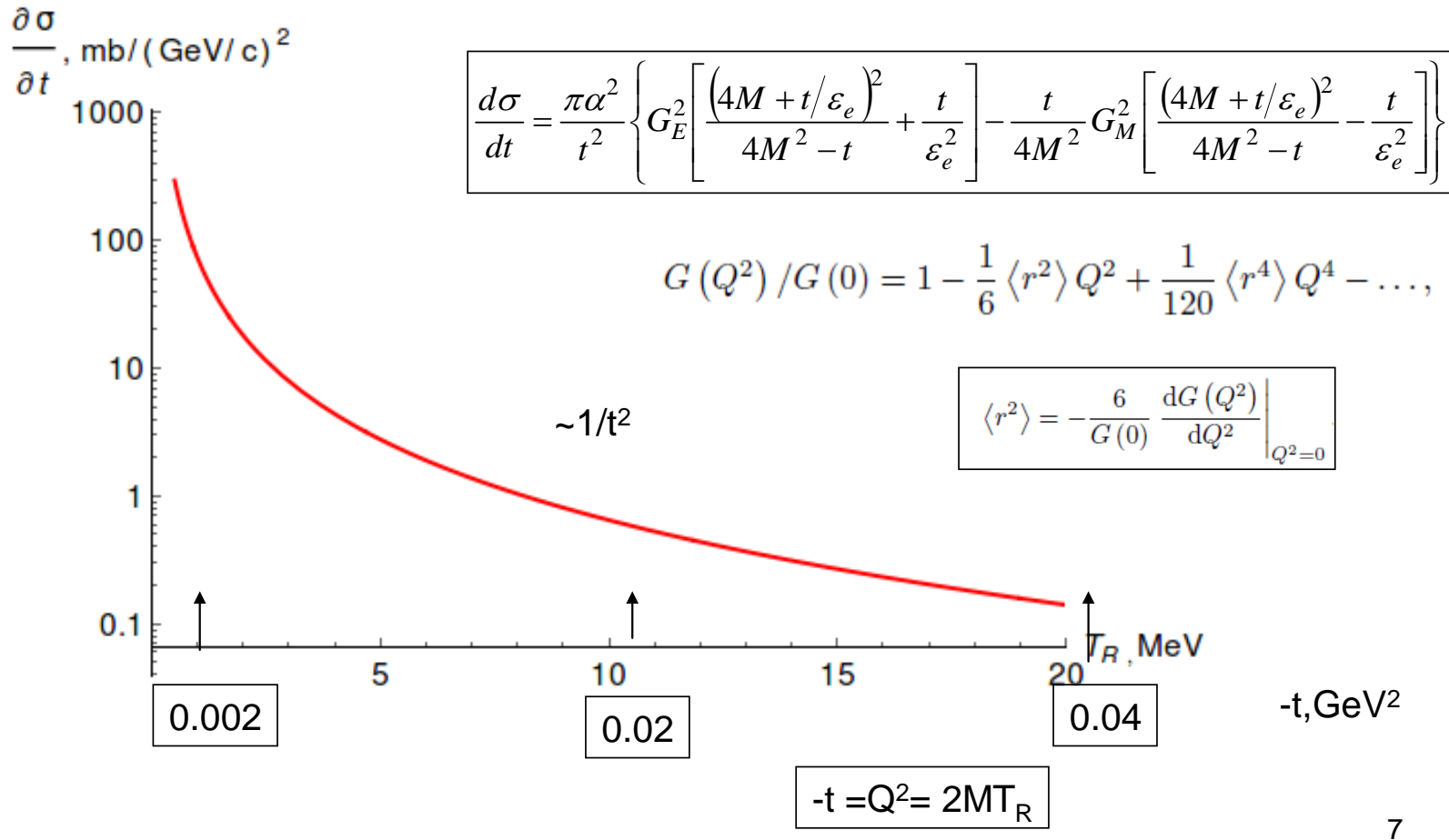
$$R_p = 0.877(8)\text{fm}$$

$e p$ scattering



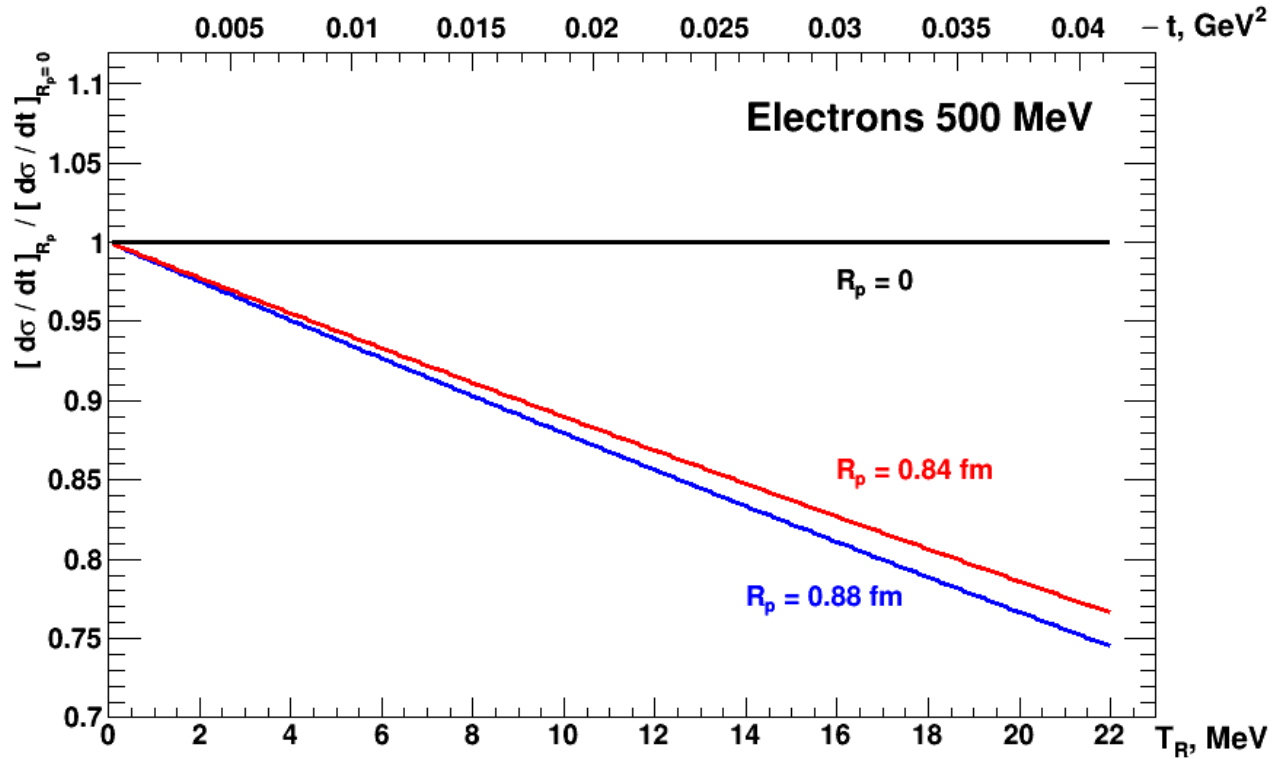
$$R_p = 0.877(7)\text{fm}$$

Extraction of proton radius from e-p cross section



The measurements of $d\sigma/dt$ should be at $Q^2 \leq 0.02 \text{ GeV}^2$

$$\left[\frac{d\sigma}{dt} \right]_{R_p} / \left[\frac{d\sigma}{dt} \right]_{R_p=0}$$

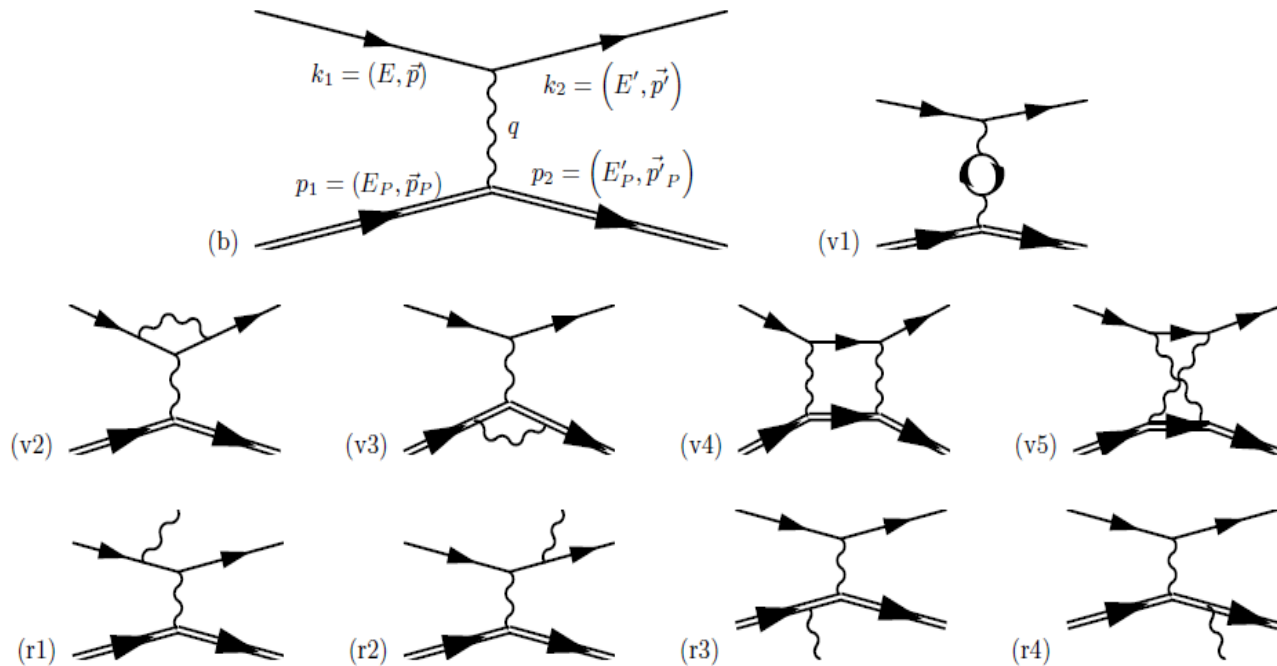


Difference in $d\sigma/dt$ between $R_p=0.84$ fm and $R_p=0.88$ fm
is only 1.3% at $Q^2 = 0.02 \text{ GeV}^2$

Measurement of $d\sigma/dt$ with point-to-point precision $\leq 0.2\%$

Radiative corrections

$$\left(\frac{d\sigma}{d\Omega}\right)_1 = \left(\frac{d\sigma}{d\Omega}\right)_0 (1 + \delta).$$



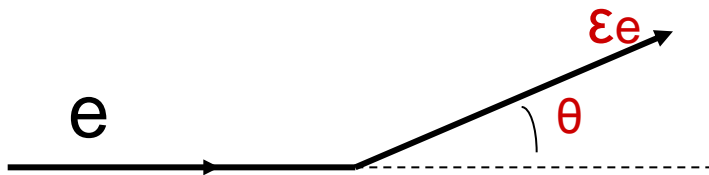
Absolute normalization of $d\sigma/dt$ with $\leq 0.2\%$ precision

Requirements to new generation measurements of proton radius in ep scattering experiments

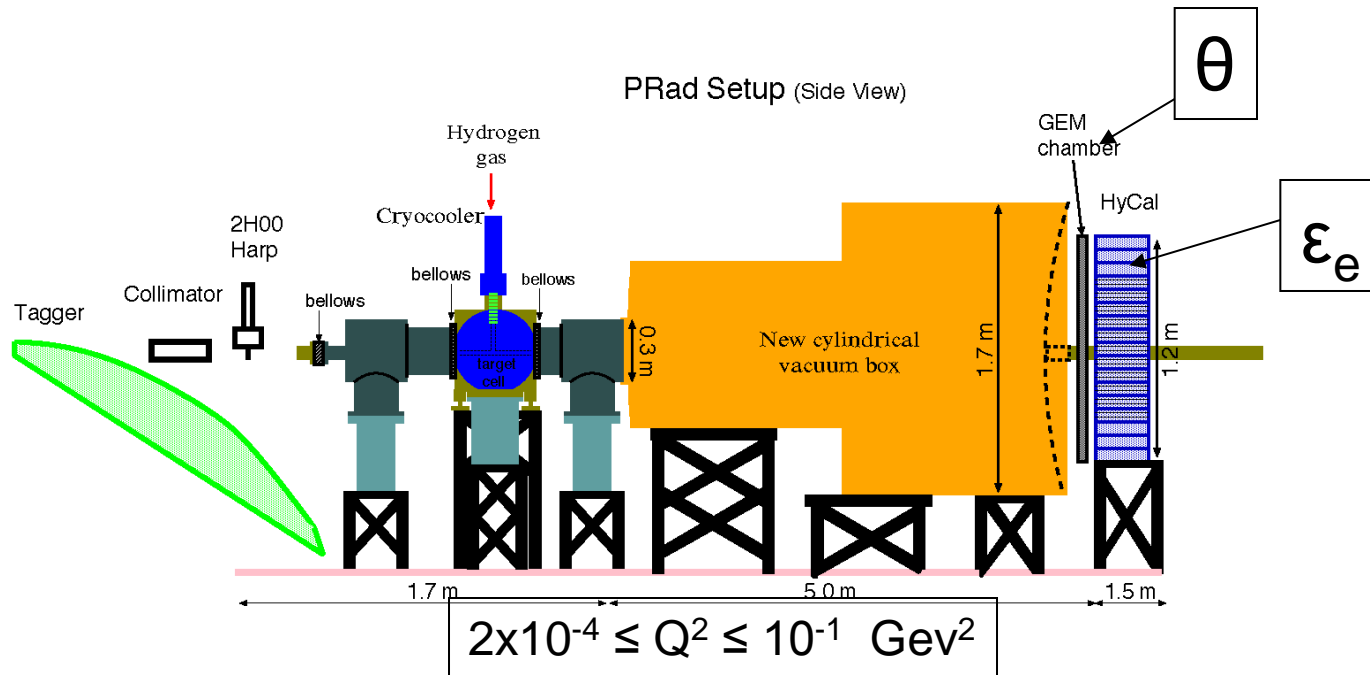
- Low transfer momentum region,
 $0.001 \text{ GeV}^2 \leq Q^2 \leq 0.02 \text{ GeV}^2$
- High resolution in Q^2 ;
- Point-to-point precision $\leq 0.2\%$
- Absolute normalization of $\leq 0.2\%$

Experiment PRad (Proton Radius)

Jefferson Lab



$$-t = \frac{4\epsilon_e^2 \sin^2 \frac{\vartheta}{2}}{1 + \frac{2\epsilon_e}{M} \sin^2 \frac{\vartheta}{2}}$$



Absolute normalization via ee-scattering

Goals of the proposed experiment

- Measurement of $d\sigma/dt$ in the Q^2 range 0.002 – 0.02 (0.04) Gev^2 ;
- High resolution in Q^2 (~100 resolved points);
- 0.1% point -to-point precision in $d\sigma/dt$;
- 0.2 % absolute precision in $d\sigma/dt$.

