

# Production of a beam of tensor-polarized deuterons using a carbon target

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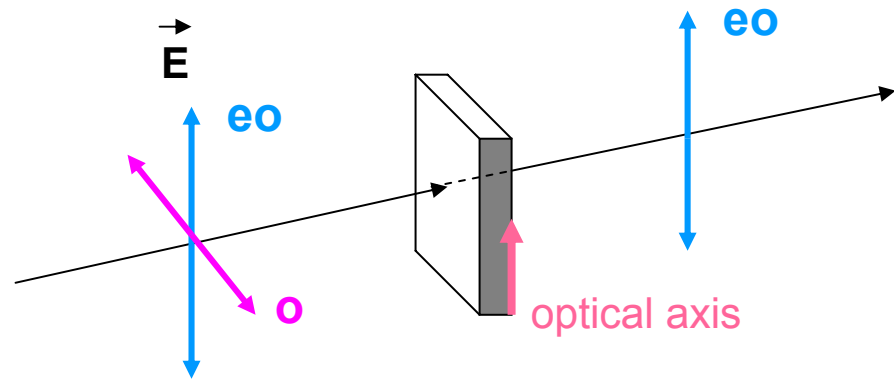
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## Introduction

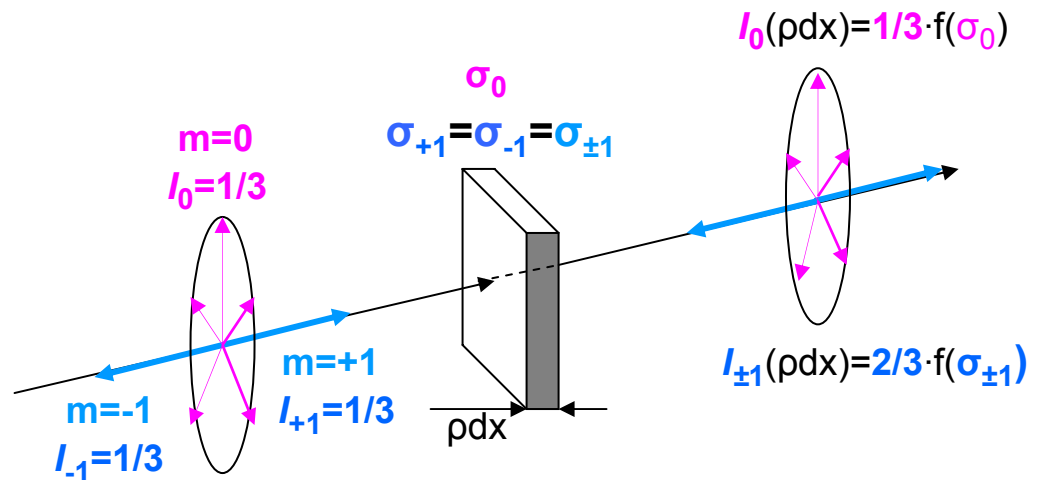
### Dichroism as an optical effect

birefringent, uniaxial crystal  
like Turmalin or filter foils



### Nuclear (spin) dichroism

initial beam: **unpolarized deuterons**  
target: **spin-zero nuclei** like **carbon**



$$I_{-1} + I_{+1} = I_{\pm 1} = 2/3$$

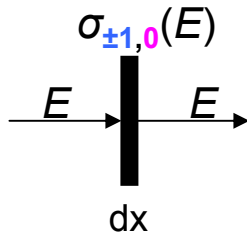
$$I_{\pm 1}(pdx) < 2I_0(pdx) \rightarrow p_{zz}(pdx) < 0$$

$$I_{\pm 1}(pdx) > 2I_0(pdx) \rightarrow p_{zz}(pdx) > 0$$

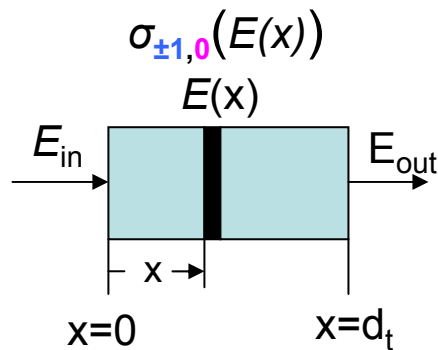
$$p_{zz}(pdx) \stackrel{\text{def}}{=} \frac{I_{+1}(pdx) + I_{-1}(pdx) - 2I_0(pdx)}{I_{+1}(pdx) + I_{-1}(pdx) + I_0(pdx)} = \frac{I_{\pm 1}(pdx) - 2I_0(pdx)}{I_{\pm 1}(pdx) + I_0(pdx)}$$

$$p_{zz}(pdx) = \frac{I_{\pm 1}(pdx) - 2I_0(pdx)}{I_{\pm 1}(pdx) + I_0(pdx)}$$

$$I_{\pm 1}(\rho dx), I_0(\rho dx) ?$$



$$p_{zz}(\rho dx) = \frac{2e^{-\rho\sigma_{\pm 1}(E)}dx - 2e^{-\rho\sigma_0(E)}dx}{2e^{-\rho\sigma_{\pm 1}(E)}dx + e^{-\rho\sigma_0(E)}dx}$$

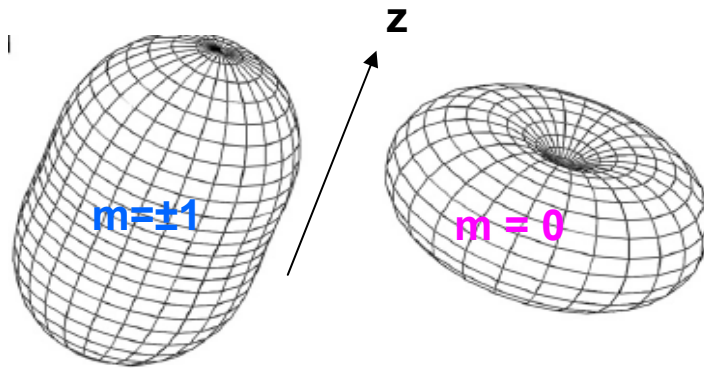


$$p_{zz}(\rho d_t) = \frac{2e^{-\rho \int_0^{d_t} \sigma_{\pm 1}(E(x)) dx} - 2e^{-\rho \int_0^{d_t} \sigma_0(E(x)) dx}}{2e^{-\rho \int_0^{d_t} \sigma_{\pm 1}(E(x)) dx} + e^{-\rho \int_0^{d_t} \sigma_0(E(x)) dx}}$$

$$\rho \int_0^{d_t} \sigma_{\pm 1}(E(x)) dx \ll 1, \quad \rho \int_0^{d_t} \sigma_0(E(x)) dx \ll 1 \quad (e^{-x} \rightarrow 1 - x)$$

$$p_{zz}(\rho d_t) = \frac{2}{3}\rho \int_0^{d_t} \left( \sigma_0(E(x)) - \sigma_{\pm 1}(E(x)) \right) dx$$

**Tasks:** calculate  $\sigma_0(E)$ ,  $\sigma_{\pm 1}(E)$  and measure  $p_{zz}$  as function of  $E_{in}$  and  $d_t$  (i.e.,  $E_{out}$ )



unpolarized deuteron beam  
beam direction  $\equiv$  quantization axis  $z$

**expectation:**  $\sigma_0 > \sigma_{\pm 1}$  resulting in  $p_{zz} > 0$

## Relativistic energies:

### Calculation

G. Fäldt, J. Phys. G: Nucl. Phys 6 (1980) 1513:  $\sigma_0 - \sigma_{\pm 1} = + 1.87 \text{ fm}^2$

### Experiment

L.S. Azhgirey et al., Particles and Nuclei, Letters 5 (2008) 728):  $\sigma_0 - \sigma_{\pm 1} = + 7.18 \text{ fm}^2$

## E = 5 to 20 MeV:

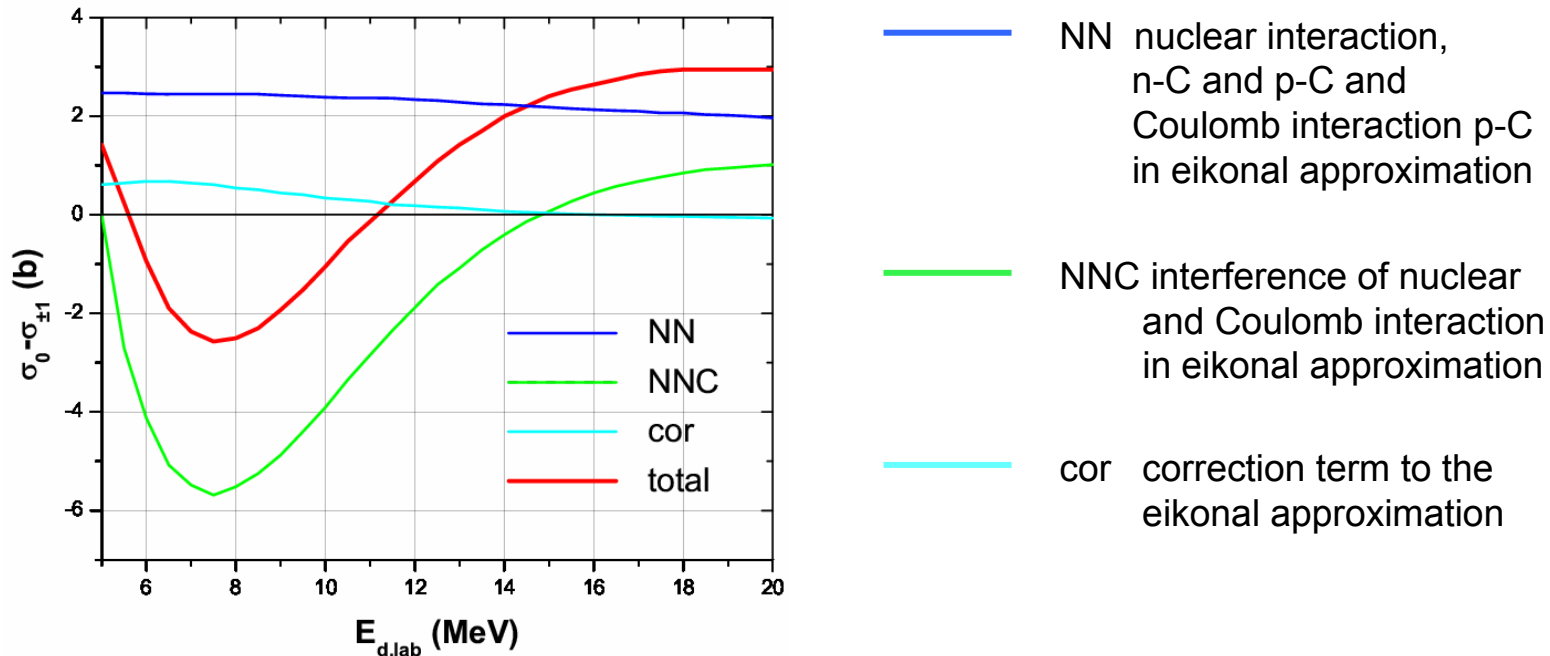
### Calculation

V. Baryshevsky and A. Rouba, Phys. Lett. B **683** (2010) 229

**Optical theorem**  $\sigma_0(E) - \sigma_{\pm 1}(E) = \frac{4\pi}{k} \text{Im}\{f_0(\theta = 0, E) - f_{\pm 1}(\theta = 0, E)\}$



