

**ПОЛЯРИЗУЕМОСТЬ НУКЛОНА**

**СТАТУС**

**СОВМЕСТНОГО (ПИЯФ-ИКП)  
ЭКСПЕРИМЕНТА НА ЭЛЕКТРОННОМ  
УСКОРИТЕЛЕ В ДАРМШТАДТЕ**



РОССИЙСКАЯ АКАДЕМИЯ НАУК  
ПЕТЕРБУРГСКИЙ ИНСТИТУТ ЯДЕРНОЙ ФИЗИКИ  
ИМ. Б.П.КОНСТАНТИНОВА

2104

NP-12-1996

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A.A. Vorobyov, N.Yu. Zaitsev**

**Compton Scattering on Protons:**

**Project of Experimental  
Determination of Electric  
and Magnetic Polarizabilities  
of the Proton**

**ГАТЧИНА 1996**

The electric and magnetic nucleon polarizabilities of the nucleon,  $\alpha$  and  $\beta$ , characterize the response of its internal structure to applied electric and magnetic fields.

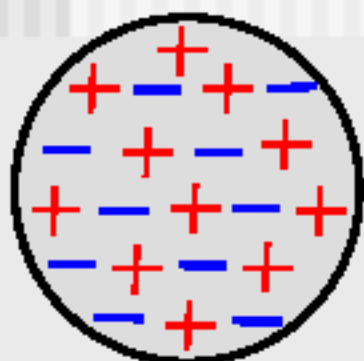
$$\mathbf{d} = \alpha \mathbf{E} \quad \boldsymbol{\mu} = \beta \mathbf{B}$$

$$\bar{\alpha} = 2 \sum_{n \neq N} \frac{|\langle n | D_z | N \rangle|^2}{E_n - E_N} + \Delta\alpha \equiv \alpha_0 + \Delta\alpha,$$

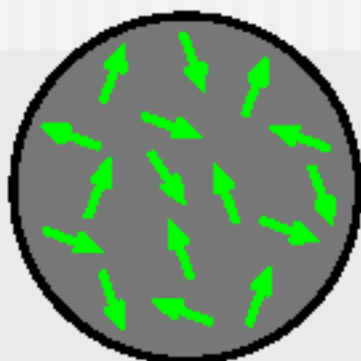
$$\bar{\beta} = 2 \sum_{n \neq N} \frac{|\langle n | M_z | N \rangle|^2}{E_n - E_N} + \Delta\beta \equiv \beta_0 + \Delta\beta.$$

**electric polarizability:  
separation of charge**

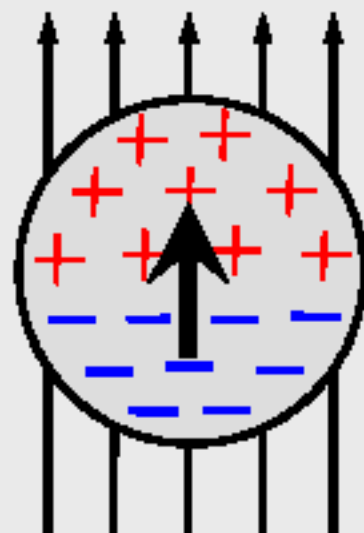
**paramagnetic polarizability:  
moments align with  $B$**