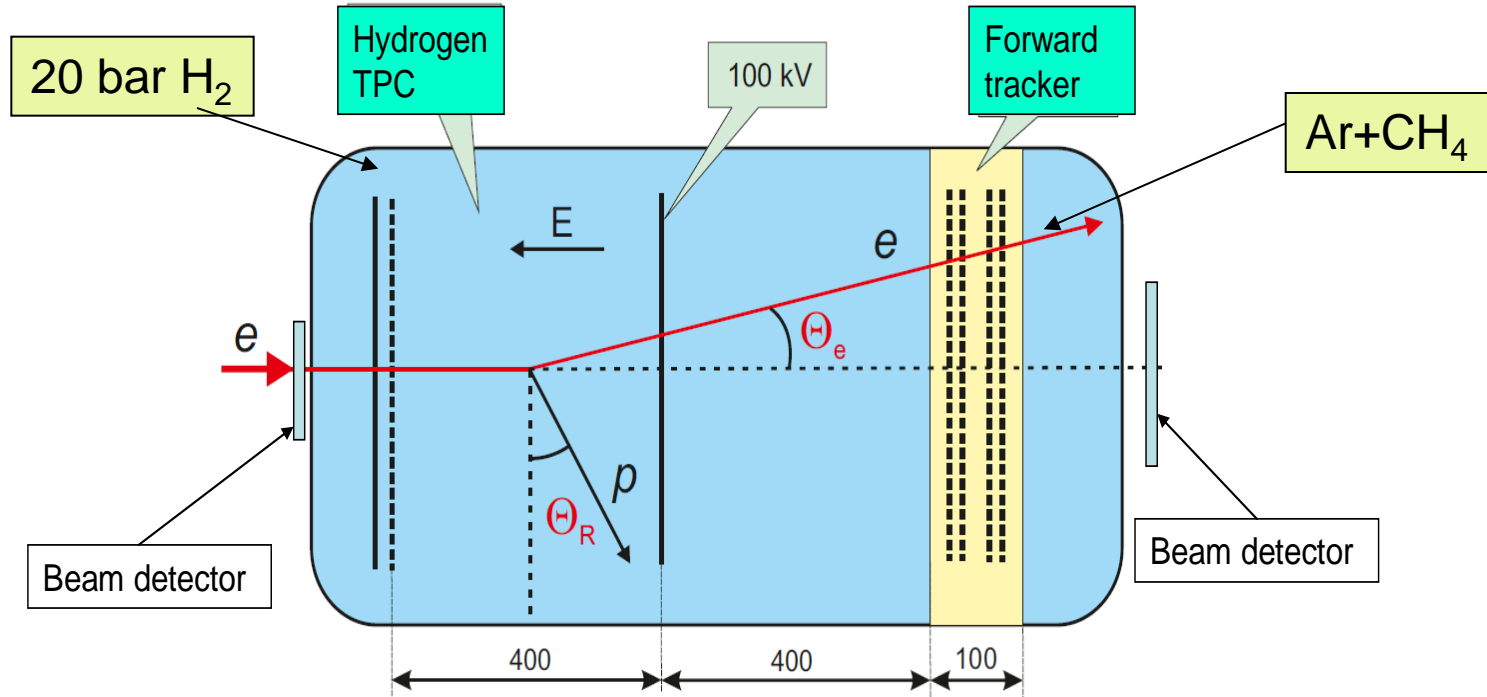
This allows to measure the proton radius with ± 0.005 fm precision
and distinguish the two options (0.877 fm and 0.841 fm)
on a 7σ confidence level

In comparison with PRad experiment:

Different systematical errors. Much lower Radiative corrections.

These two experiments will be complementary to each other.

Recoiled proton @ Scattered Electron Detector



Measured quantities:

Recoil energy T_R

Recoil angle Θ_R

Vertex **Z** coordinate

E scattering angle Θ_e

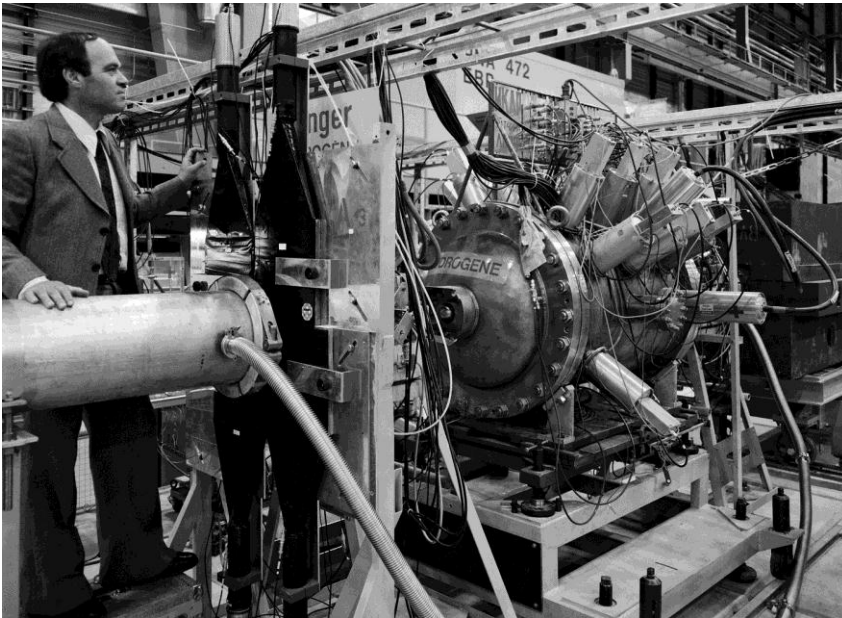
$$-t = \frac{4\epsilon_e^2 \sin^2 \frac{\vartheta}{2}}{1 + \frac{2\epsilon_e}{M} \sin^2 \frac{\vartheta}{2}}$$

$$-t = 2MT_R$$

$$\sin(q_R) = \frac{(e_e + M)T_R}{P_e P_R}$$

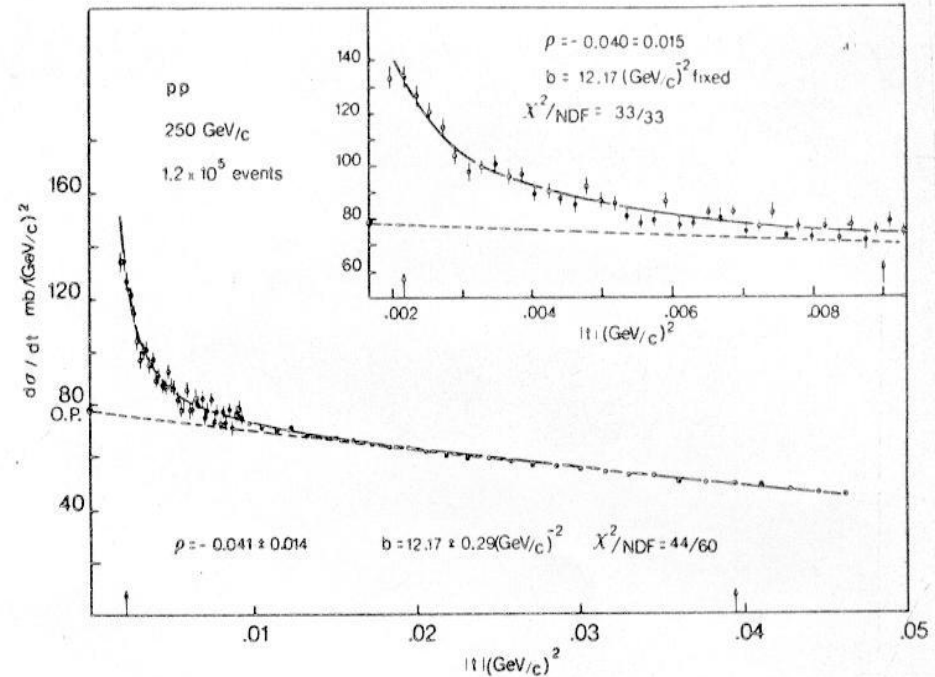
The proposed experiment is based on
the recoiled proton detection method
 which was used in WA9 and NA8 experiments
 at CERN to measure small angle pp- and $\pi\pi$ - scattering.

Nuclear Physics B217 (1983) 285-335



Recoiled proton detector ICAR at CERN

H₂ 10 bar TPC



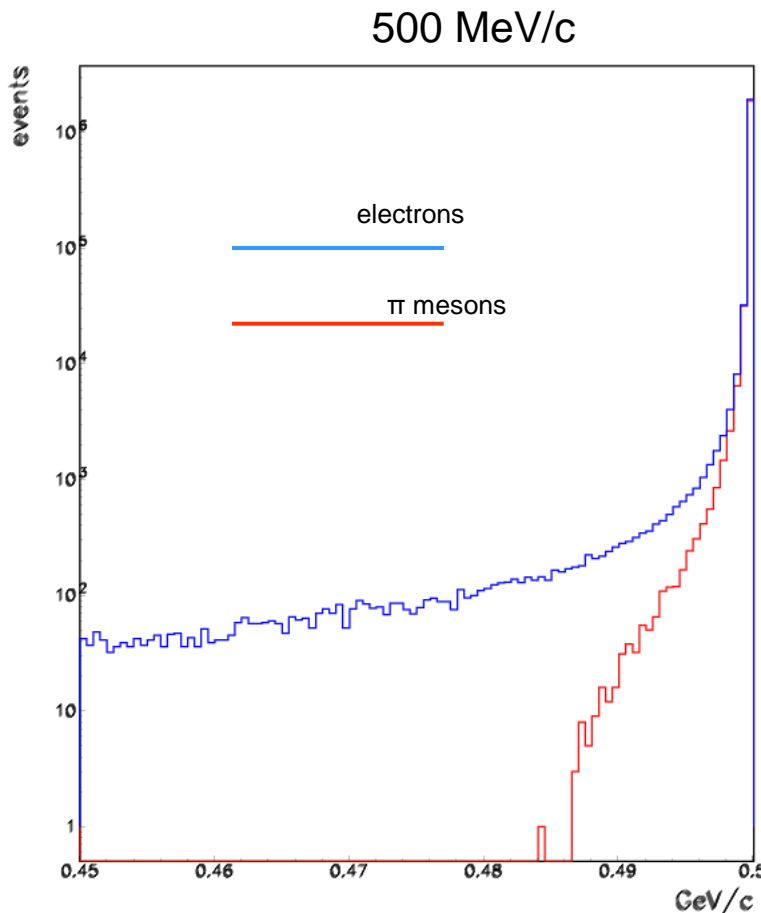
If compared with WA9/NA8 experiments

- Higher pressure from 10 bar to 20 bar
- Larger diameter from 400 mm to 600 mm
- Higher precision in $d\sigma/dt$ measurements
relative and absolute factor of 5.