V. Baryshevsky and A. Rouba, Phys. Lett. B **683** (2010) 229



Essential results: (a)  $\sigma_0 - \sigma_{\pm 1}$  up to  $b$  compared to  $fm^2=10^{-2} b$  at high energies  
 (b) **change of sign** due to **nuclear-Coulomb interference**

$$\rho_{\text{graphite}} = 1 \text{ g/cm}^3 \text{ or } 5 \cdot 10^{22} \text{ C atoms/cm}^3$$

$$E_{\text{in}} = 20 \text{ MeV}, E_{\text{out}} = 11 \text{ MeV}: \quad p_{zz}(\rho d_t) = \frac{2}{3} \rho \int_0^{0.18 \text{ cm}} \left( \sigma_0(E(x)) - \sigma_{\pm 1}(E(x)) \right) dx = +0.014$$

$$E_{\text{in}} = 11 \text{ MeV}, E_{\text{out}} = 5.5 \text{ MeV}: \quad p_{zz}(\rho d_t) = \frac{2}{3} \rho \int_0^{0.07 \text{ cm}} \left( \sigma_0(E(x)) - \sigma_{\pm 1}(E(x)) \right) dx = -0.0035$$

# Measurements

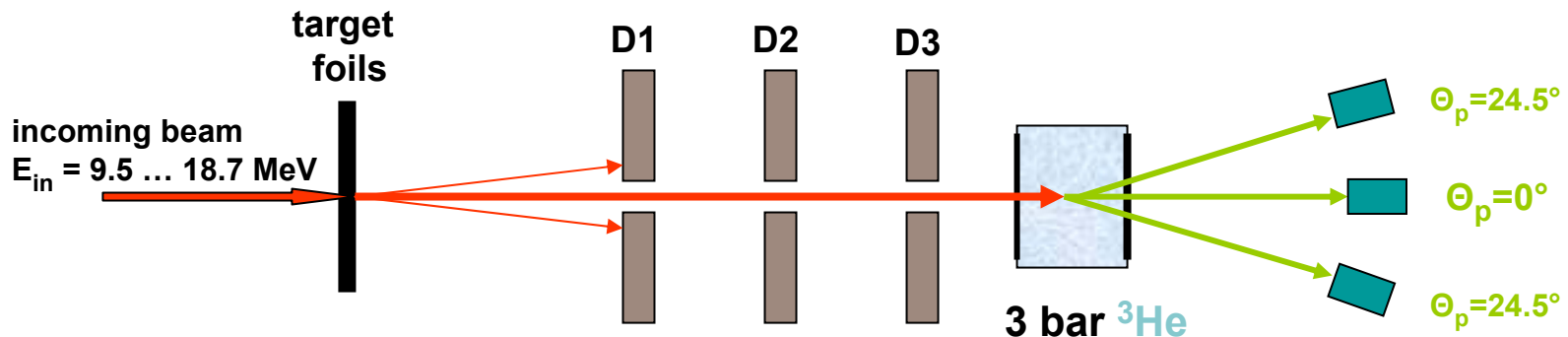
Performed with

**unpolarized deuteron beam from Van-de-Graaff tandem accelerator**

operated by

**Institut für Kernphysik of Universität zu Köln**

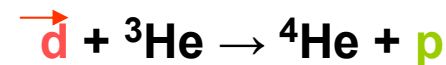
(J. Jolie, H. Paetz gen Schieck, J. Eberth, and A. Dewald, Nucl. Phys. News **12**, 4 (2002))



thickness labelled  
 $\text{mg}/\text{cm}^2$  as

empty

Au	5.0	<b>Au5</b>
Au	9.7	<b>Au10</b>
C	35.90	<b>C36</b>
C	57.69	<b>C58</b>
C	93.59	<b>C94</b>
C	129.49	<b>C129</b>
C	152.63	<b>C153</b>
C	165.39	<b>C165</b>
C	187.93	<b>C188</b>

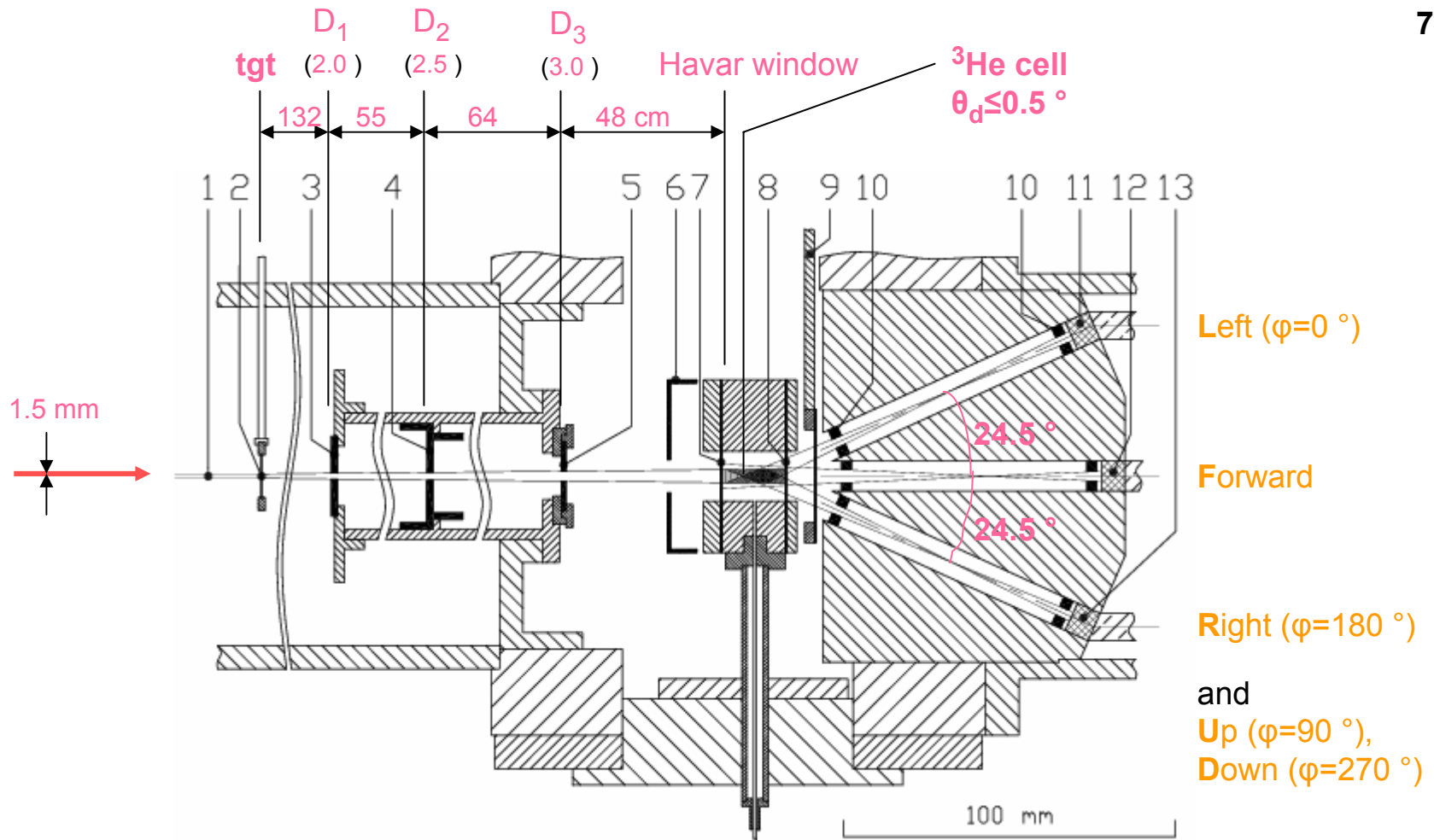


$$E_{\text{cell}} = f(E_{\text{in}}, d_{\text{target}})$$

$$\sigma(E_{\text{cell}}, \theta_p) = \underbrace{\sigma_o(E_{\text{cell}}, \theta_p)}_{\text{known}} \cdot \underbrace{[1 + 1/2 \cdot p_{zz}(E_{\text{cell}})]}_{\text{to derive}} \cdot \underbrace{A_{zz}(E_{\text{cell}}, \theta_p)}_{\text{known}}$$

measured

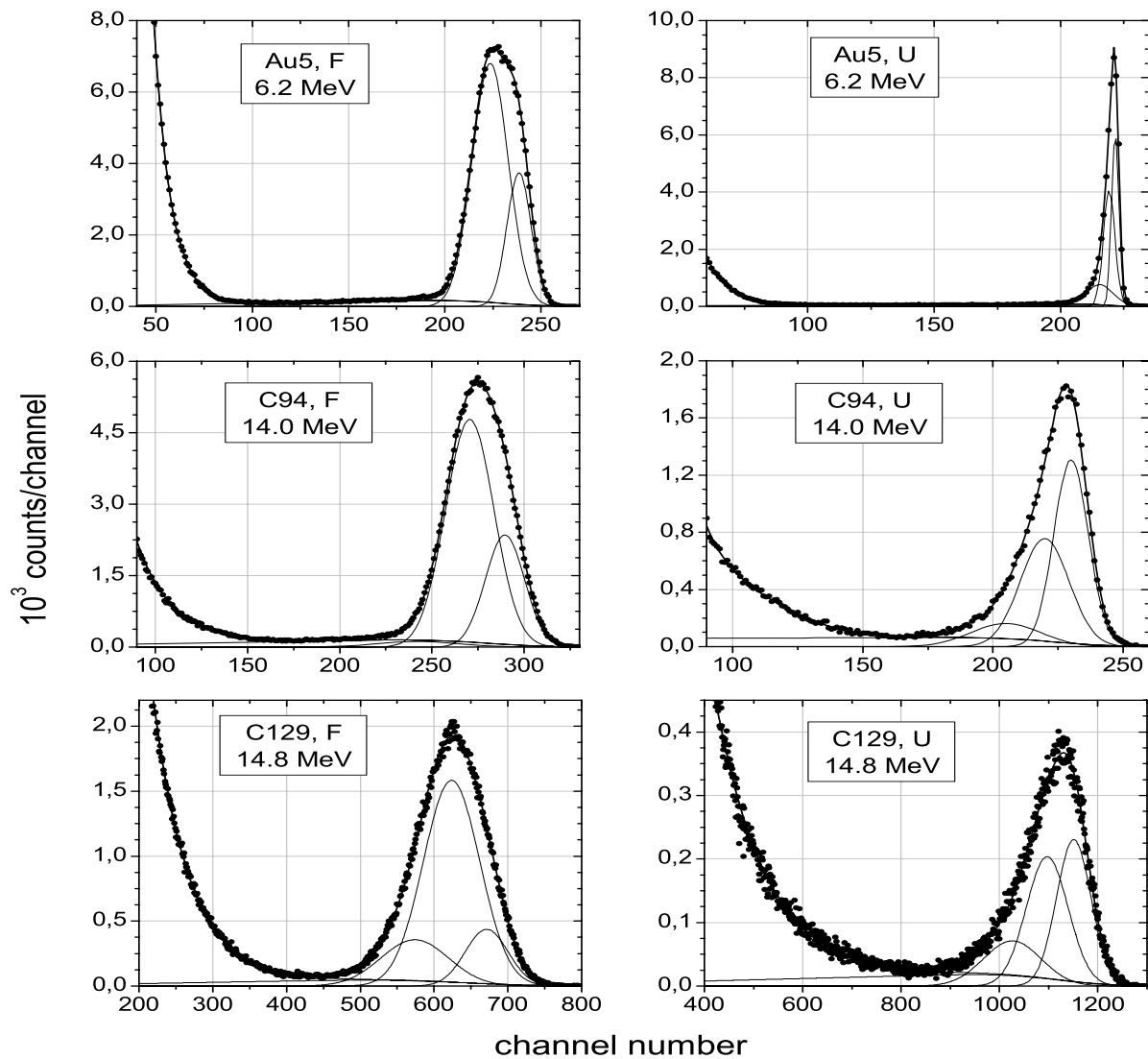
to derive



$$r(E_{\text{cell}}) = \frac{N_L(E_{\text{cell}}) + N_U(E_{\text{cell}}) + N_R(E_{\text{cell}}) + N_D(E_{\text{cell}})}{N_F(E_{\text{cell}})}$$

$$N_i(E_{\text{cell}}) = \rho_{\text{He}} \cdot l_i \cdot \Omega_i \cdot \varepsilon_i \cdot \int j_{\text{cell}}(t) dt \cdot \overline{\sigma(E_{\text{cell}}, (24.5 \pm 2.9)^\circ)}$$

$$N_F(E_{\text{cell}}) = \rho_{\text{He}} \cdot l_F \cdot \Omega_F \cdot \varepsilon_F \cdot \int j_{\text{cell}}(t) dt \cdot \overline{\sigma(E_{\text{cell}}, (0 \pm 2.6)^\circ)}$$