Some advantages of the recoil method in measurements of the ep elastic scattering cross sections

- High resolution in low Q^2 -region;
- Direct measurement of Q^2 ($Q^2 = 2MT_R$) independently on the electron energy.
- No wall effects;
- Well determined gas target length;
- Close to 100% detection efficiency (under control):
- Precision absolute measurement of $d\sigma/dt$.
- Much smaller radiative corrections.

$$\frac{d\sigma}{dt} = \frac{\pi\alpha^2}{t^2} \left\{ G_E^2 \left[\frac{(4M + t/\epsilon_e)^2}{4M^2 - t} + \frac{t}{\epsilon_e^2} \right] - \frac{t}{4M^2} G_M^2 \left[\frac{(4M + t/\epsilon_e)^2}{4M^2 - t} - \frac{t}{\epsilon_e^2} \right] \right\}$$



$$-t = 2MT_R$$

T_R determines $d\sigma/dt$ with very little dependence on the electron energy losses before the collision

$$d\sigma_t/\sigma_t = +0.005 dP/P$$

$$T_R = 1\text{MeV},$$

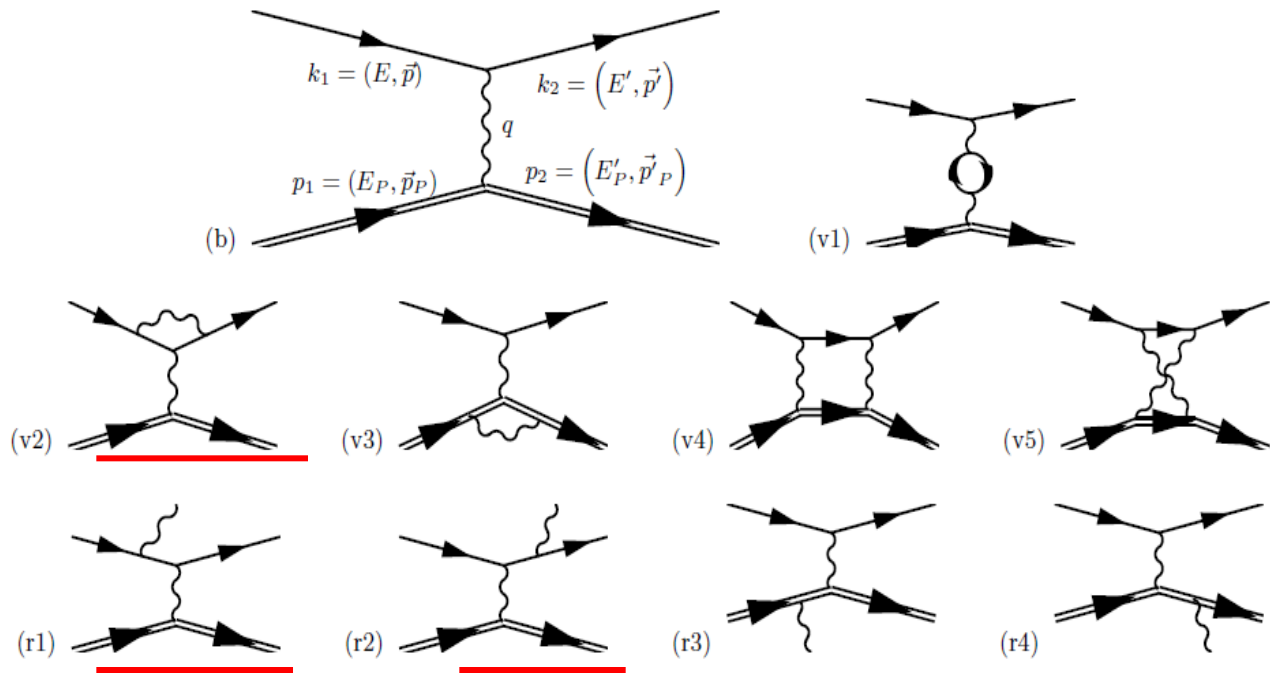
$$d\sigma_t/\sigma_t = +0.05 dP/P$$

$$T_R = 10\text{MeV}$$

$$\sigma_t = d\sigma/dt$$

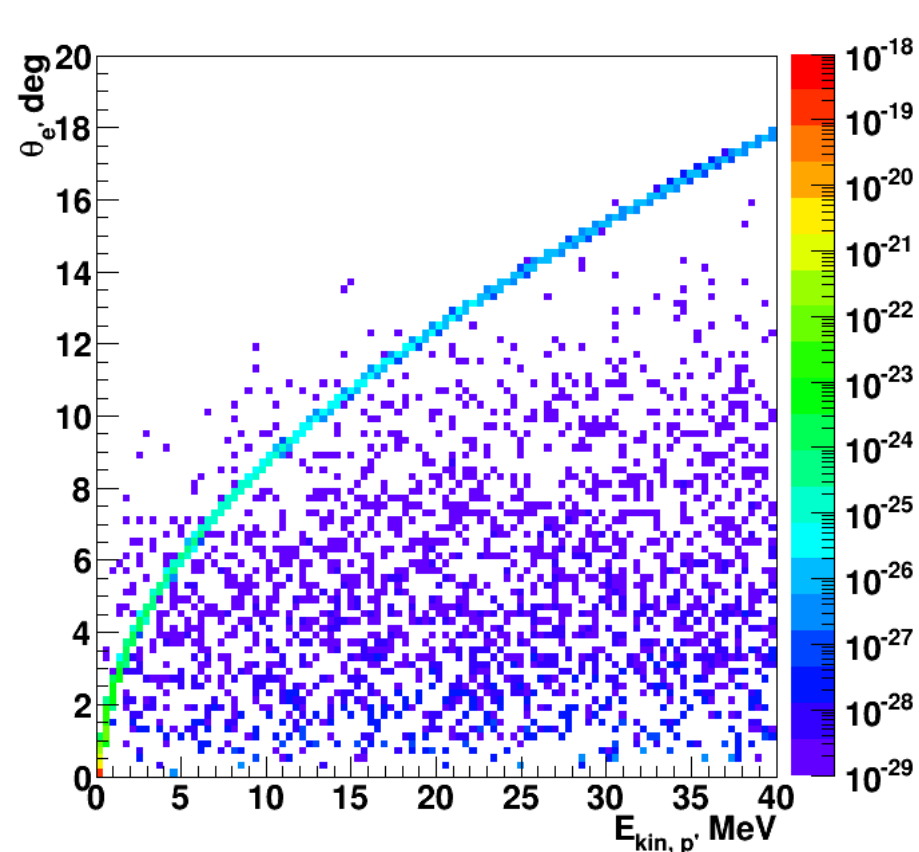
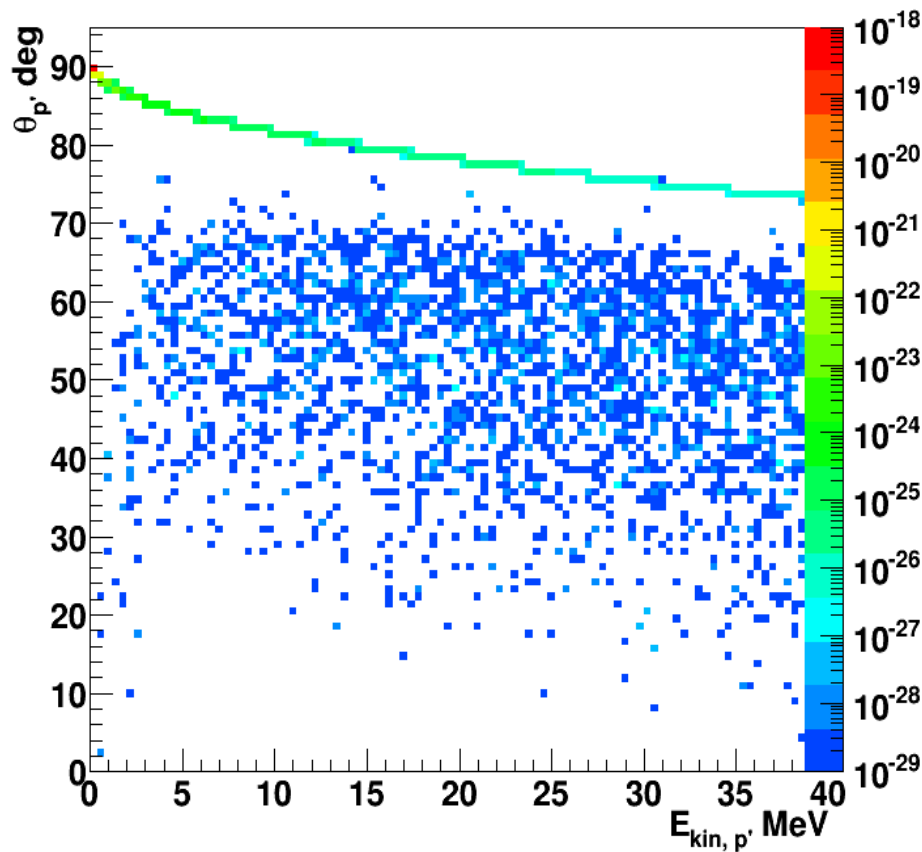
Radiative corrections

$$\left(\frac{d\sigma}{d\Omega}\right)_1 = \left(\frac{d\sigma}{d\Omega}\right)_0 (1 + \delta).$$



Experts on RC A.Arbusov and A. Gramolin (group of V.Fadin) agreed to calculate the radiative corrections for our experiment

MC calculated $\theta_e - T_R$ and $\theta_R - T_R$ plots
calculated for the elastic ep scattering and for
the background reaction $ep \rightarrow ep\pi^0$ for $\epsilon_e = 900$ MeV.



Main experimental problem

High precision calibration of the recoiled proton energy scale.

In our experiment this calibration will be done with **0.04 %** precision via the T_R - θ_e correlation relying on high precision (**0.02%**) linear scale of the Forward Tracker.

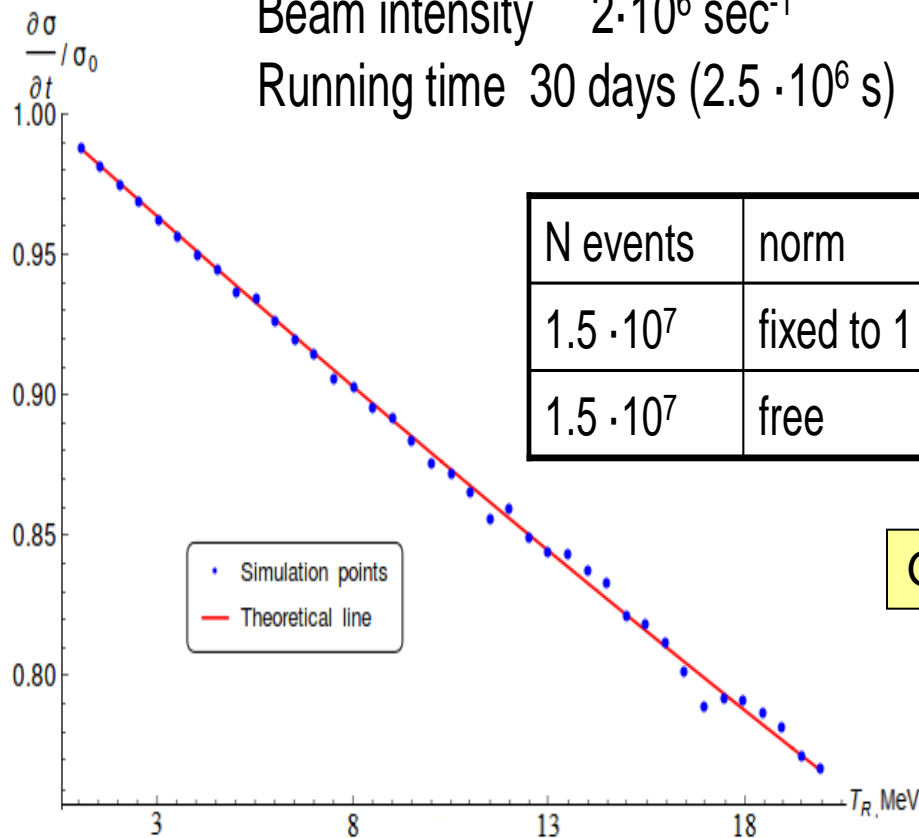
Statistics and beam time

Target thickness = $3.6 \cdot 10^{22}$ p/cm²

P = 20bar L = 35cm

Beam intensity $2 \cdot 10^6$ sec⁻¹

Running time 30 days ($2.5 \cdot 10^6$ s)



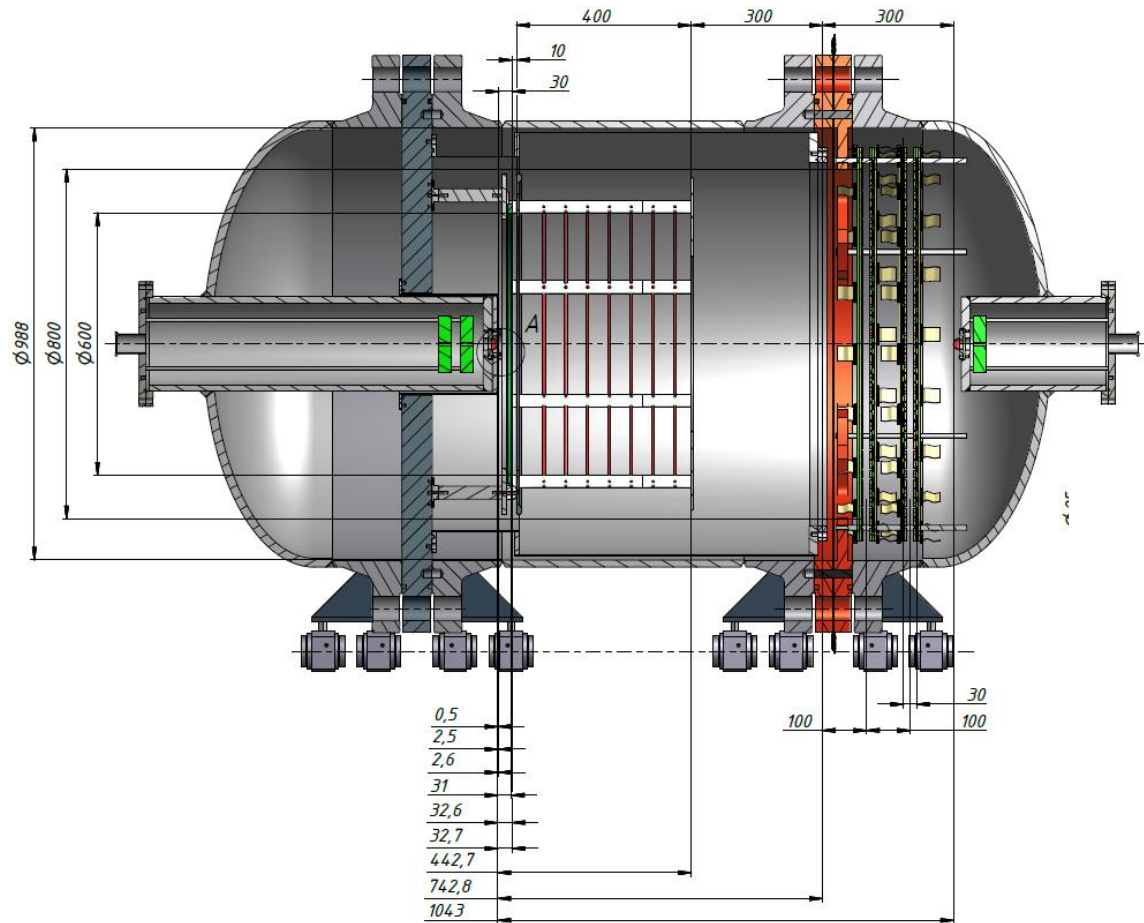
N events	norm	t-scale	$\sigma(Rp)$
$1.5 \cdot 10^7$	fixed to 1	fixed	± 0.002 fm
$1.5 \cdot 10^7$	free	fixed	± 0.003 fm

Goal : $\sigma(Rp) \leq 0.005$ fm

The systematic errors entering the measured $d\sigma/dt$

		Syst. Error %	comments
1	Drift velocity, $W1$	0.01	
2	High Voltage, HV	0.01	
3	Temperature, K	0.015	
4	Pressure, P	0.01	
5	H ₂ density, ρ_p	0.025	Sum of errors 3 and 4
6	Target length, L_{tag}	0.02	
7	Number of protons in target, N_p	0.045	Sum of errors 5 and 6
8	Number of beam electrons, N_e	0.05	Clean Tr0 free of pileups
9	Detection efficiency	0.05	
10	Electron beam energy, ϵ_e	0.02	
11	Electron scattering angle, θ_e	0.02	
12	t-scale calibration, T_R relative	0.04	Follows from error 11
13	t-scale calibration, T_R absolute	0.08	Follows from errors 11 and 10
	$d\sigma/dt$, relative	0.1	0.08% from error 12
	$d\sigma/dt$, absolute	0.2	0.16% from err.13 plus errors 7,8,9

Tentative design of the TPC& FT detector



MAMI and beam specifications

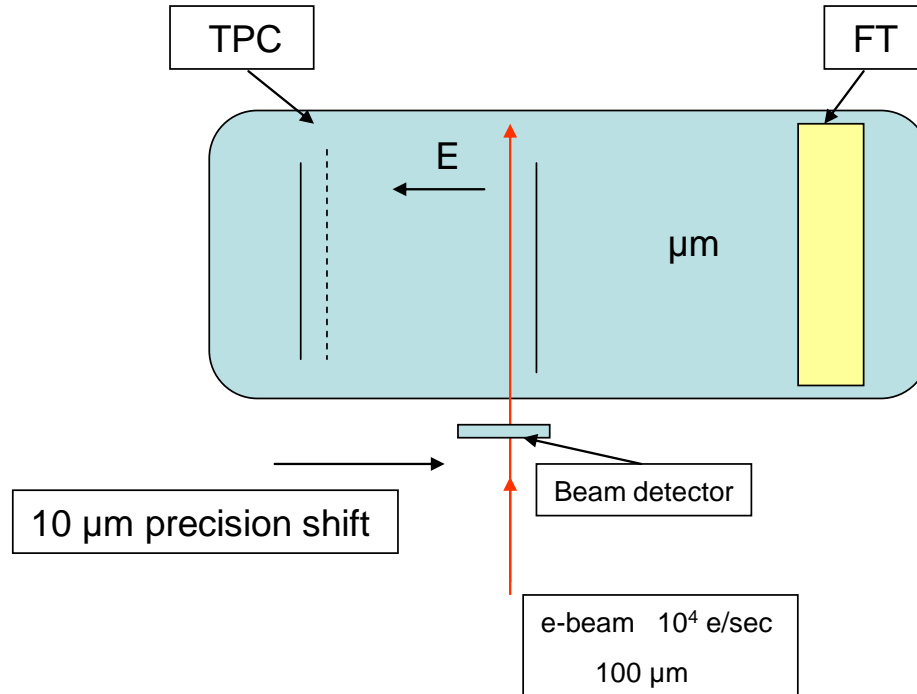
- **MAMI Specifications**

- Beam energy 500 MeV, 720 MeV
- Energy spread < 20 keV (1σ)
- Energy shift < 20 keV (1σ)
- Absolute energy $\leq \pm 150$ keV (1σ)

- **Electron Beam Specifications**

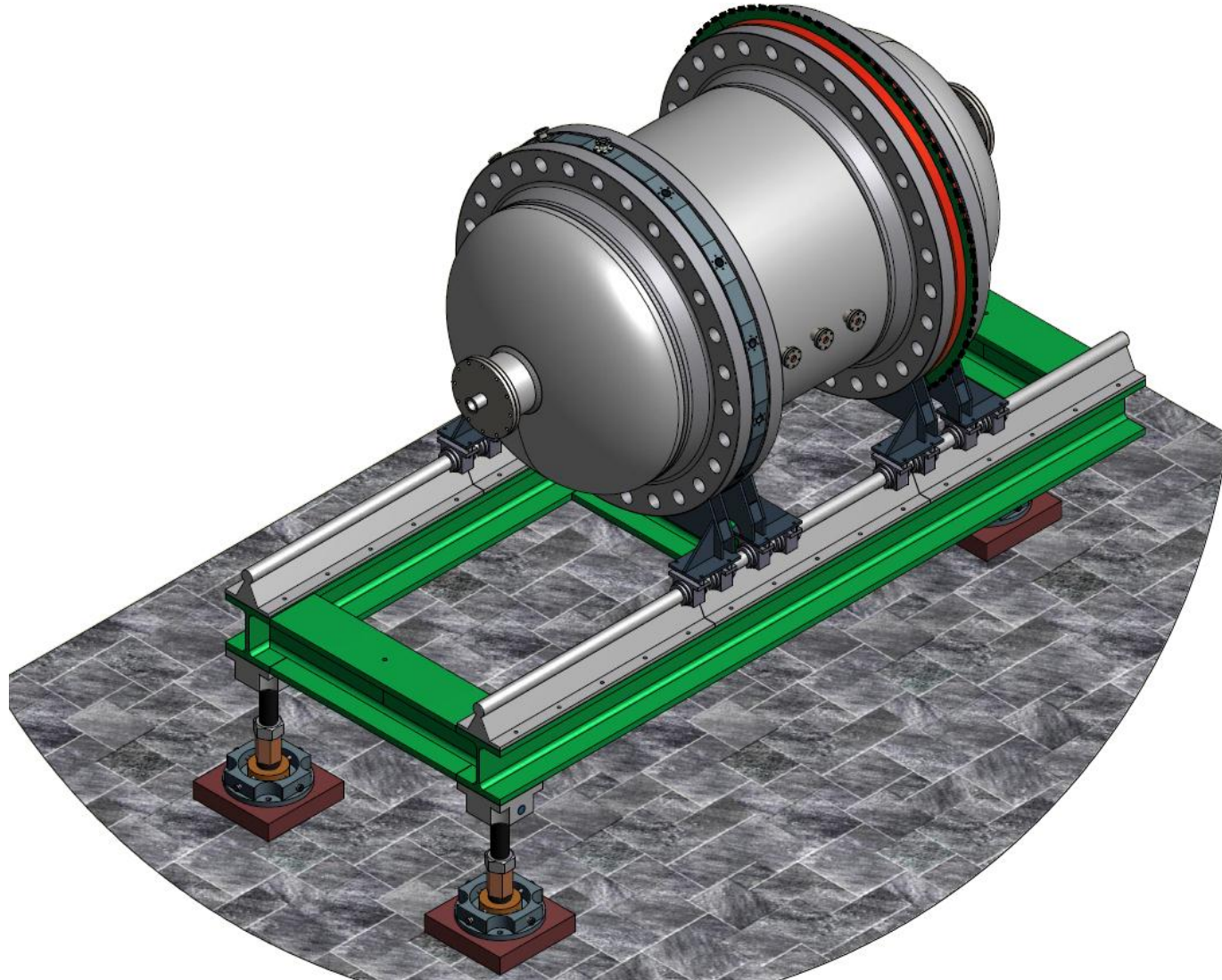
- Beam intensity (main run) 2×10^6 e/sec
- Beam intensity for calibration 10^4 e/sec and 10^3 e/sec
- Beam divergency ≤ 0.5 mrad
- Beam size ≤ 100 μm

Drift velocity measurement

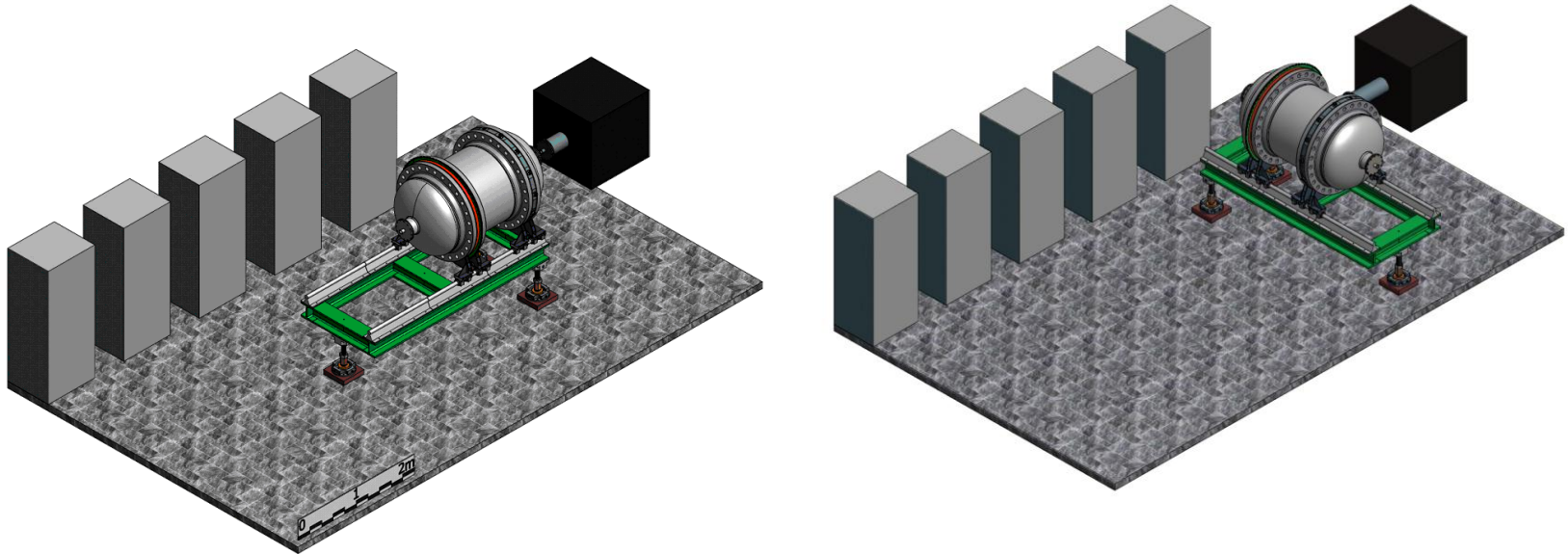


Precision in W measurements 0.01%

The TPC&FT detector on a movable platform.



Experimental layout for the physics run (Left panel)
and
for drift velocity measurements (Right panel).



The space for TPC platform 3m x 3m.