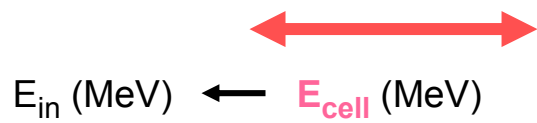
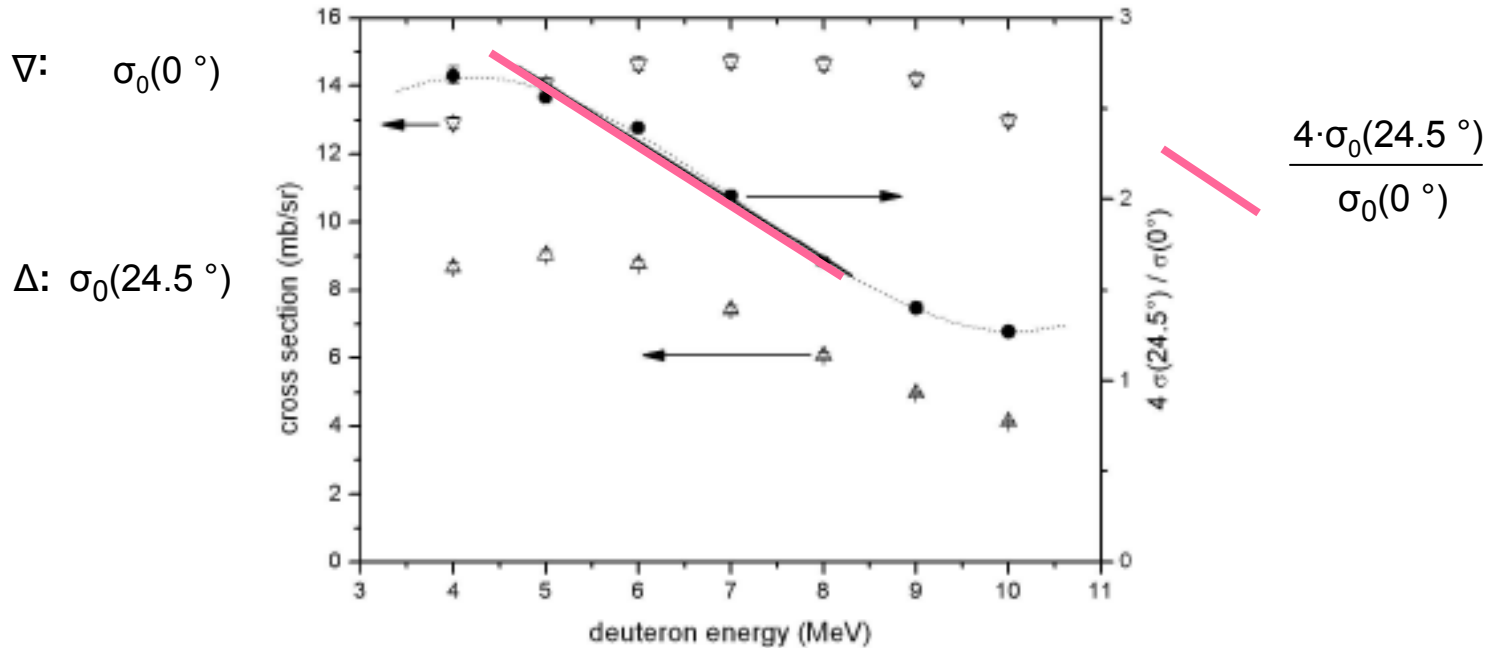




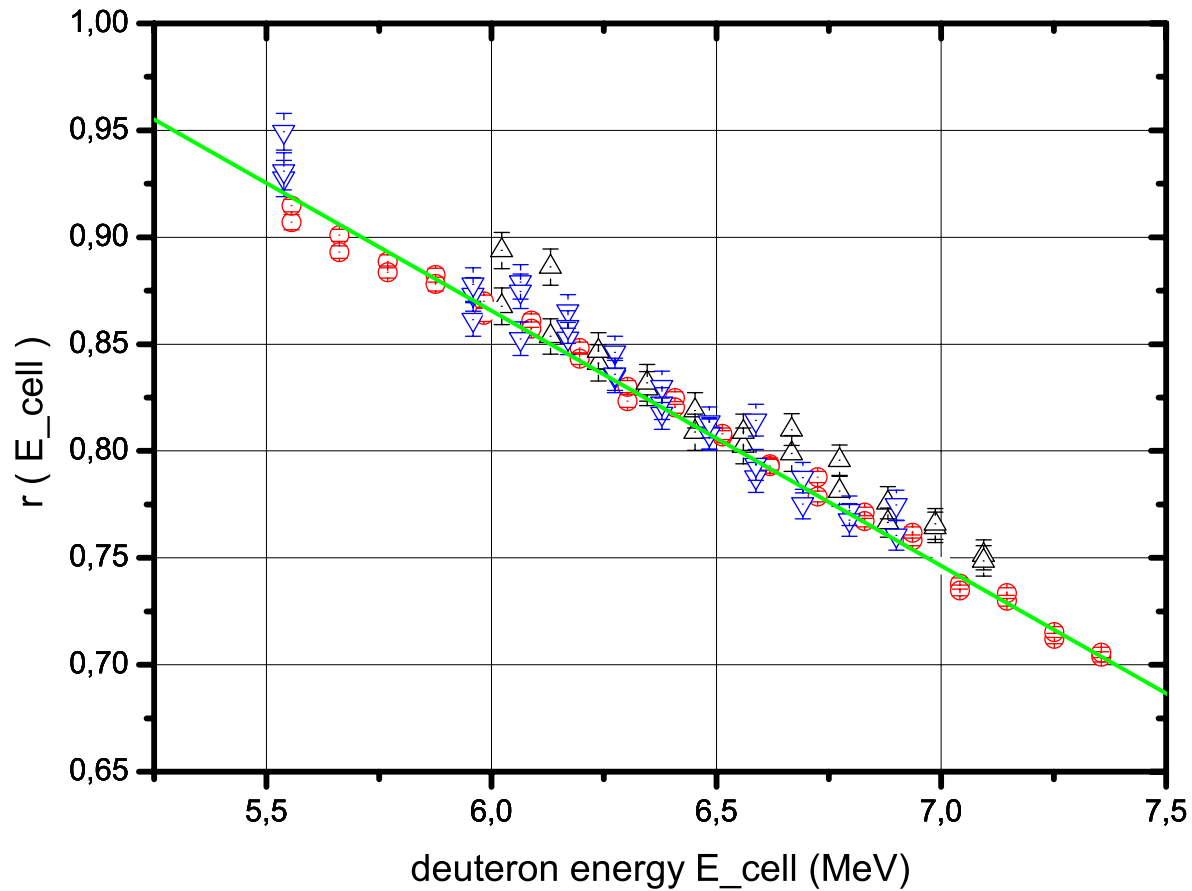
## What is expected with an unpolarized beam?

$$\sigma(E_{\text{cell}}, \theta_p) = \sigma_o(E_{\text{cell}}, \theta_p) \cdot [1 + 1/2 \cdot p_{zz}(E_{\text{cell}}) \cdot A_{zz}(E_{\text{cell}}, \theta_p)]$$

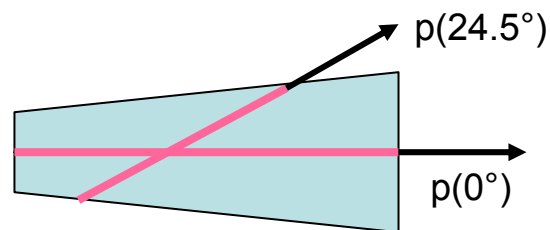
Unpolarized cross sections from M. Bittcher et al., Few-Body Systems **9** (1990) 165



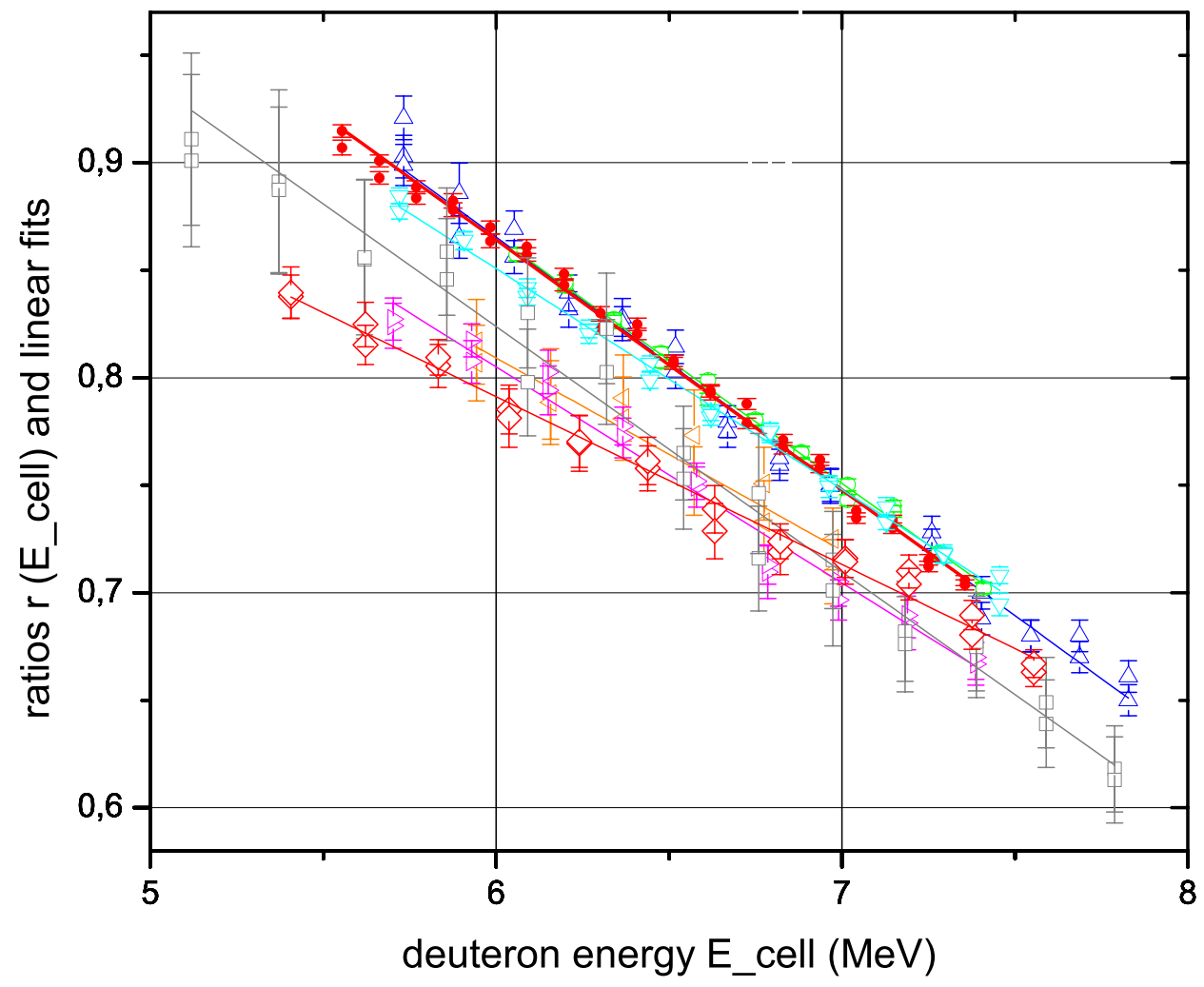
Au5	6.20 .... 7.90	<b>5.56 .... 7.36</b>
C36	9.50 .... 10.50	<b>6.06 .... 7.41</b>
C188	17.50 .... 18.70	<b>5.11 .... 7.78</b>



—  $4\sigma_0(24.5^\circ)/\sigma_0(0^\circ)\}_{\text{calc}} \cdot f_{\text{norm}}(r_{\text{Au5}}^{\text{fit}}(6.5\text{MeV}))$

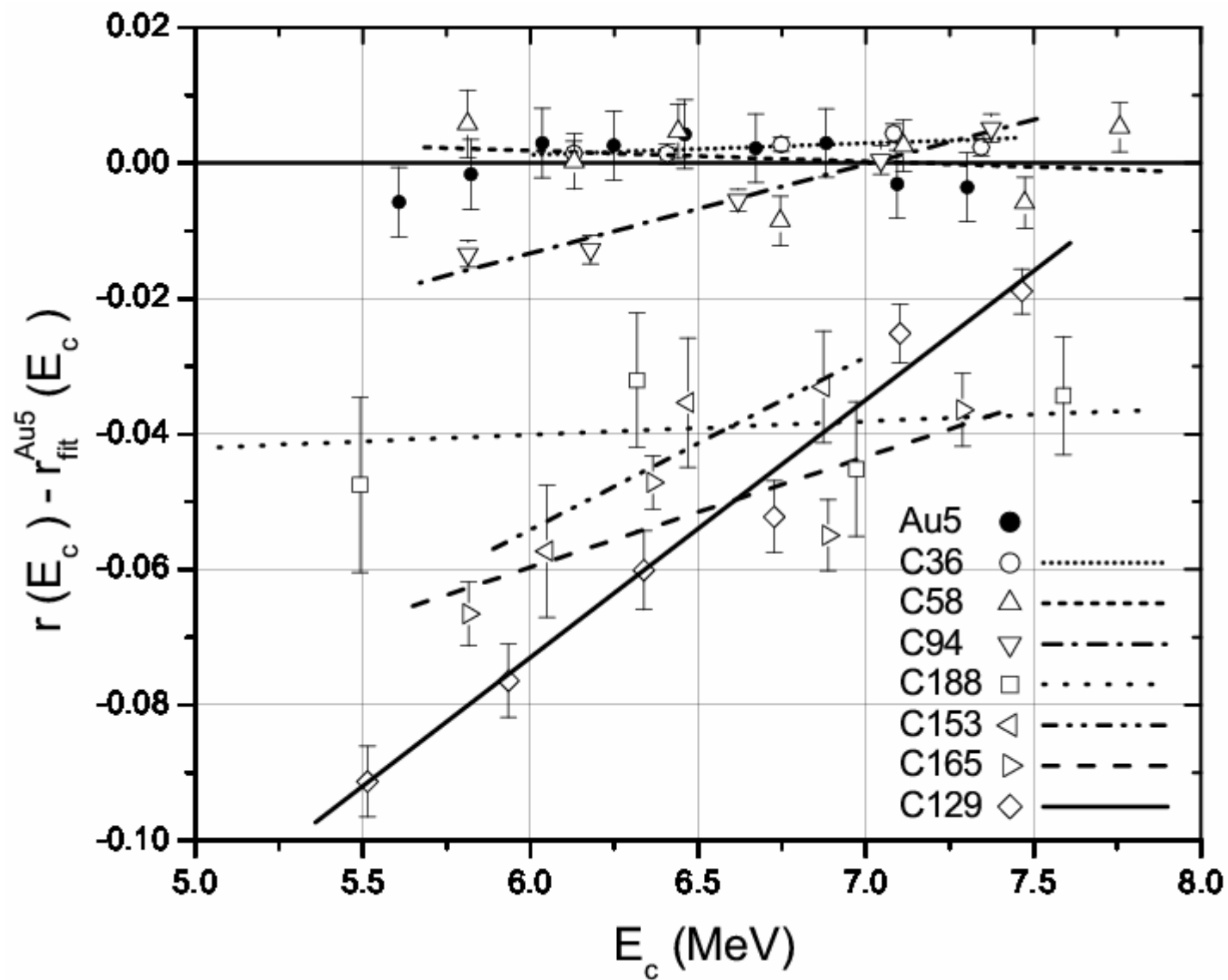


$f_{\text{norm}} = 0.374$



Measured proton-peak ratios with linear fits

- Au5
- C36
- △ C58
- ▽ C94
- ◇ C129
- ◁ C153
- ▷ C165
- C188

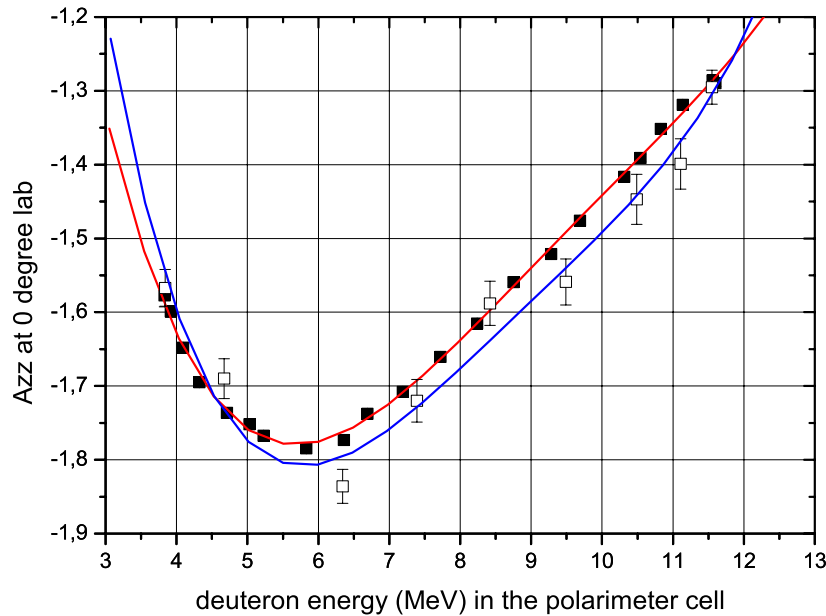


$$\frac{r_{\text{Cx}}^{\text{fit}}(E_{\text{cell}})}{r_{\text{Au5}}^{\text{fit}}(E_{\text{cell}})} = \frac{\left[ \frac{(C_{\text{L}}+C_{\text{R}}+C_{\text{U}}+C_{\text{D}}) \cdot \sigma_0(E_{\text{cell}}, 24.5^\circ) \cdot [1 + \frac{1}{2} p_{\text{zz}}(E_{\text{cell}}) A_{\text{zz}}(E_{\text{cell}}, 24.5^\circ)]}{C_{\text{F}} \cdot \sigma_0(E_{\text{cell}}, 0^\circ) \cdot [1 + \frac{1}{2} p_{\text{zz}}(E_{\text{cell}}) A_{\text{zz}}(E_{\text{cell}}, 0^\circ)]} \right]_{\text{Cx}}}{\left[ \frac{(C_{\text{L}}+C_{\text{R}}+C_{\text{U}}+C_{\text{D}}) \cdot \sigma_0(E_{\text{cell}}, 24.5^\circ)}{C_{\text{F}} \cdot \sigma_0(E_{\text{cell}}, 0^\circ)} \right]_{\text{Au5}}}$$

$$C_i = \rho_{\text{He}} \cdot l_i \cdot \Omega_i \cdot \varepsilon_i \cdot \int j_{\text{cell}}(t) dt$$

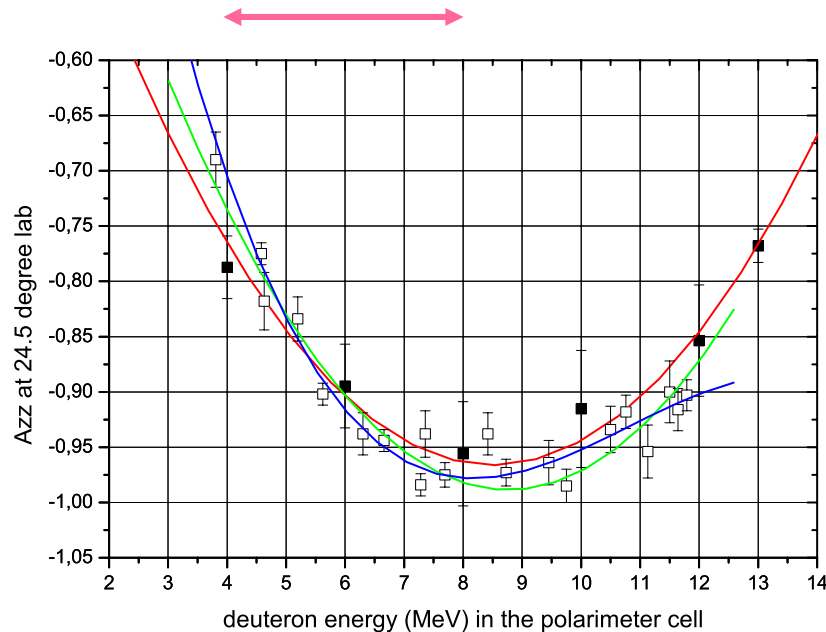
$$= \frac{1 + \frac{1}{2} p_{\text{zz}}(E_{\text{cell}}) \cdot A_{\text{zz}}(E_{\text{cell}}, 24.5^\circ)}{1 + \frac{1}{2} p_{\text{zz}}(E_{\text{cell}}) \cdot A_{\text{zz}}(E_{\text{cell}}, 0^\circ)}$$

$$p_{\text{zz}}(E_{\text{cell}}) = \frac{2 \cdot [ r_{\text{Au5}}^{\text{fit}}(E_{\text{cell}}) - r_{\text{Cx}}^{\text{fit}}(E_{\text{cell}}) ]}{r_{\text{Cx}}^{\text{fit}}(E_{\text{cell}}) \cdot A_{\text{zz}}(E_{\text{cell}}, 0^\circ) - r_{\text{Au5}}^{\text{fit}}(E_{\text{cell}}) \cdot A_{\text{zz}}(E_{\text{cell}}, 24.5^\circ)}$$