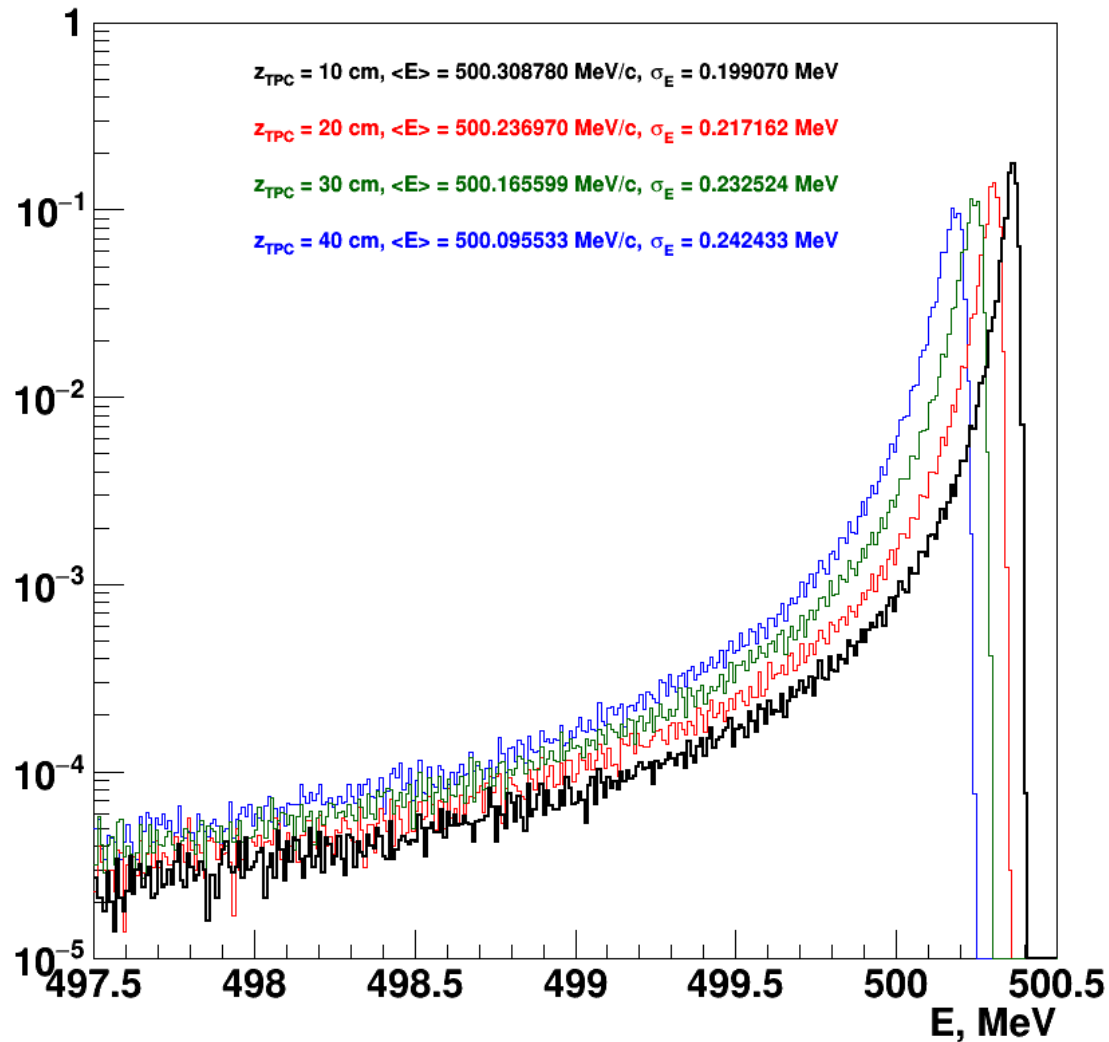
Five racks could be placed within 10 m from TPC.
Some space is needed outside to keep H₂ containers

Working plan

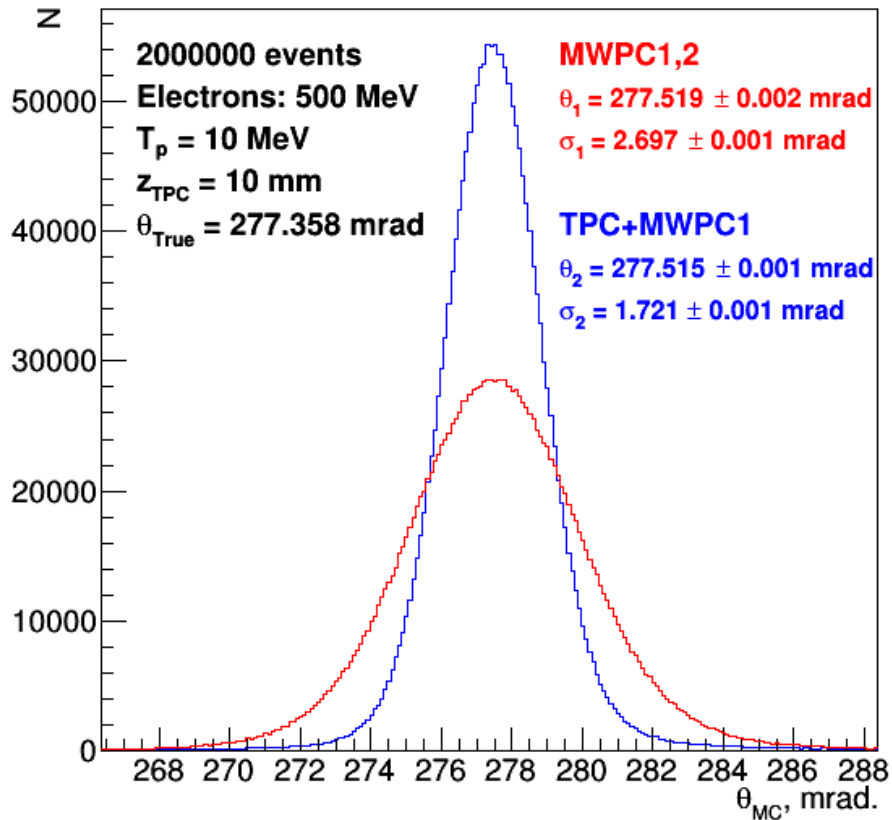
- 2017 Test experiment in the electron beam at MAMI with a TPC prototype **now available** at GSI.
Beam test equipment, TPC background
- 2018 Construction of the whole setup.
First physics run.

Thank you for your attention

Electron energy E^* in the collision point

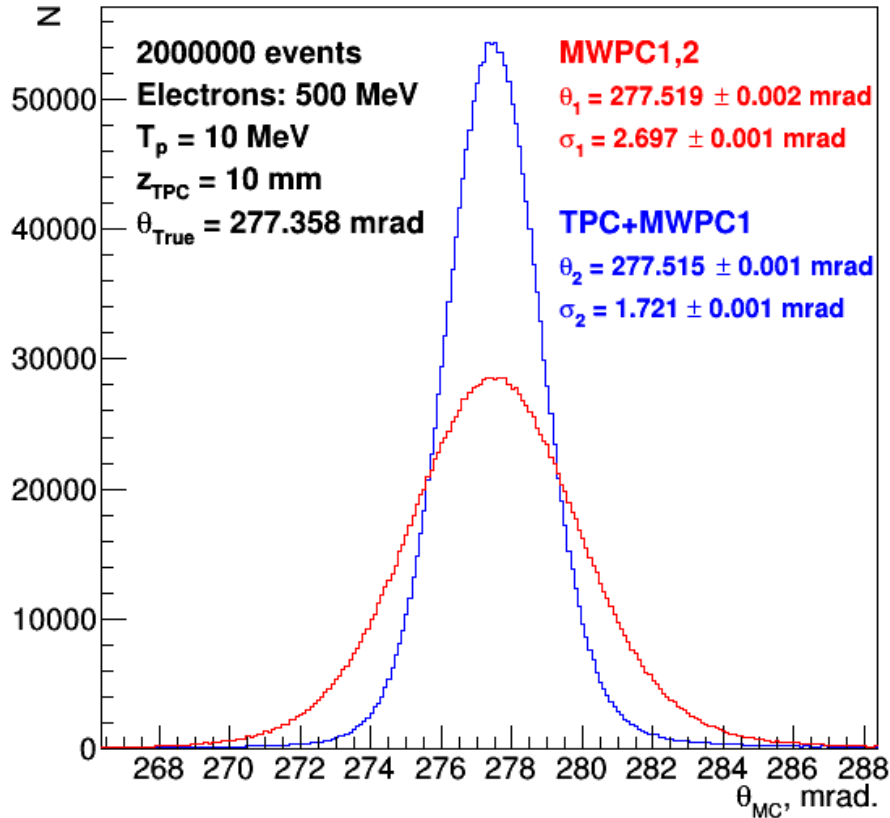


T_R scale calibration via T_R - θ_e correlation



$$T_R^*(E_0, \theta_e) / T_R = 1 + 1.2 \cdot 10^{-3}$$

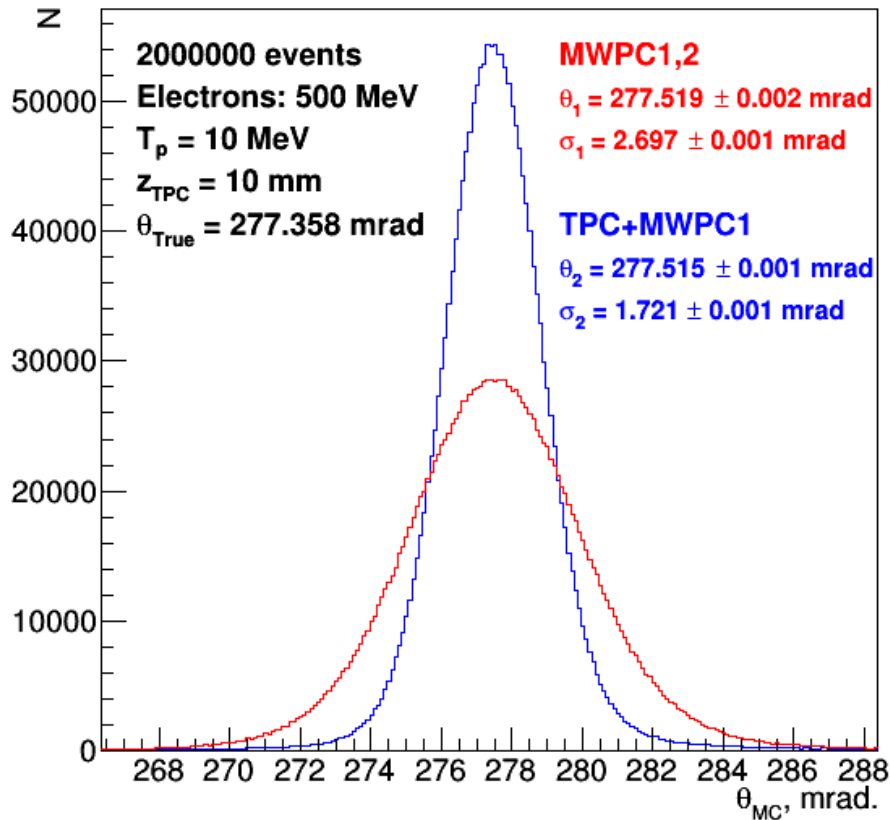
T_R scale calibration via T_R - θ_e correlation



$$T_R^*(E_0, \theta_e) / T_R = 1 + 1.2 \cdot 10^{-3}$$

$$T_R^*(E^*, \theta_e) / T_R = 1 + 3.8 \cdot 10^{-4}$$

T_R scale calibration via T_R - θ_e correlation



$$T_R^*(E_0, \theta_e) / T_R = 1 + 1.2 \cdot 10^{-3}$$

$$T_R^*(E^*, \theta_e) / T_R = 1 + 3.8 \cdot 10^{-4}$$

$$T_R^*(E^*, \theta_e^*) / T_R = 1 + 0.8 \cdot 10^{-4}$$

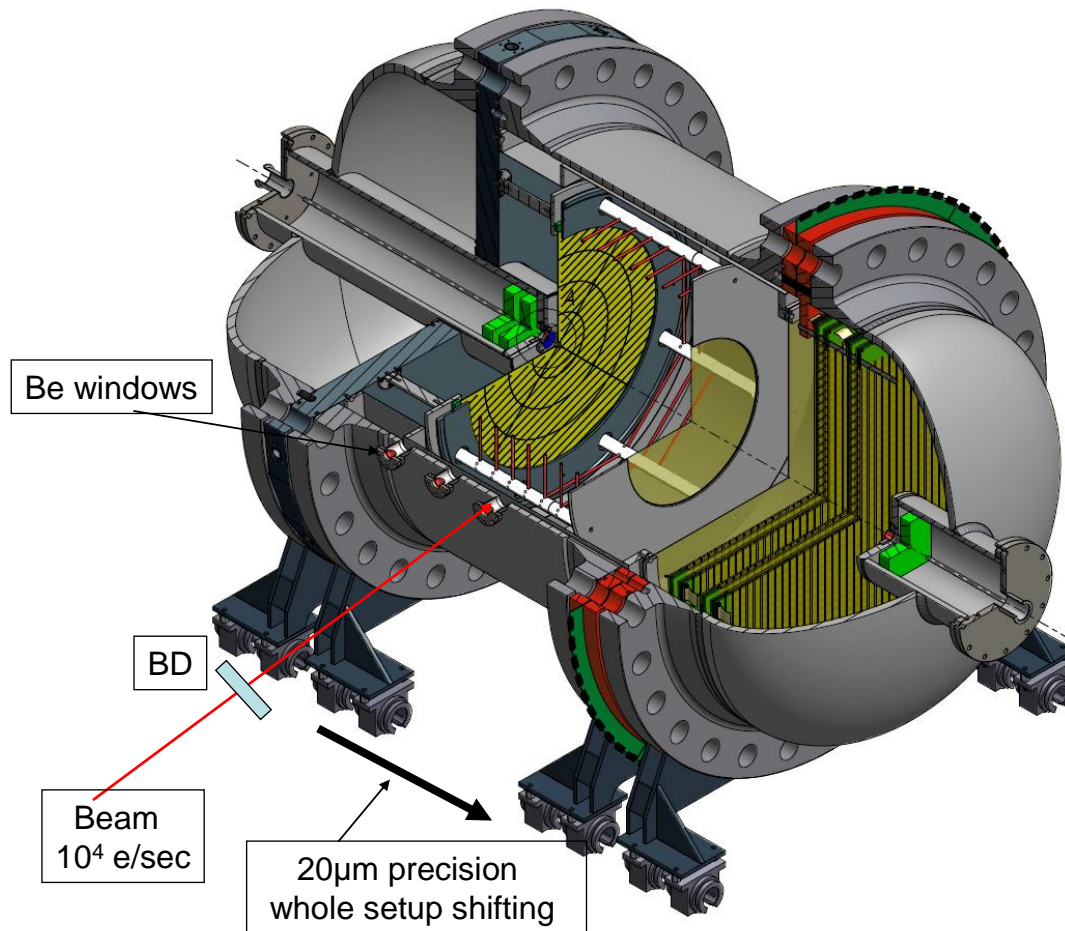
The TPC@FT detector
can be also used
to study