$$A_{zz}(E_{\text{cell}}, 0^\circ)$$

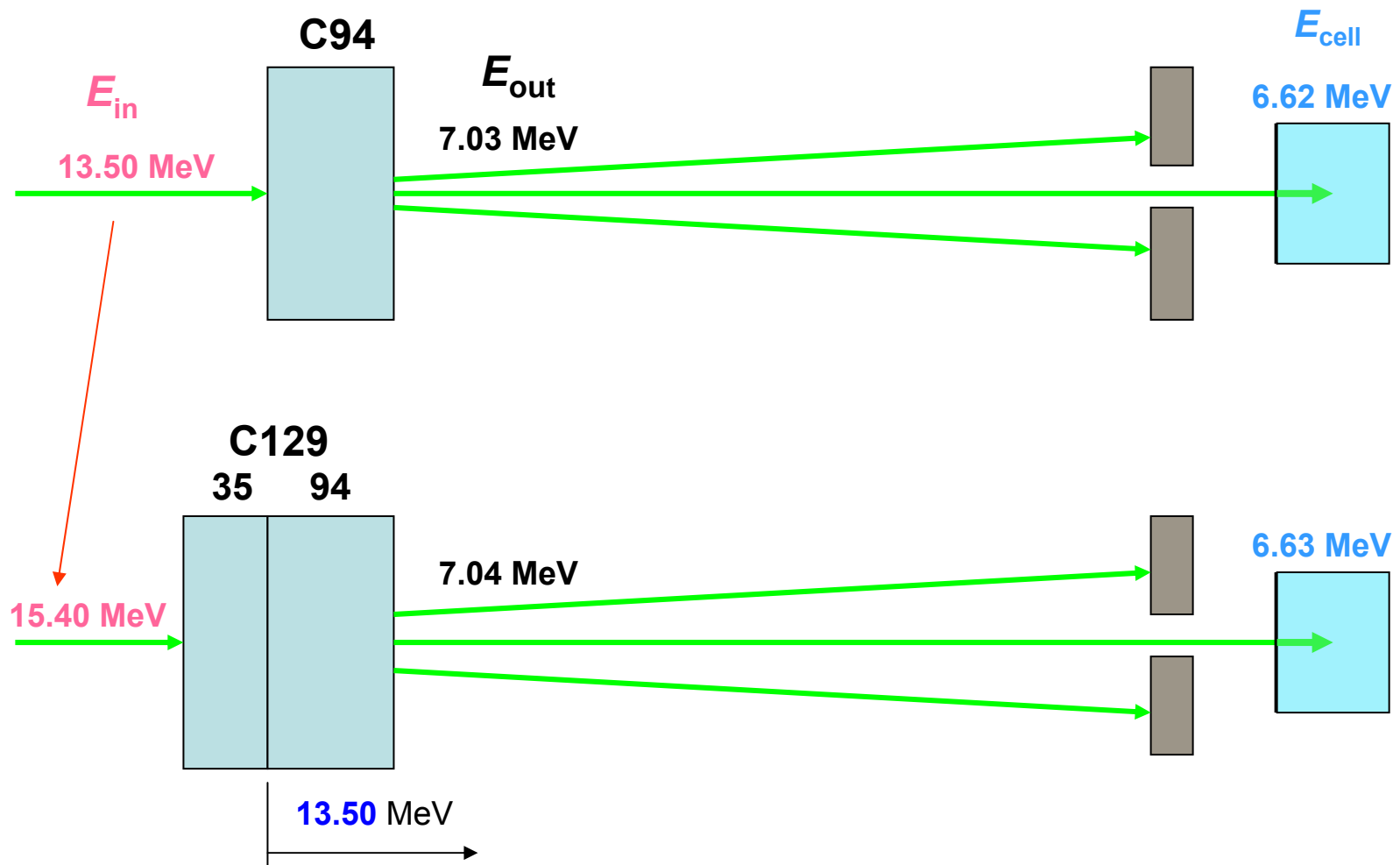
- P.A. Schmelzbach, W. Grüebler, V. König, R. Risler, D.O. Boerma, and B. Jenny, Nucl. Phys. **A264**, 45 (1976) .
- S.A. Tonsfeldt, PhD Thesis, University of North Carolina, 1983.



$$A_{zz}(E_{\text{cell}}, 24.5^\circ)$$

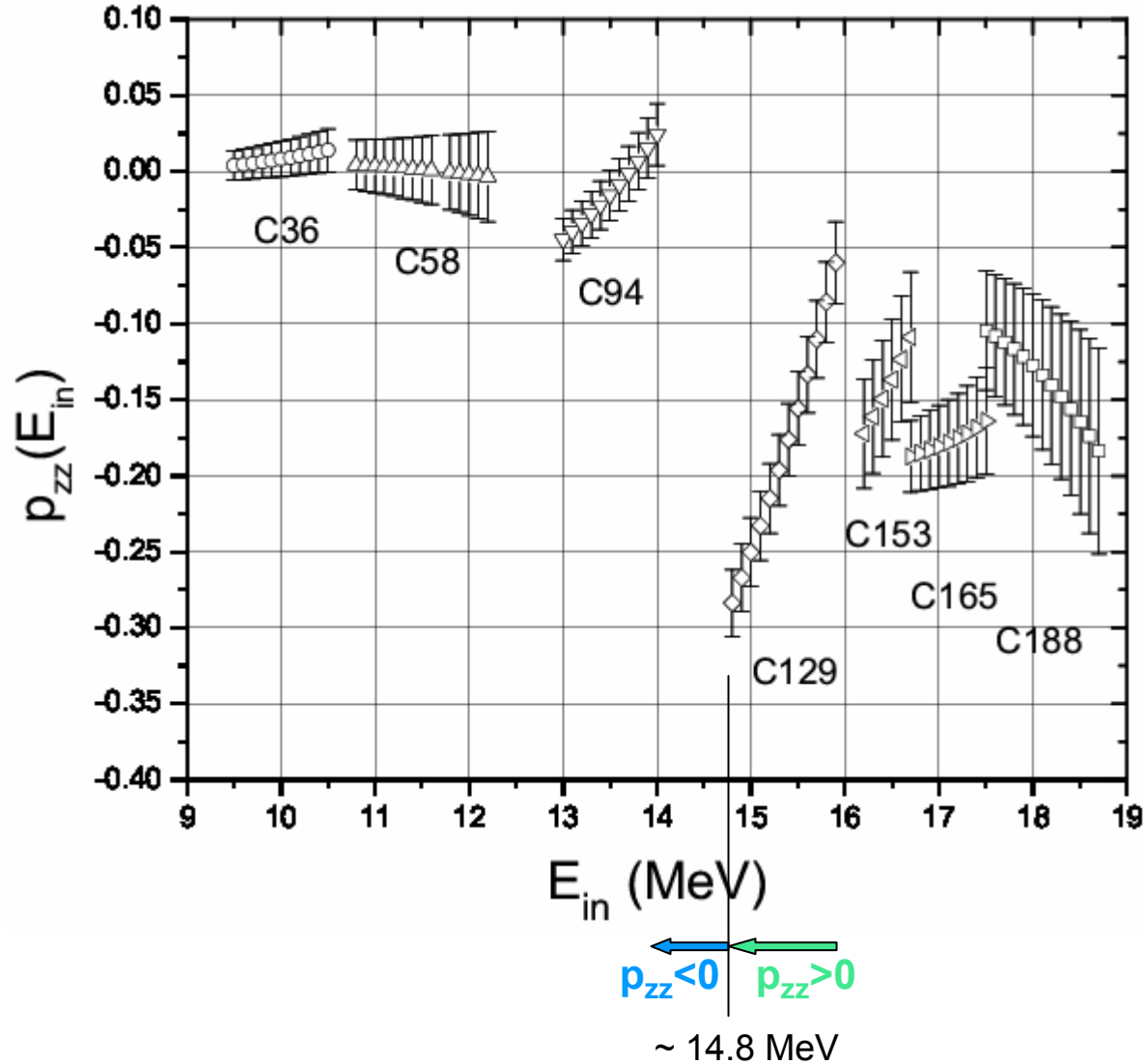
- M. Bittcher, W. Grüebler, V. König, P.A. Schmelzbach, B. Vuaridel, and J. Ulbricht, Few-Body Systems 9, 165 (1990)
- S.A. Tonsfeldt, PhD Thesis, University of North Carolina, 1983.

$p_{zz}$  measured at  $E_{\text{cell}}$  in the polarimeter cell



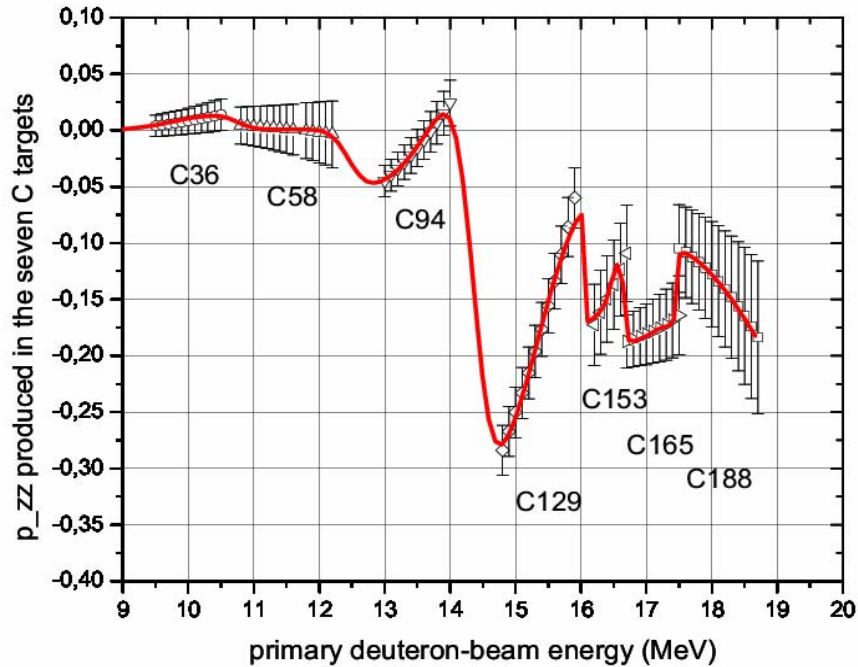
$$p_{zz}(E_{\text{cell}}) \rightarrow p_{zz}(E_{\text{in}})$$

## The (unexpected) experimental result



Theoretical values in the order of  $10^{-2}$ , change of sign at 11 Mev, energy dependence much slower





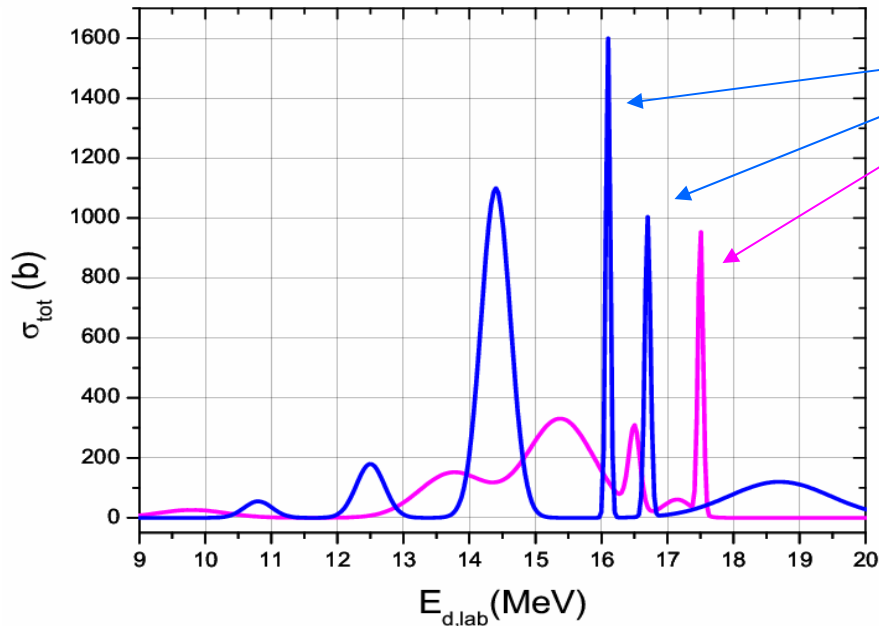
$$p_{zz}(\rho d_t) = \frac{2e^{-\rho \int_0^{d_t} \sigma_{\pm 1}(E(x)) dx} - 2e^{-\rho \int_0^{d_t} \sigma_0(E(x)) dx}}{2e^{-\rho \int_0^{d_t} \sigma_{\pm 1}(E(x)) dx} + e^{-\rho \int_0^{d_t} \sigma_0(E(x)) dx}}$$

Fit by **12 Gaussian-distributed cross sections**

Adjustment of  $E_0$ ,  $\sigma(E_0)$ ,  $\Gamma$

For **6** of them  $\sigma_{\pm 1} = 0 \rightarrow p_{zz} > 0$

For **6** of them  $\sigma_0 = 0 \rightarrow p_{zz} < 0$



**16.1**, **16.7**, and **17.5** MeV  
possibly caused by uncertainties  
in the target thicknesses

—  $\sigma_{\pm 1} \neq 0, \sigma_0 = 0 \rightarrow p_{zz} < 0$

—  $\sigma_{\pm 1} = 0, \sigma_0 \neq 0 \rightarrow p_{zz} > 0$

$$E^*(^{14}\text{N}) = E_d^{cms} + m_d + m_{^{12}\text{C}} - m_{^{14}\text{N}} = \frac{m_{^{12}\text{C}}}{m_d + m_{^{12}\text{C}}} E_d^{lab} + m_d + m_{^{12}\text{C}} - m_{^{14}\text{N}}$$

$$= 0.85628 \cdot E_d^{lab} + 10.2720 [\text{MeV}].$$

resonance data from the present fit						$^{12}\text{C}(d, \alpha_2)^{10}\text{B}^*(1.74\text{MeV})$					
no.	$E_0^{lab}$ [MeV]	$\sigma(E_0)$ [b]	$\Gamma$ [keV]	p <sub>zz</sub> produced by isolated resonance	$E^*(^{14}\text{N})$ [MeV]	$(d\sigma/d\omega)_{c.m.}$ backward			$(d\sigma/d\omega)_{c.m.}$ forward		
						$E^*(^{14}\text{N})$ [MeV]	$\mu\text{b/sr}$	ref.	$E^*(^{14}\text{N})$ [MeV]	$\mu\text{b/sr}$	ref.
1	18.7±0.3	120±40	1800±300	-0.14±0.03	26.3±0.3						
2	17.5±0.2	950±100	90±30	+0.06±0.01	25.3±0.2						
3	17.15±0.4	60±20	500±100	+0.05 <sup>+0.01</sup> <sub>-0.03</sub>	25.1±0.3						
4	16.7±0.2	1000±200	100±30	-0.083 <sup>+0.006</sup> <sub>-0.033</sub>	24.6±0.2	~24.6	4±1	a			
5	16.5±0.3	280±50	200±50	+0.062±0.013	24.4±0.3	~24.3	6±2	a			
6	16.1±0.2	1600±400	80±30	-0.12±0.02	24.0±0.2	~24.1	5±1	a			
7	15.38±0.03	330±40	1200±400	+0.228±0.016	23.44±0.03	~23.5	6±2	a	23.36	~60	b
8	14.4±0.1	1100±100	520±100	-0.375±0.014	22.6±0.1	~22.6	19 <sup>+4</sup> <sub>-12</sub>	a	22.6±0.1	~90	b, c
9	13.75±0.05	150±20	1200±200	+0.10±0.02	22.05±0.04				21.8	~40	d
10	12.5±0.1	180±20	500±100	-0.05 <sup>+0.01</sup> <sub>-0.03</sub>	21.0±0.1				21.2	~110	d
									20.7	~90	d
11	10.8±0.1	50±30	500±200	-0.011 <sup>+0.004</sup> <sub>-0.021</sub>	19.5±0.1				~19.0	~50	e
12	9.8±0.1	25±25	1200±500	+0.014 <sup>+0.018</sup> <sub>-0.006</sub>	18.7±0.1						

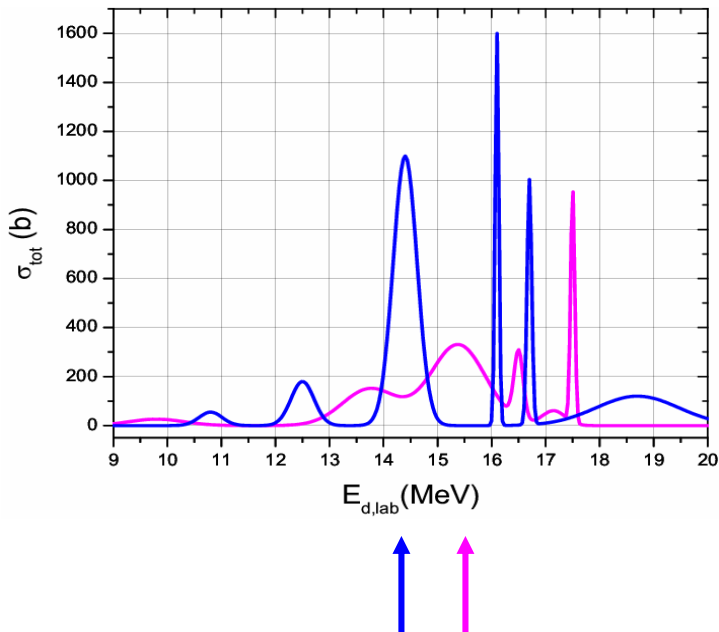
$\sigma(E_0) \cdot \Gamma$  (b·MeV)

400

570

- a) D. von Ehrenstein et al., Phys. Rev. Lett. **27**, 107 (1971); b) P.L. Jolivette, Phys. Rev. **C 9**, 16 (1974);  
c) J. Jänecke et al., Phys. Rev. **175**, 1301(1968); d) H. Vernon Smith, Jr., and H.T. Richards,  
Phys. Rev. Lett. **23**, 1409 (1969); e) L. Meyer-Schützmeister et al., Phys. Rev. **147**, 743 (1966).

## An attempt to interpret the two strong resonances at 14.4 and 15.4 MeV



### present work

$E_0$ (MeV)	$14.4 \pm 0.1$	$15.38 \pm 0.03$
$\sigma(E_0)$ (b)	<b><math>1100 \pm 100</math></b>	<b><math>330 \pm 40</math></b>
$\Gamma$ (keV)	$520 \pm 100$	$1000 \pm 250$
$p_{zz}$	$-0.375 \pm 0.014$	$+0.228 \pm 0.016$
$E^*(^{14}\text{N})$ (MeV)	<b><math>22.6 \pm 0.1</math></b>	<b><math>23.44 \pm 0.03</math></b>

### earlier (d, $\alpha$ ) experiments

D. von Ehrenstein et al., Phys. Rev. Lett. **27**, 107 (1971):

$E^*(^{14}\text{N})$  (MeV)       **$\sim 22.6$**                        **$\sim 23.5$**

$d\sigma/d\Omega$  ( $\mu\text{b}/\text{sr}$ )       $\sim 19$                                        $\sim 6$

P.L. Jolivet, Phys. Rev. **C 9**, 16 (1974):

$E^*(^{14}\text{N})$  (MeV)       **$22.6 \pm 0.1$**                        **$23.36$**

$d\sigma/d\Omega$  ( $\mu\text{b}/\text{sr}$ )      90    60

The giant resonance in  $^{14}\text{N}$  spreads around **22.5 MeV** with a width (FWHM) of 3.5 MeV

M. Goldhaber and E. Teller, Phys. Rev. **74**, 1046 (1948): **dipole vibration of the bulk of protons against that of neutrons**

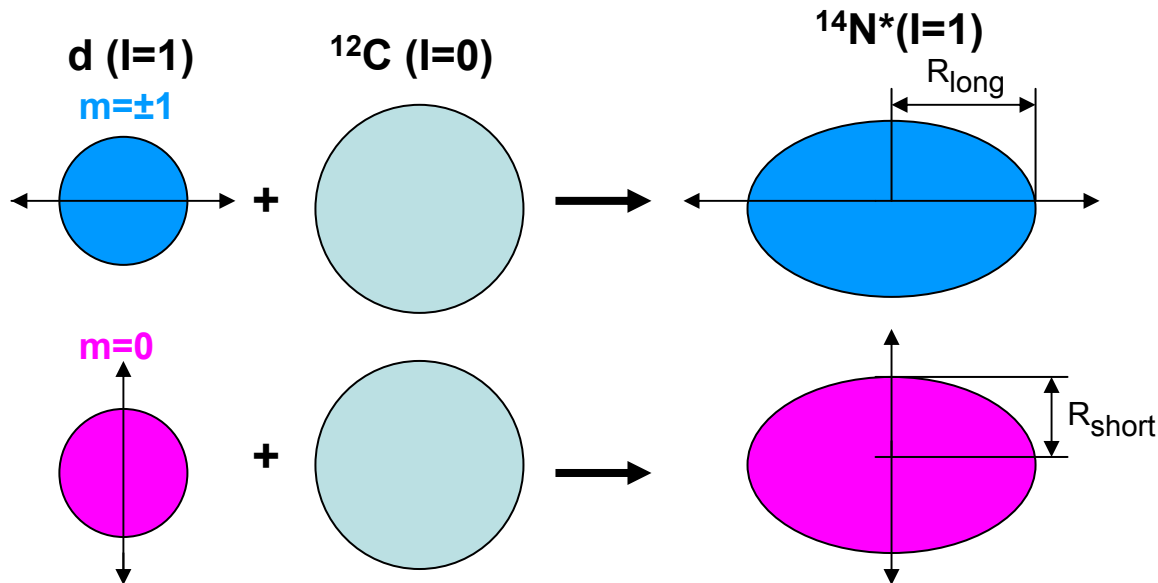
$$\hbar\omega = \left( \frac{3\varphi\hbar^2}{\varepsilon R_0 m} \right)^{\frac{1}{2}}$$

$\varphi=30$  MeV,  $\varepsilon=2.4$  fm, and  $R_0=R_e=3.13$  fm  $\rightarrow \hbar\omega=$  **22.3 MeV**

## Extension of the vibrational model to 2 orthogonal vibrations in a deformed nucleus

Tentative use of the quadrupole moment of the  $^{14}\text{N}$  ground state of  $+0.0193$  b yields

$$R_{\text{long}} = R_0 + 0.07 \text{ fm} = 3.20 \text{ fm} \text{ and } R_{\text{short}} = R_0 - 0.07 \text{ fm} = 3.06 \text{ fm}$$



These modified values of  $R_0$  yield

$$\hbar\omega(R_{\text{long}}) = 22.1 \text{ MeV}$$

Creation of the compound state leads to the removal of deuterons in the  $m=\pm 1$  state from the beam

and

$$\hbar\omega(R_{\text{short}}) = 22.6 \text{ MeV}$$

Creation of the compound state leads to the removal of deuterons in the  $m=0$  state from the beam

vibrational model			present experiment	
excitation energy (MeV)	spin-projection quantum number $m$	$p_{zz}$	resonance energy $E^*(^{14}\text{N})$ (MeV)	$p_{zz}$ produced by the resonance
22.1	$\pm 1$	$< 0$	$22.6 \pm 0.1$	$-(0.375 \pm 0.014)$
22.6	0	$> 0$	$23.44 \pm 0.03$	$+(0.228 \pm 0.016)$

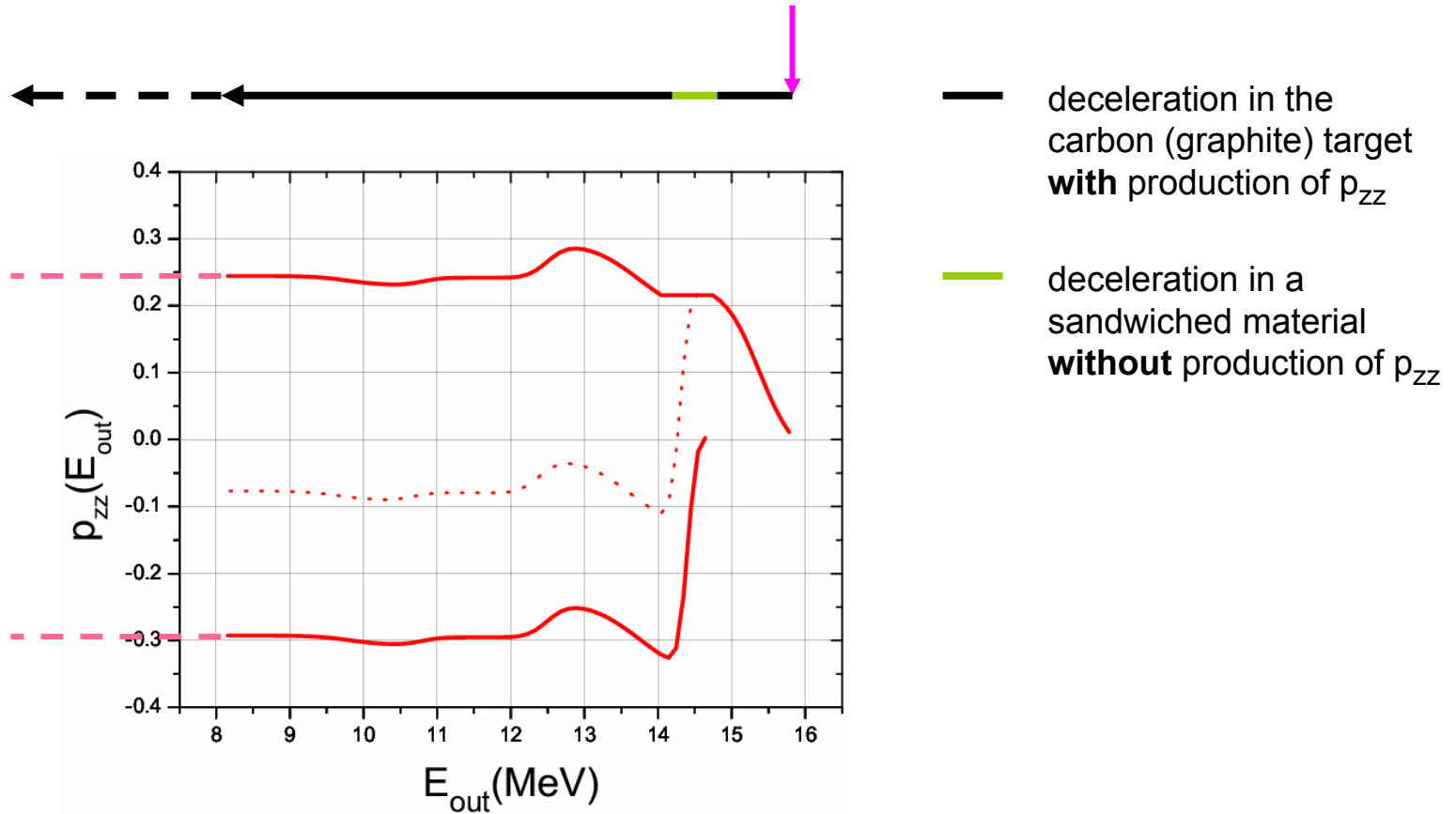
The simple picture would allow a first interpretation. Is it, however, valid?