e-d, He scattering

μ -p,d,He scattering

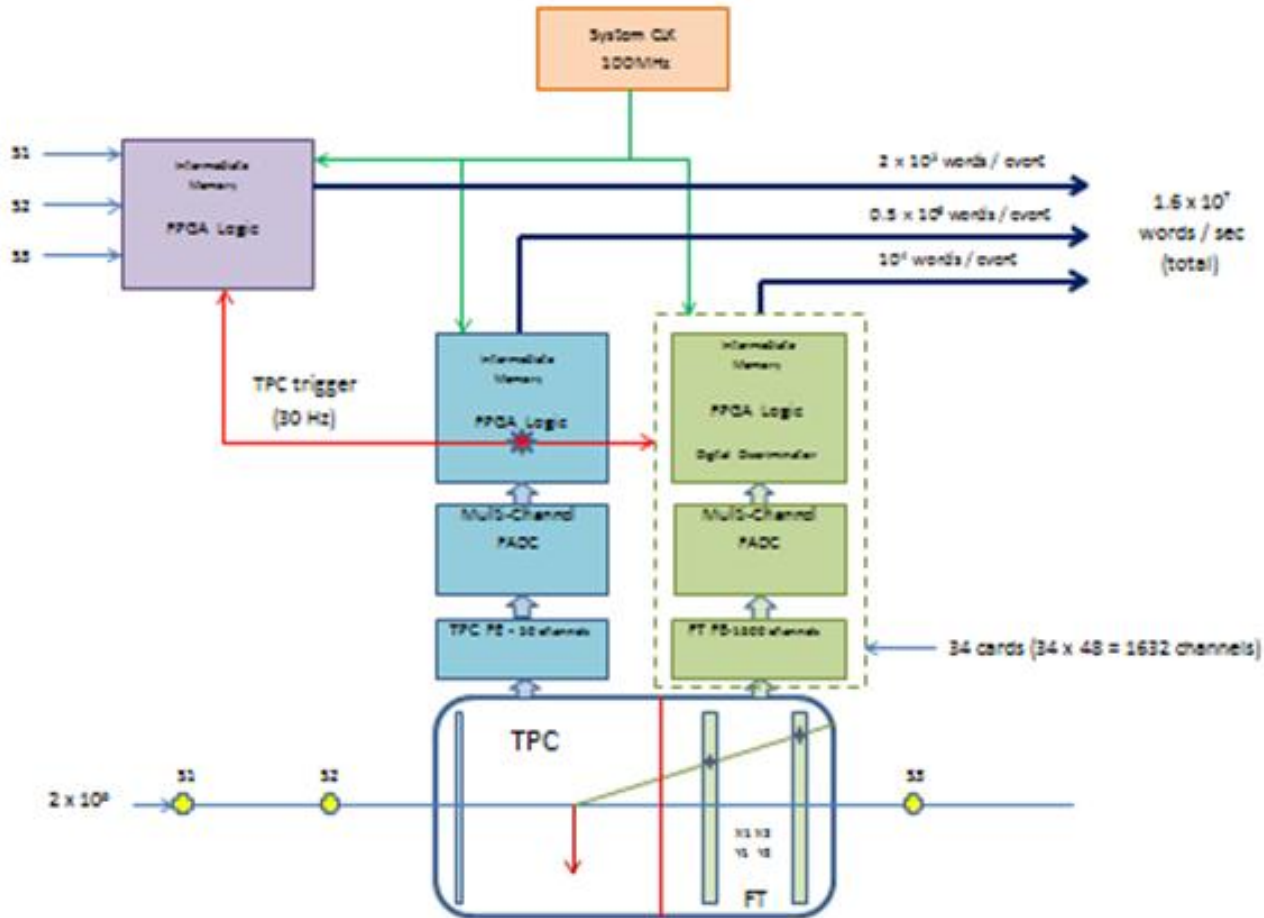
- Exotic nuclei –p,d,He scattering

Experimental layout for high precision measurement of electron drift velocity.

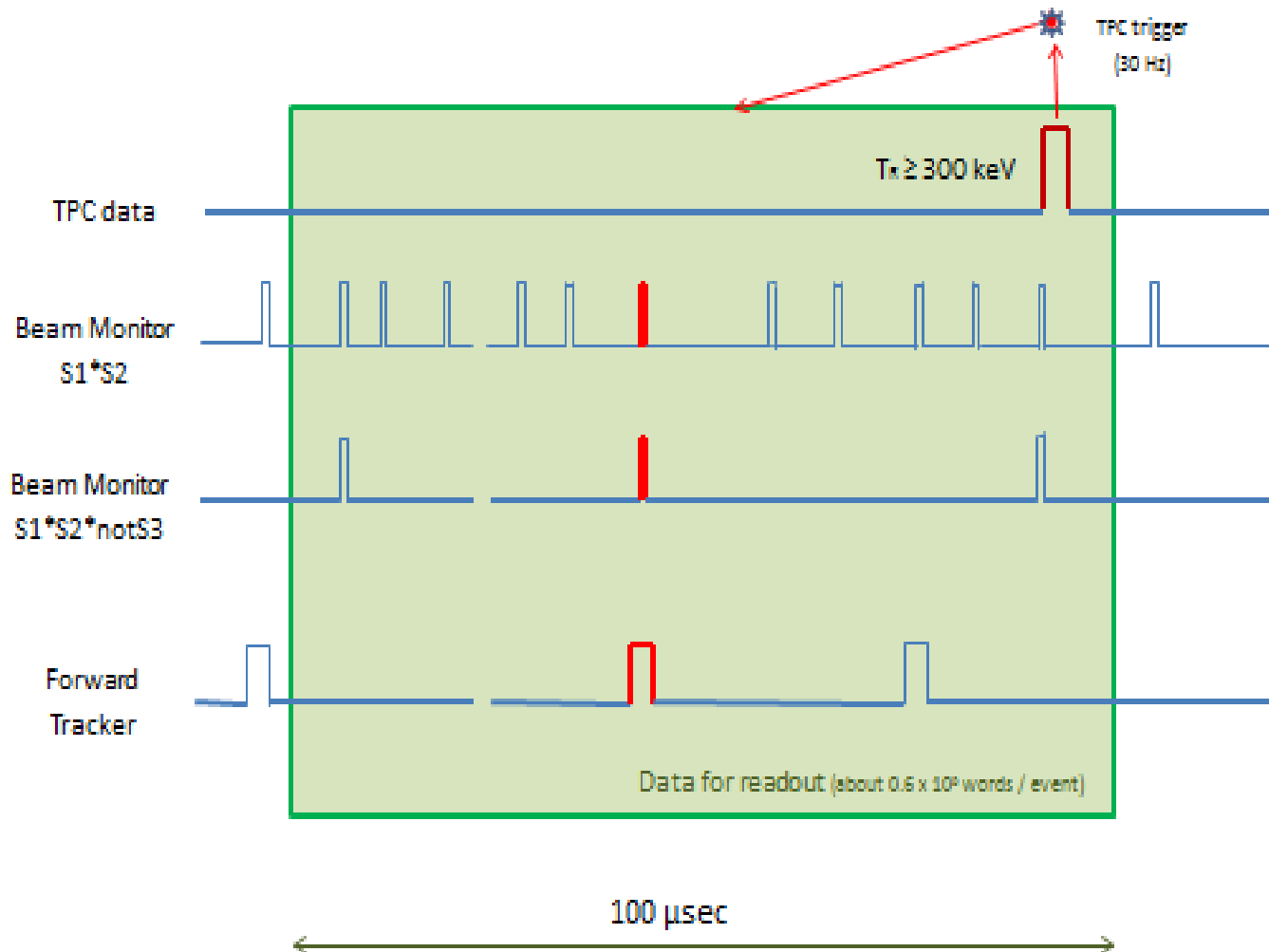


DAQ system

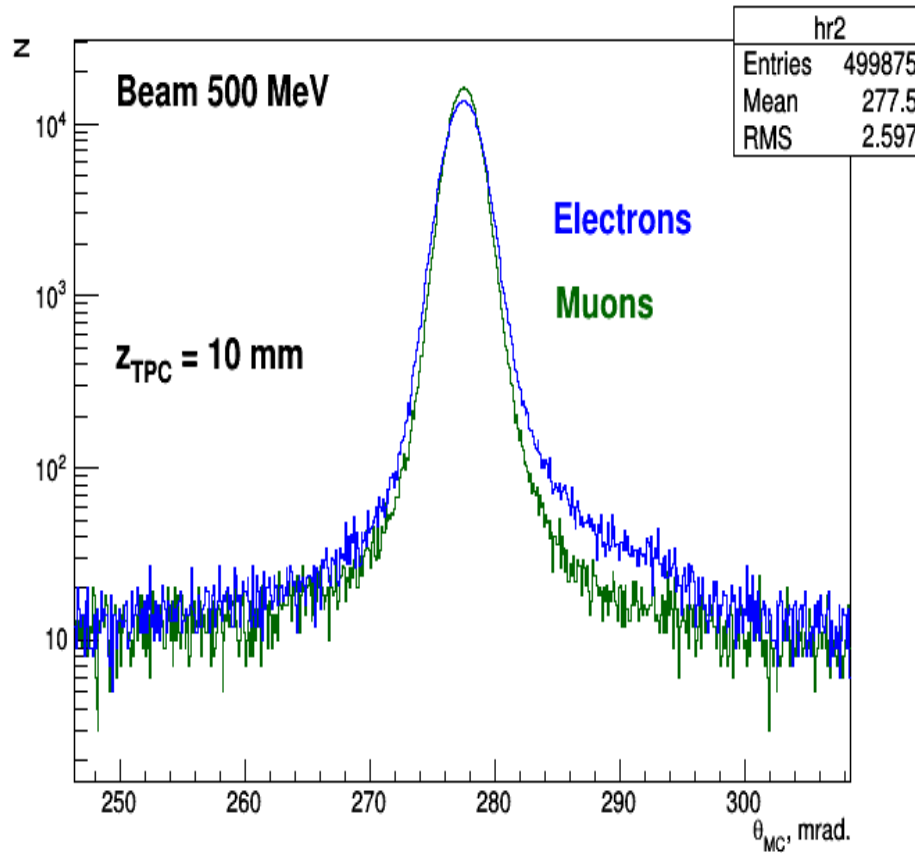
Continuous data flow . 100 MHz clock. T_R trigger



All data from 100 μs interval before T_R trigger are sent to memory without introducing any dead time in data acquisition.



θ_e^* corrected for the radiation tail



$$\theta_e = 277.514 \text{ mrad}$$
$$\theta_e^* = 277.471 \text{ mrad}$$

Fig. 15. Schematic view of the ACTAR2 prototype (side view).