At present **no real understanding** of the surprising results,  
mainly due to the requested **large cross section** values

**Extra-nuclear effects?**  
**(polarization of the deuterons in the Coulomb field,**  
i.e., change of the deuteron wave function,  
**spin-orbit coupling?)**

**The results, however, would allow the  
(inexpensive) production of tensor-polarized deuteron beams**

$E_{in}$  at the upper edge of the 15.38 MeV resonance

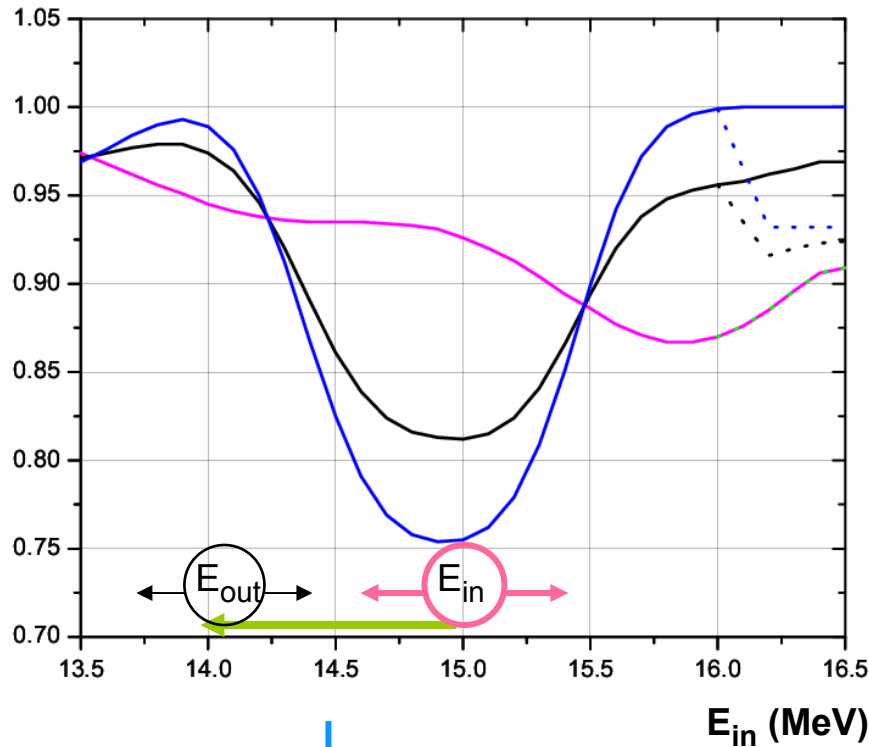


$E_{in}$  at the upper edge of the 14.4 MeV resonance

## Confirmatory measurement under consideration:

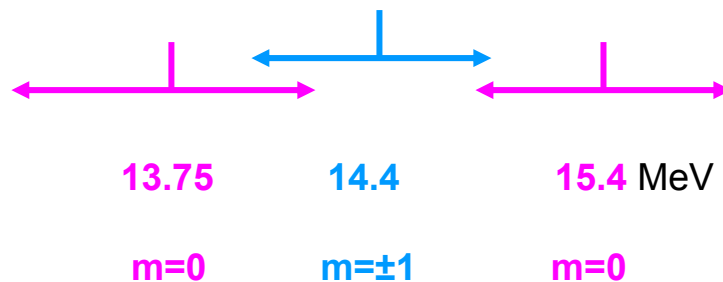
Transmission of 13.5 to 16.5 MeV deuteron beams through a **20 mg/cm<sup>2</sup> carbon foil**

Energy loss in the foil  $\Delta E_d \sim 1$  MeV



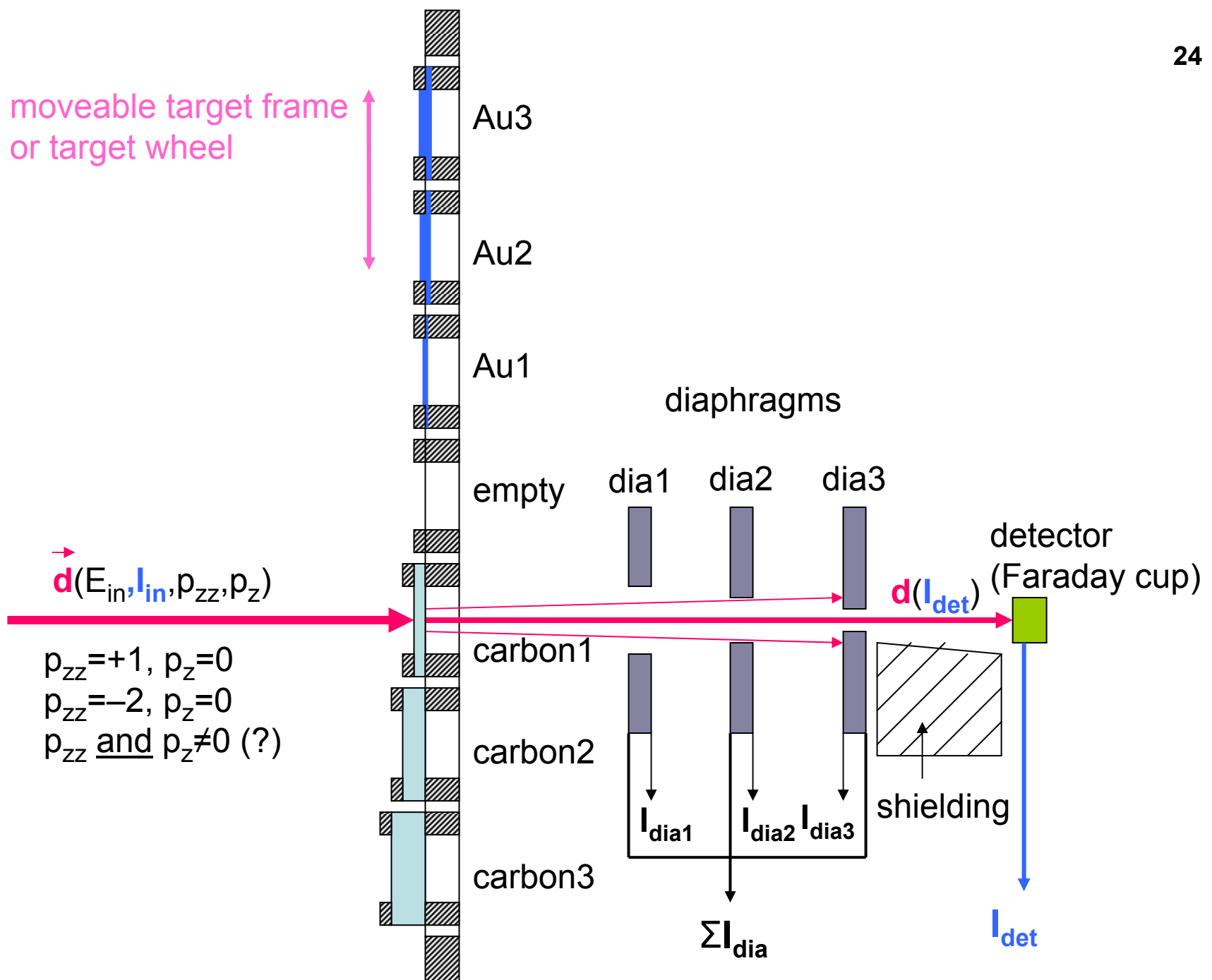
- $p_{zz} = +1, p_z = 0$   
(100%  $m = \pm 1$ )
- unpolarized beam  
(2/3  $m = \pm 1, 1/3 m = 0$ )
- $p_{zz} = -2, p_z = 0$   
(100%  $m = 0$ )

dashed lines: with the possibly artificial resonance at 16.1 MeV

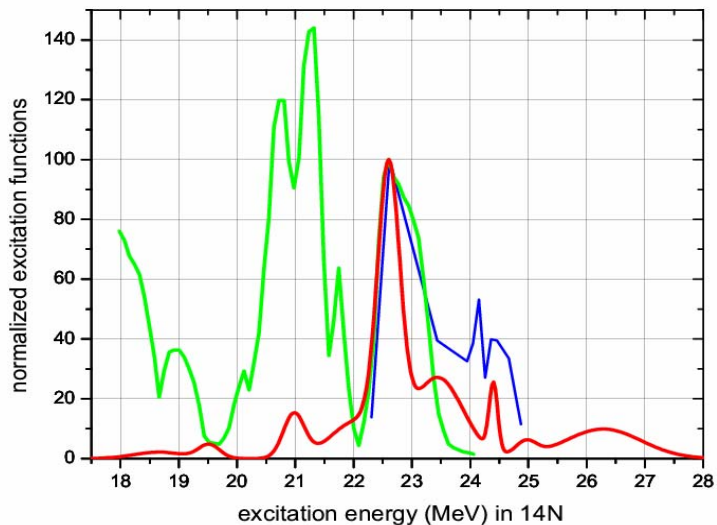


resonance  
removes  
deuterons from the beam

! Calculated with  
either  $\sigma_0$  or  $\sigma_{\pm 1}$   
equal to zero







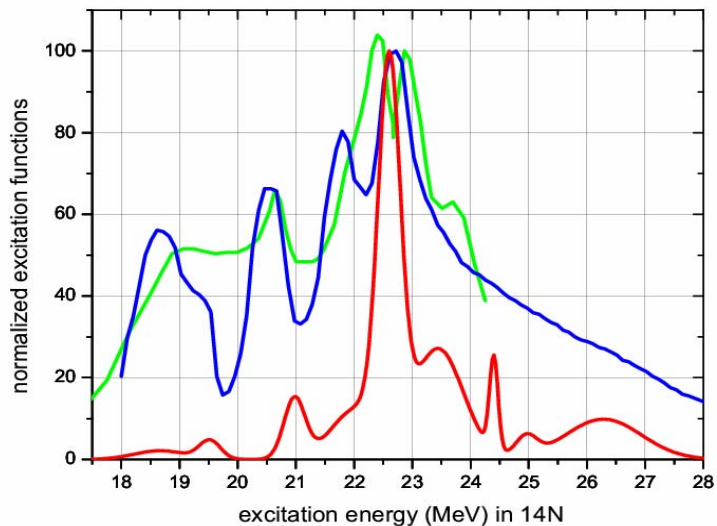
**α emission forward**

L. Meyer-Schützmeister et al., Phys. Rev. **147**, 743 (1966);  
H. Vernon Smith, Jr., and H.T. Richards, Phys. Rev. Lett.  
**23**, 1409 (1969); P.L. Jolivette, Phys. Rev. **C 9**, 16 (1974)