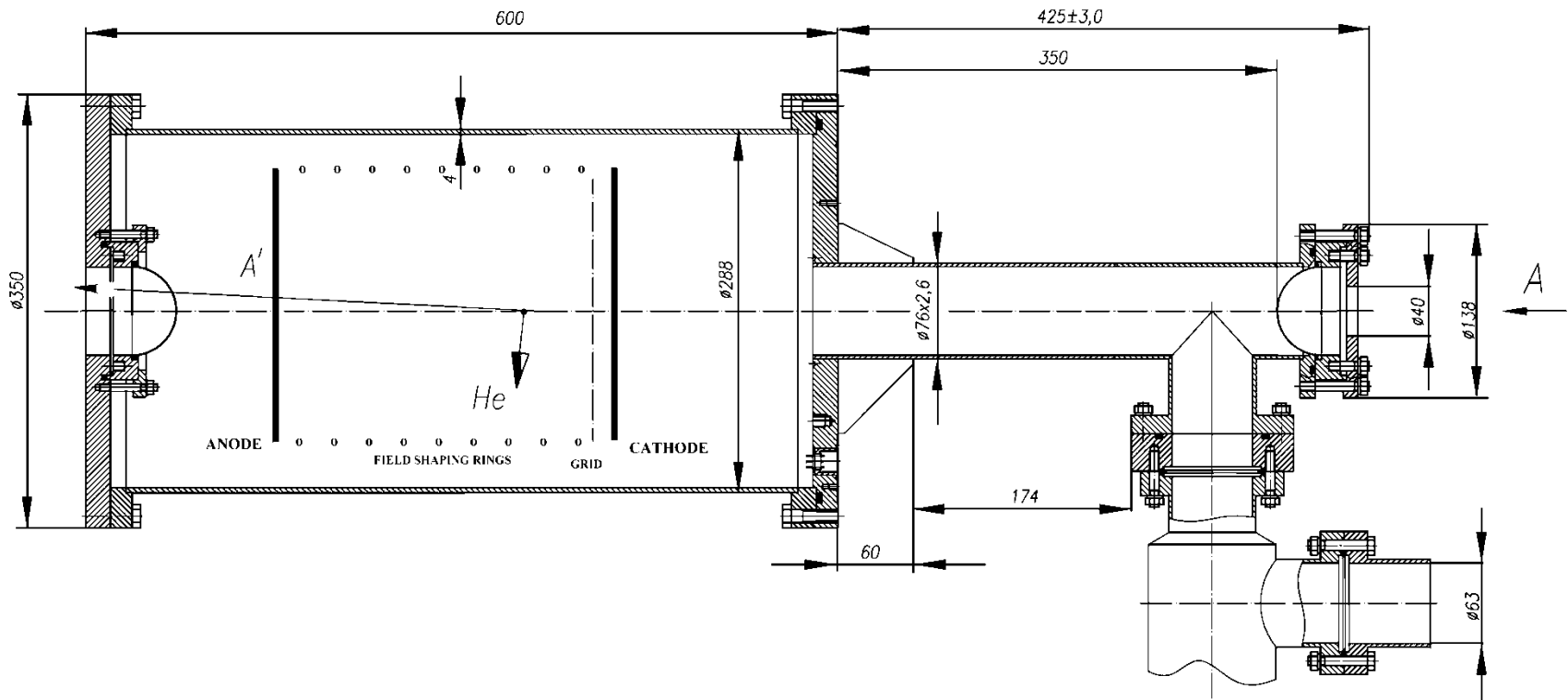
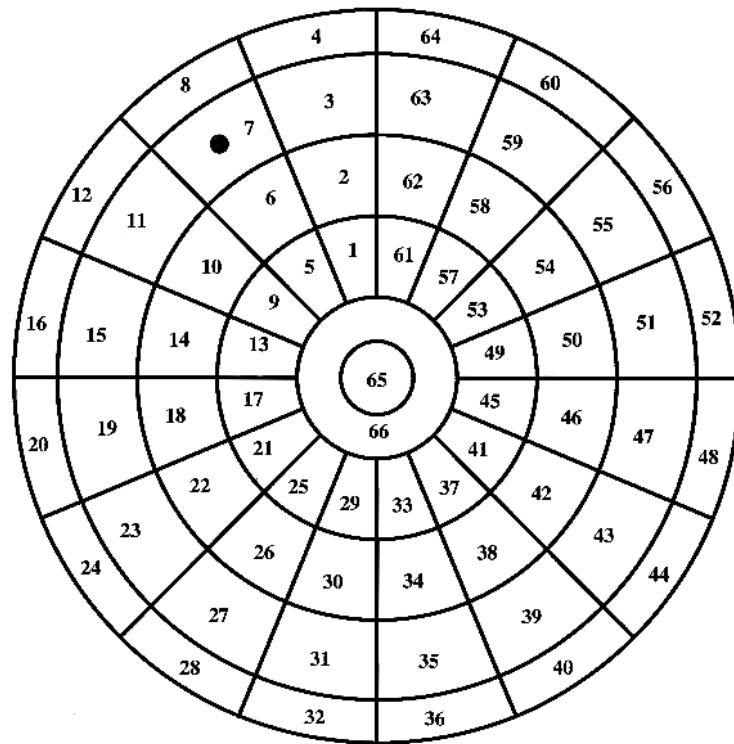
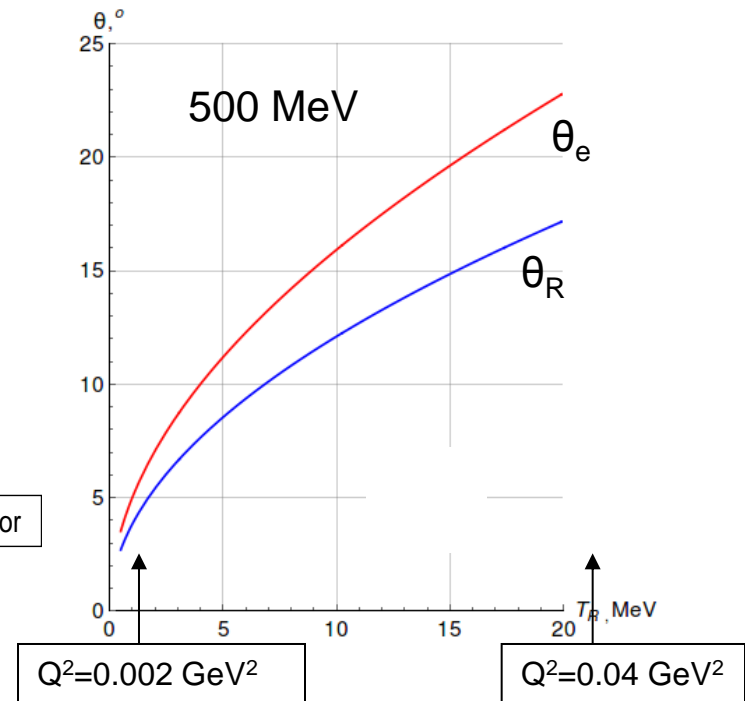
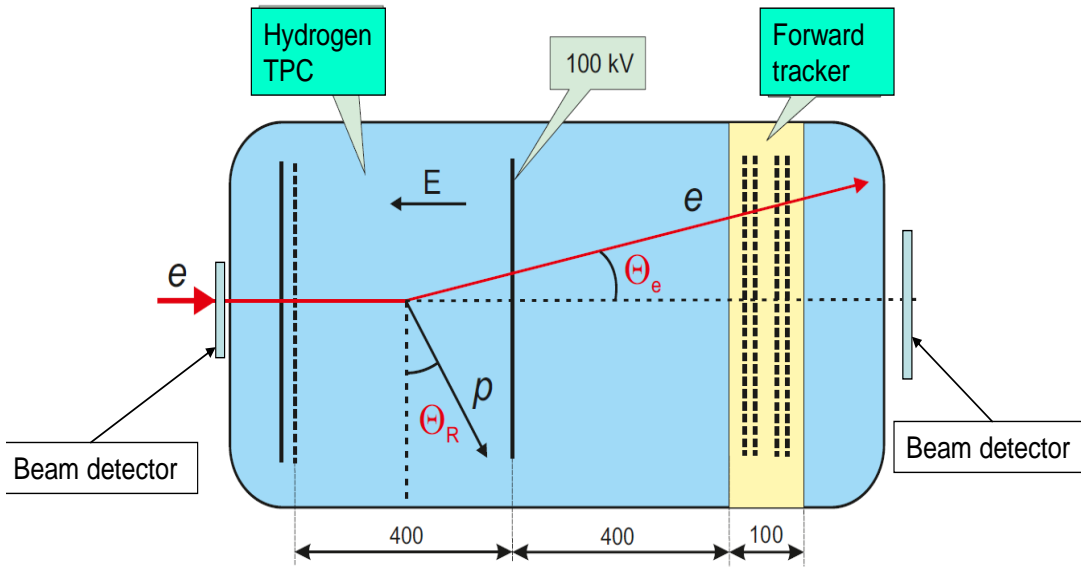


Fig.16. Layout of the ACTAR2 prototype anodes. An ^{241}Am α -source is deposited on the cathode of the chamber opposite to the black spot on the anode number 7. The outer diameter of the anodes is 200 mm.



TPC@ FT detector

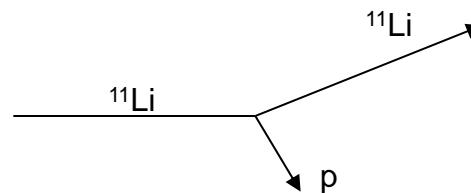
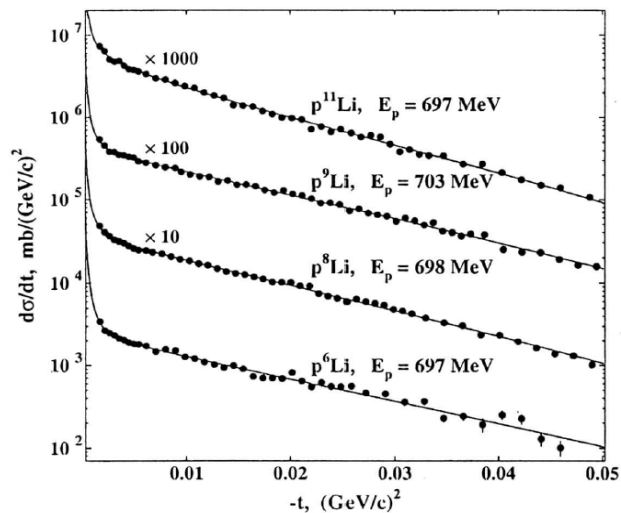


Experiment is designed for $\varepsilon_e = 500 - 900 \text{ MeV}$
 $\Theta_e \text{ max} = 25 \text{ deg.}$

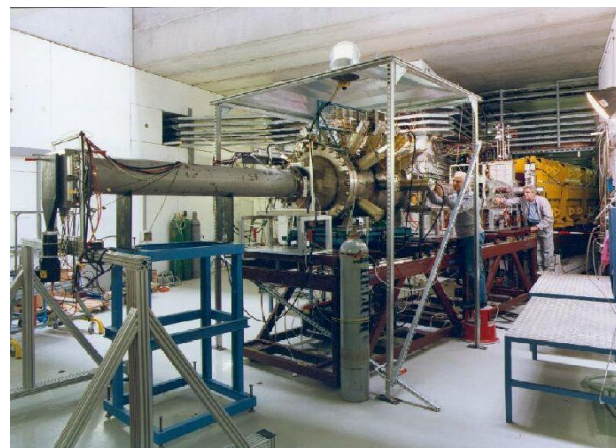
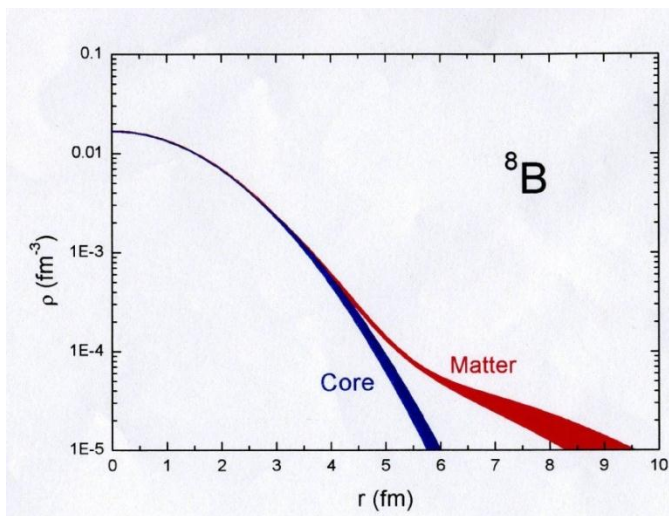
TPC and FT are in common body at 20 bar pressure
 TPC: extra-pure H_2 , FT: $\text{Ar}+\text{CH}_4$

Study of elastic scattering of exotic nuclei on proton

Nuclear Physics A766 (2006)1-24



^4He , ^6He , ^8He
 ^6Li , ^8Li , ^9Li , ^{11}Li
 ^7Be , ^9Be , ^{10}Be , ^{11}Be , ^{12}Be , ^{14}Be
 ^8B
 ^{13}C , ^{14}C , ^{15}C , ^{17}C .



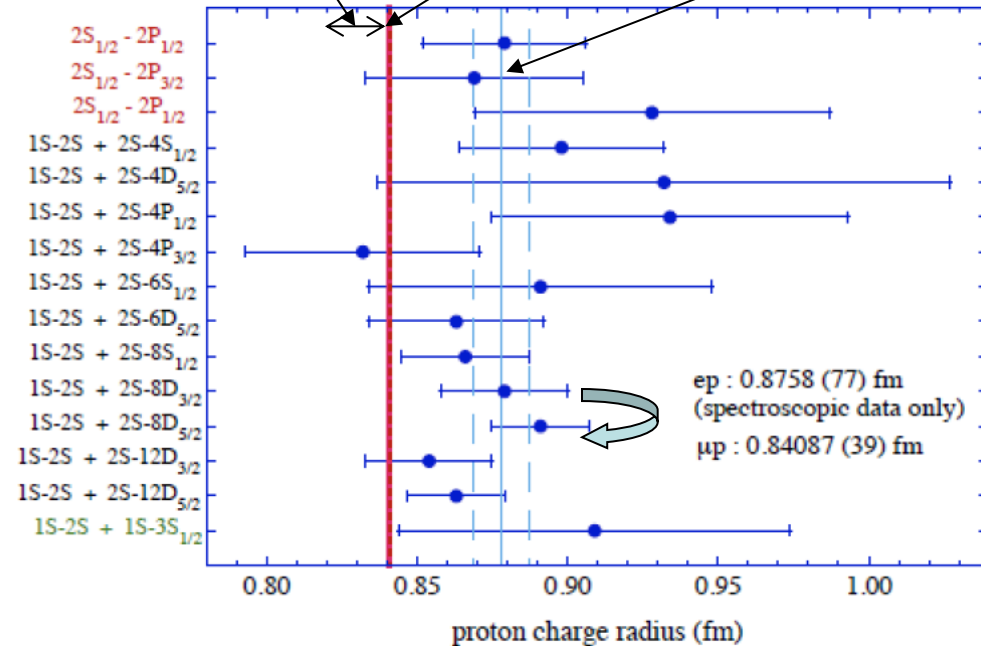
ICAR at GSI

New measurement of 2S-4P in ep-atom Garching

New ep-atom result

μ p-data

Previous ep-data



Previous Garching-Paris data
 $R_p = 0.877(7)$
 $R_\infty = 10973731.568508(65) \text{ m}^{-1}$

New Garching-Garching data
 $R_p = 0.830(9)$
 $R_\infty = 10973731.568082(91) \text{ m}^{-1}$

If compared with WA9/NA8 experiments

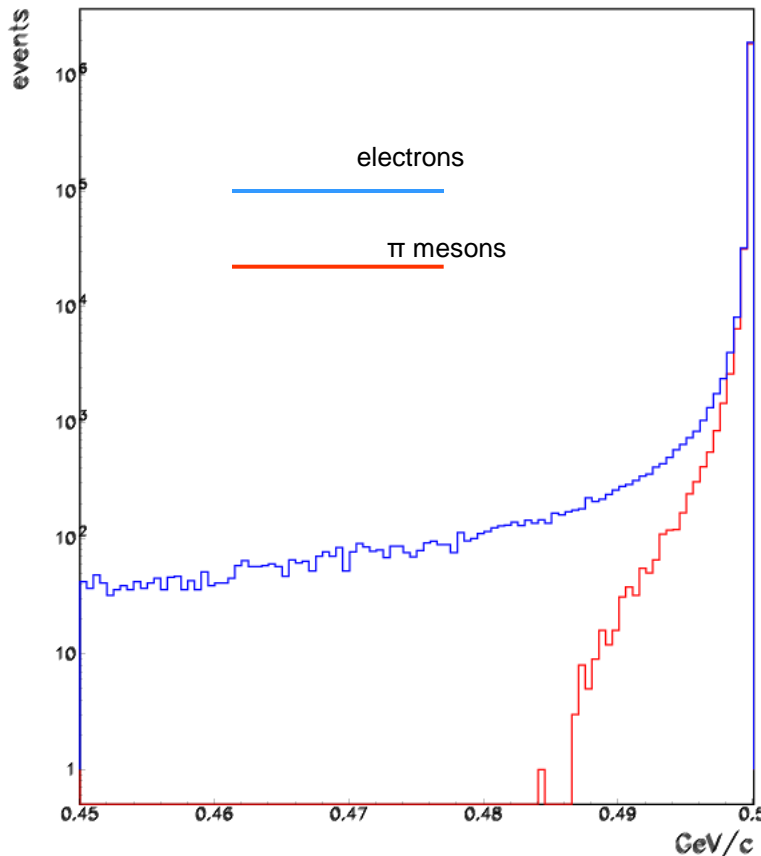
- Higher pressure from 10 bar to 20 bar
- Larger diameter from 200 mm to 300 mm
- Higher precision in $d\sigma/dt$ measurements
relative and absolute factor of 5.

Some advantages of the recoil method in measurements of the ep elastic scattering cross sections

- High resolution in low Q^2 -region;
- **Direct measurement of Q^2** ($Q^2 = 2MT_R$) independently on the electron energy.
- No wall effects;
- Well determined gas target length;
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- **Much smaller radiative corrections.**

$$\frac{d\sigma}{dt} = \frac{\pi\alpha^2}{t^2} \left\{ G_E^2 \left[\frac{(4M + t/\epsilon_e)^2}{4M^2 - t} + \frac{t}{\epsilon_e^2} \right] - \frac{t}{4M^2} G_M^2 \left[\frac{(4M + t/\epsilon_e)^2}{4M^2 - t} - \frac{t}{\epsilon_e^2} \right] \right\}$$

500 MeV/c



$$-t = 2MT_R$$

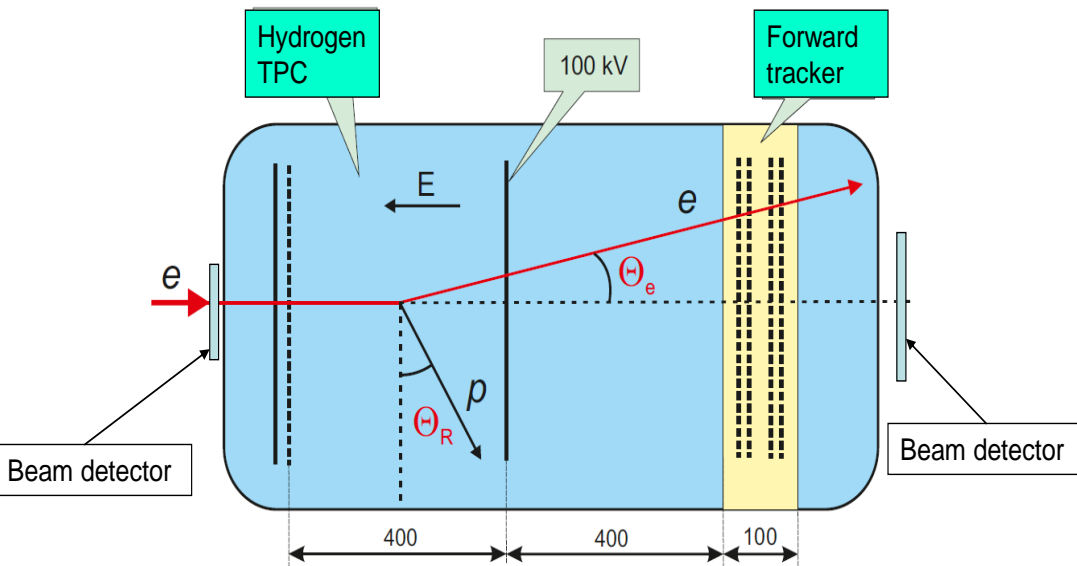
T_R determines $d\sigma/dt$ with very little dependence on the electron energy losses before the collision

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High precision calibration of the recoiled proton energy scale.

In our experiment this calibration will be done with **0.04 %** precision via the T_R - θ_e correlation relying on high precision (**0.02%**) linear scale of the Forward Tracker.

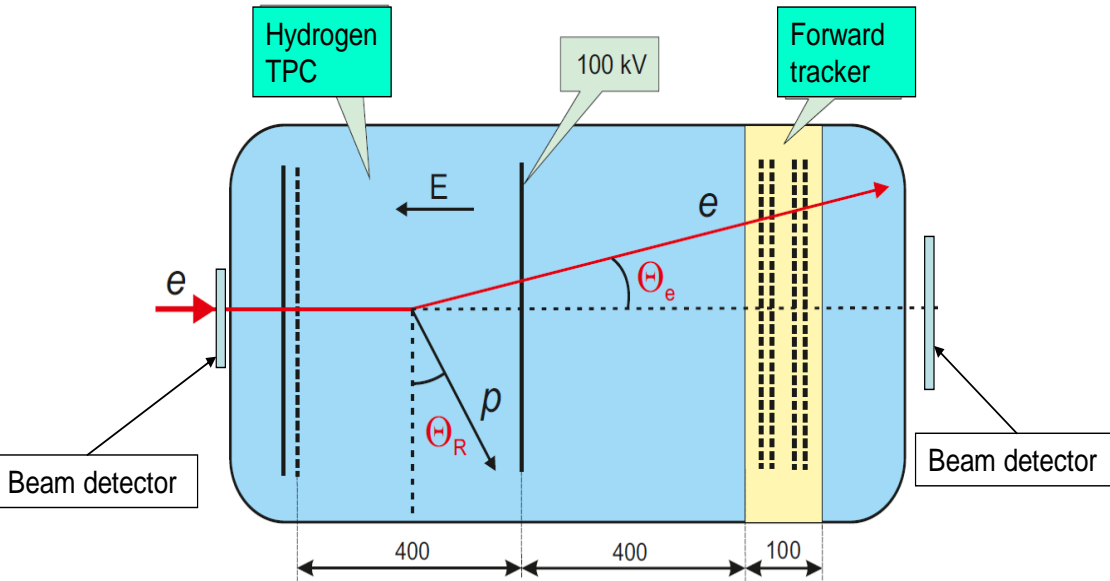
Hydrogen Time Projection Chamber



H_2 Pressure: 20 bar and 4 bar
 Drift velocity: 0.42 cm/ μ s
 Max drift time 100 μ s
 Gas impurities 10^{-6}

		Resolution, σ	
Recoil proton energy	T_R	60 KeV	$1\text{MeV} \leq T_R \leq 10\text{ MeV}$
Recoil proton angle	θ_R	15 mrad	Recoil range > 60 mm
Z of ep vertex	Z_V	200 μm	
Time arrival of TPC signals	t_{arr}	40 ns	

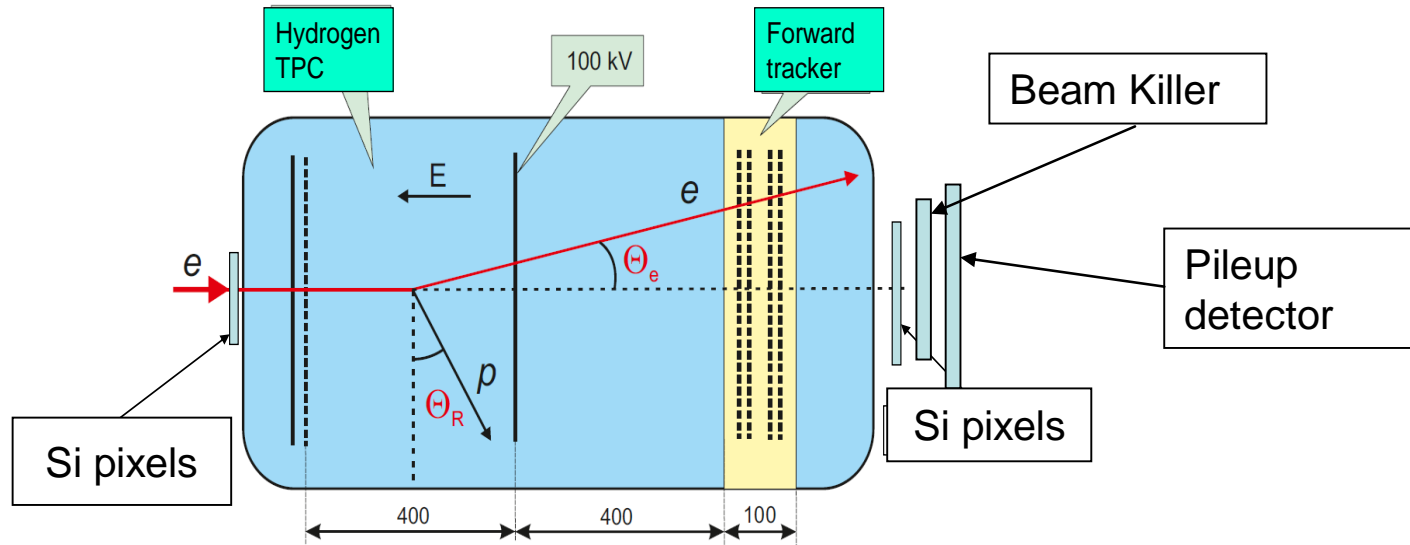
Forward Tracker



Two pairs of Cathode Strip Chambers X1/Y1 and X2/Y2.
Size: 600mm x 600 mm.
Strip width: 2mm.
Spatial resolution: **30 μm .**
Time resolution : **5 ns.**

Linear scale with 0.02 % absolute precision

Beam Detectors



Si-pixels 3x3 mm: Input trajectory $\sigma_x = \sigma_y = 30 \mu\text{m}$ Time resolution 10 ns
Beam Killer: SC counter 1 ns resolution
Pileup detector: SC counter 0.1 ns resolution

Beam intensity 2×10^6 electrons/sec