**α emission backward**

D. von Ehrenstein et al., Phys. Rev. Lett. **27**, 107 (1971)

peaks of the present fit without the possibly artificial resonances at 16.1, 16.7, and 17.5 MeV



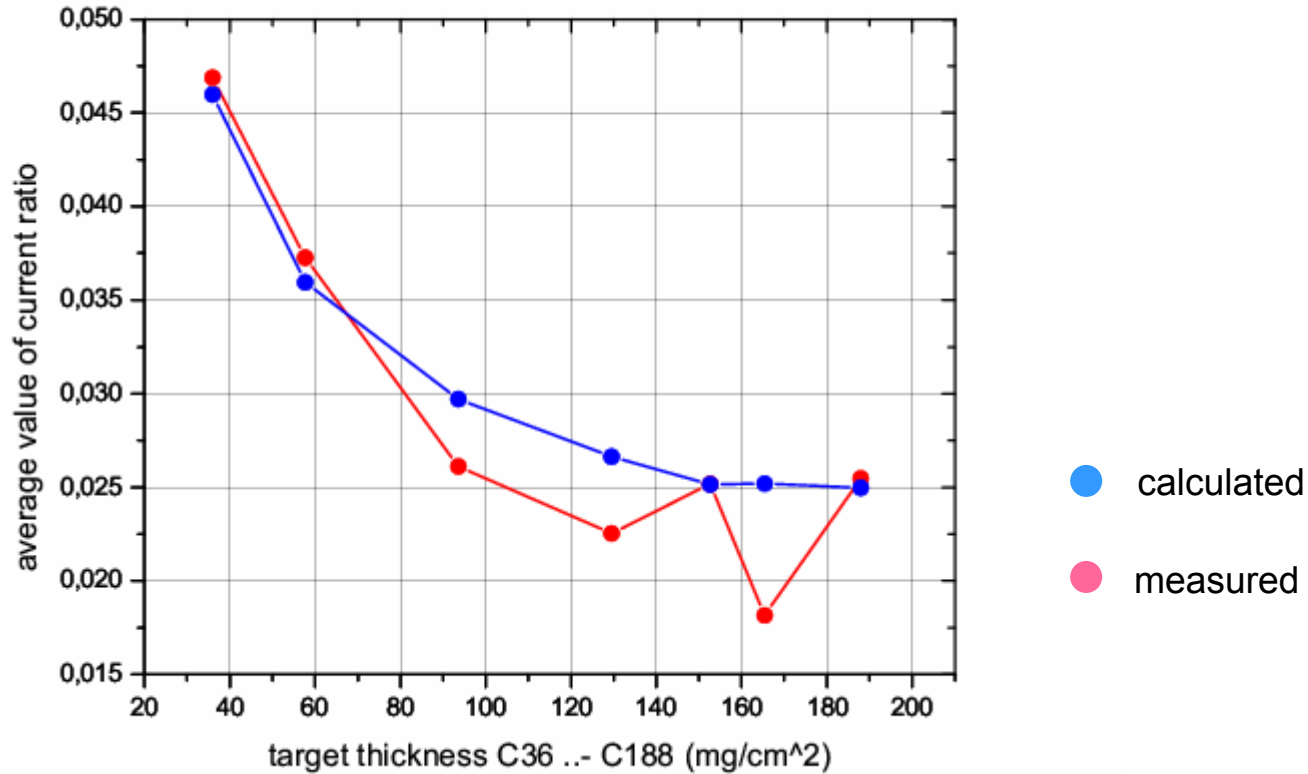
**$^{13}\text{C}(p, \gamma)^{14}\text{N}$**

F. Riess et al., Nucl. Phys. A175, 462 (1971)

**$^{14}\text{N}(\gamma, p)^{13}\text{C}$**

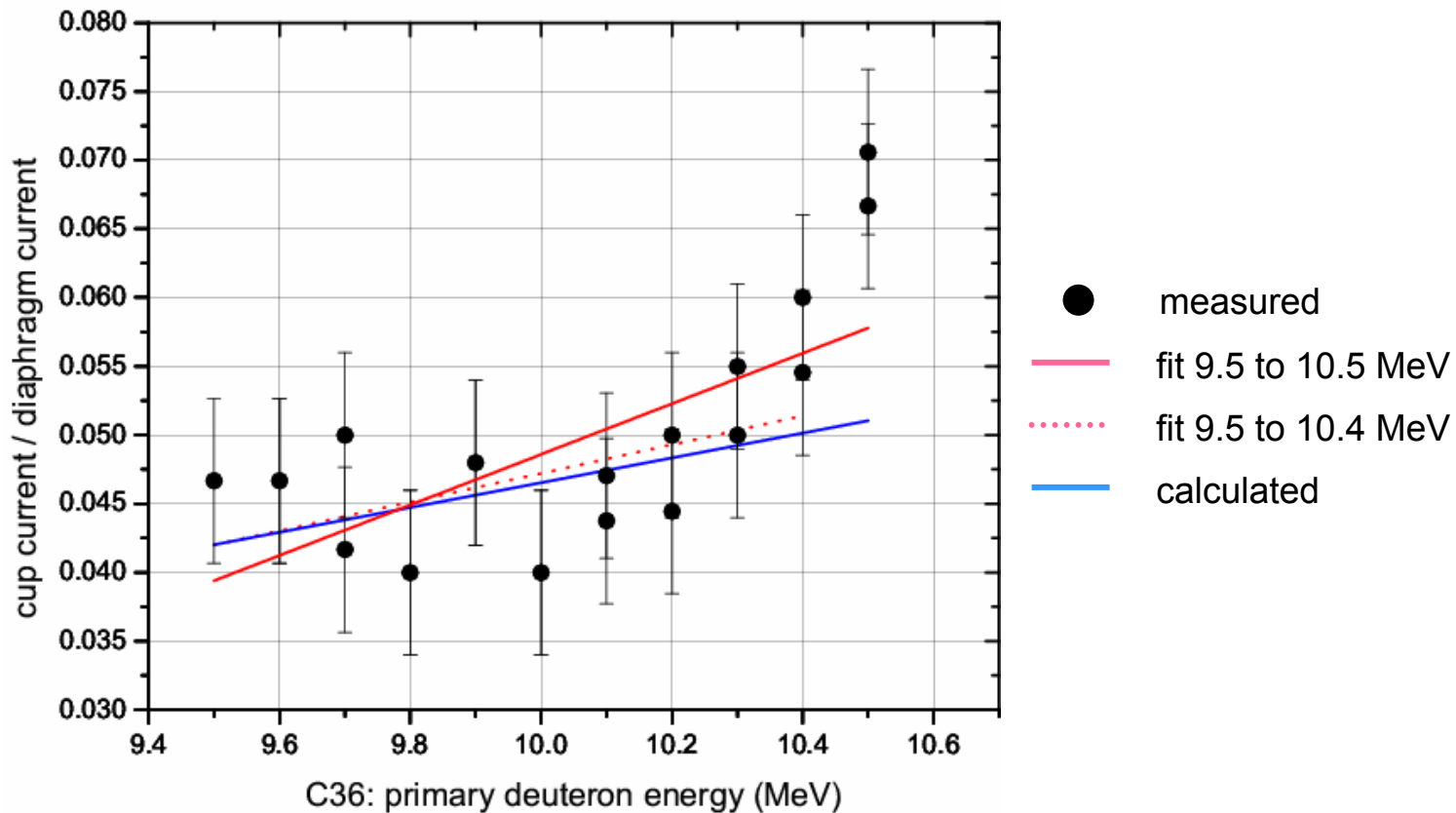
R. Kosiek, K. Maier, and K Schlüpmann,  
Phys. Lett. **9**, 260 (1964)

**Agreement in the peak positions accidental?**



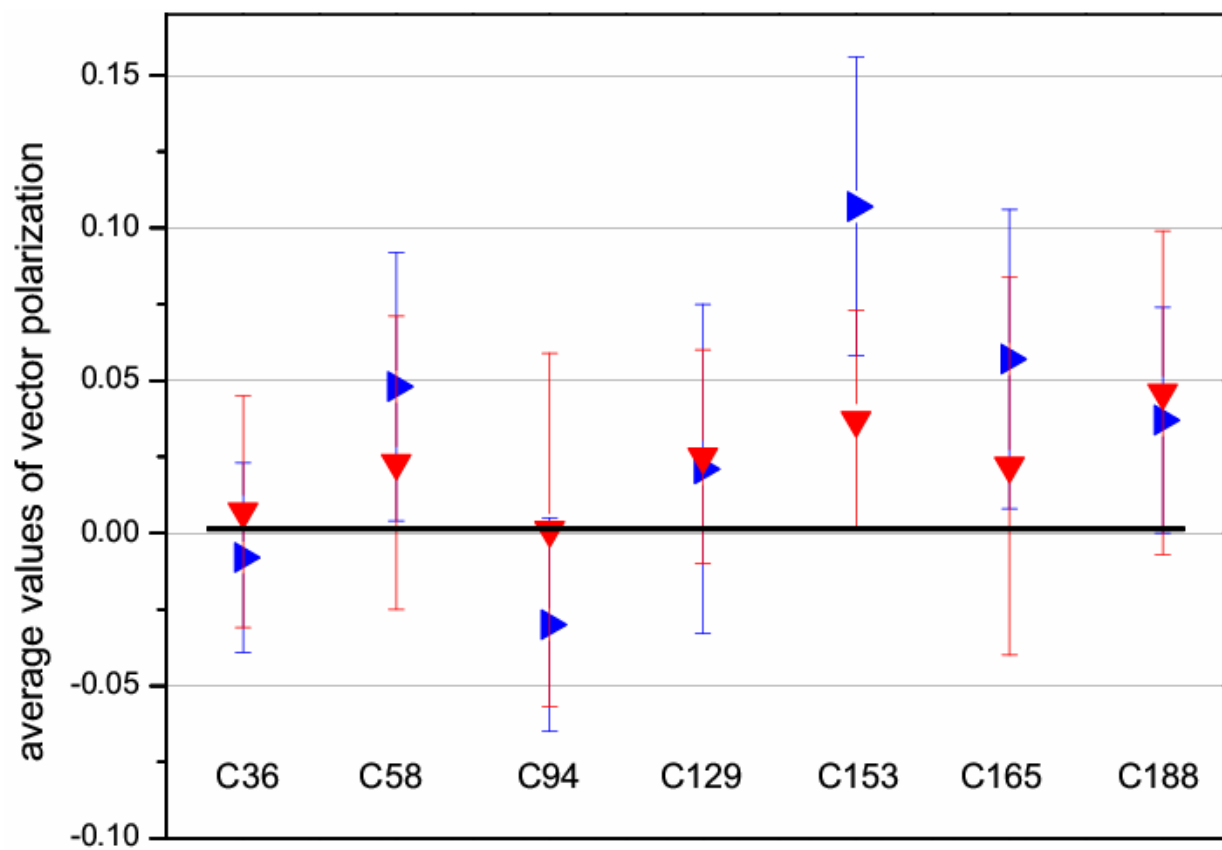
Average values of the ratio  $I_{\text{cup}}/I_{\text{diaphragms}}$  for the 7 carbon targets

Width of the angular distribution  $\sim \frac{1}{v_p} \sqrt{d_{\text{target}}} \rightarrow$  ratio decreases with  $d_{\text{target}}$



Energy dependence of the ratio  $I_{\text{cup}}/I_{\text{diaphragms}}$  for the C36 carbon target

Width of the angular distribution  $\sim (vp)^{-1} \rightarrow$  ratio increases with energy



▼  $(U-D)/(U+D)$

►  $(L-R)/(L+R)$