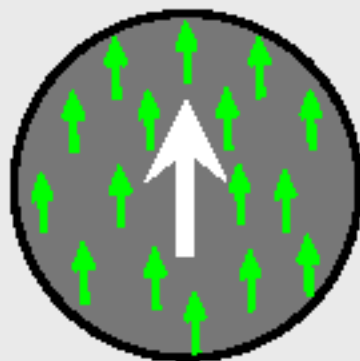
$$D = 0$$



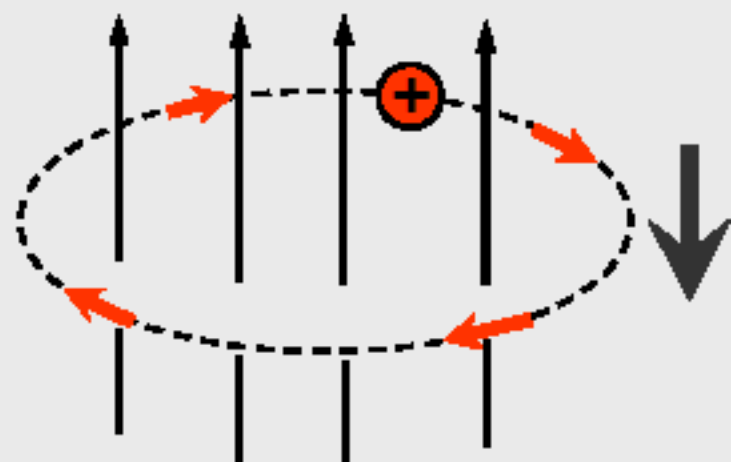
$$M = 0$$



$$D = \alpha E$$



$$M = \beta_{para} B$$



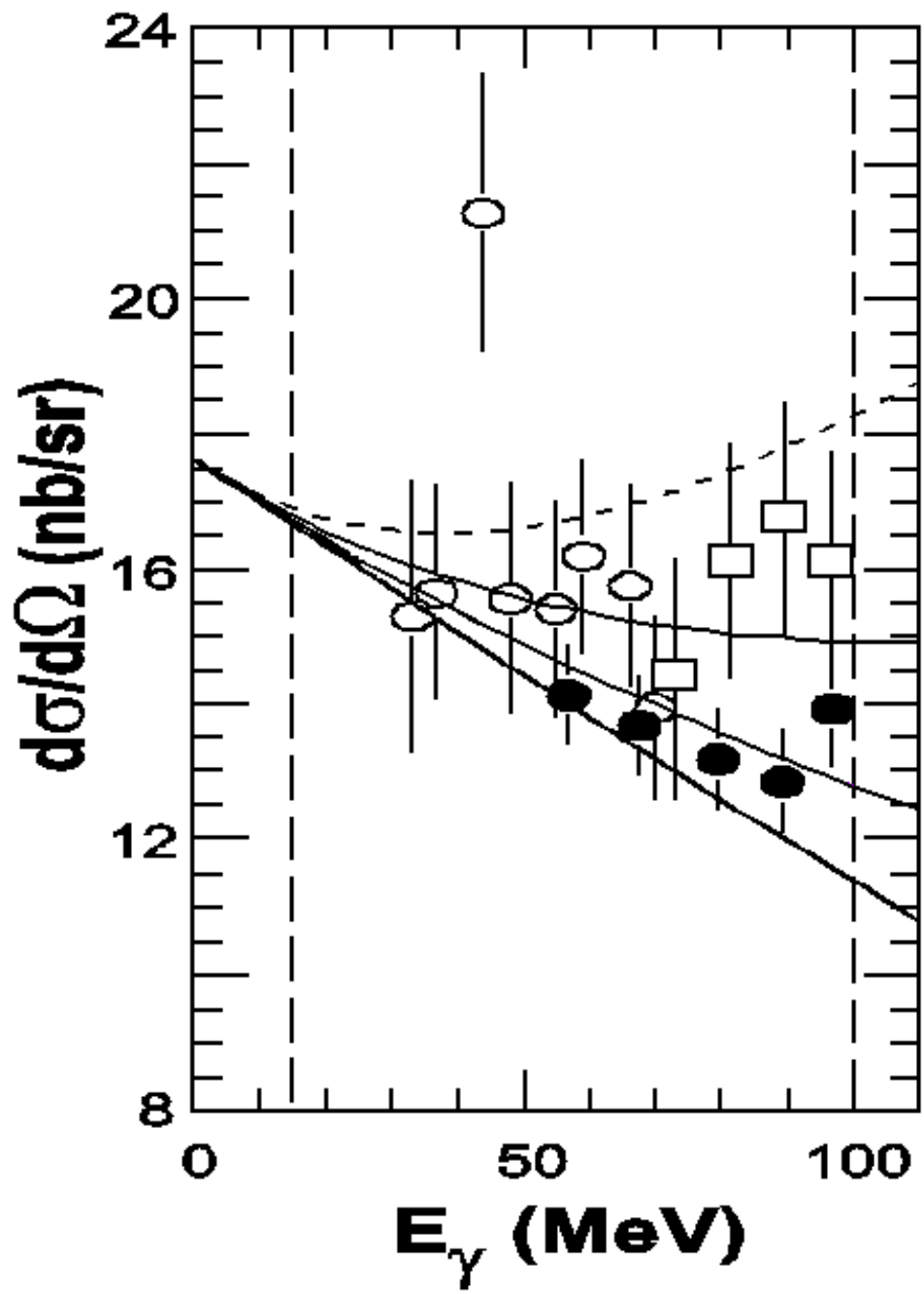
$$M = \beta_{dia} B$$

**diamagnetic polarizability:  
induced current opposes  $B$**

## Cross section for Compton scattering

$$\left[ \frac{d\sigma(E_\gamma, \theta)}{d\Omega} \right]_{\text{LET}} = \left[ \frac{d\sigma(E_\gamma, \theta)}{d\Omega} \right]_{\text{Powell}} - \rho + \mathcal{O}(E_\gamma^4)$$

$$\rho = \frac{e^2}{4\pi m_p} \left( \frac{E_{\gamma'}}{E_\gamma} \right)^2 \frac{E_\gamma E_{\gamma'}}{(\hbar c)^2} \times$$
$$\times \left[ \frac{\bar{\alpha} + \bar{\beta}}{2} (1 + \cos \theta)^2 + \frac{\bar{\alpha} - \bar{\beta}}{2} (1 - \cos \theta)^2 \right]$$

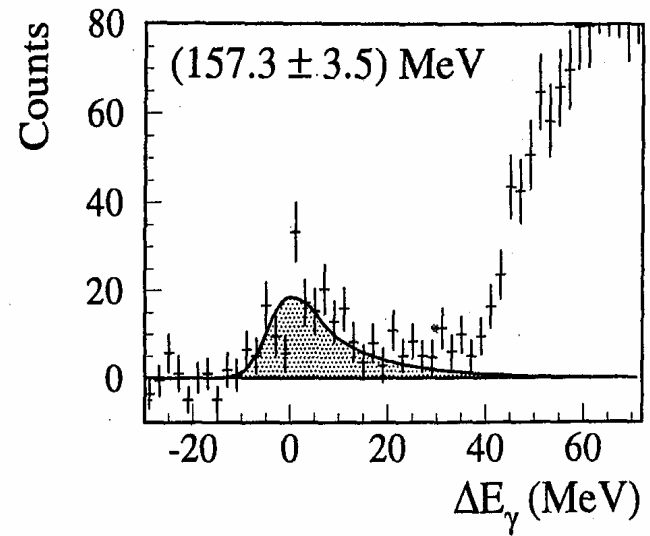
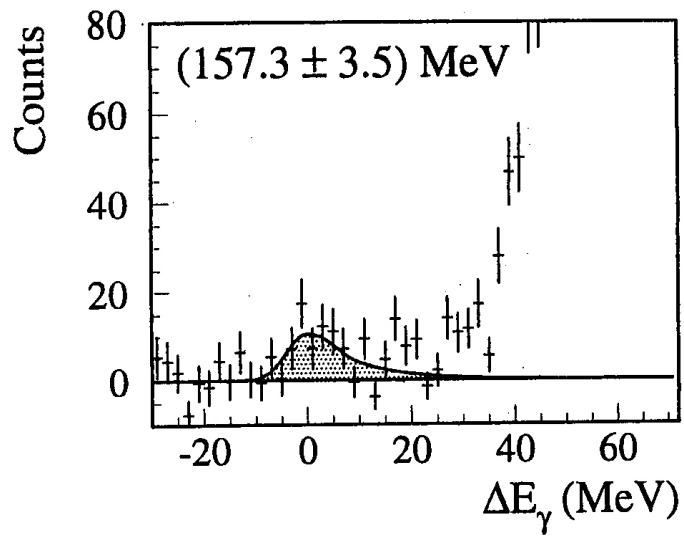
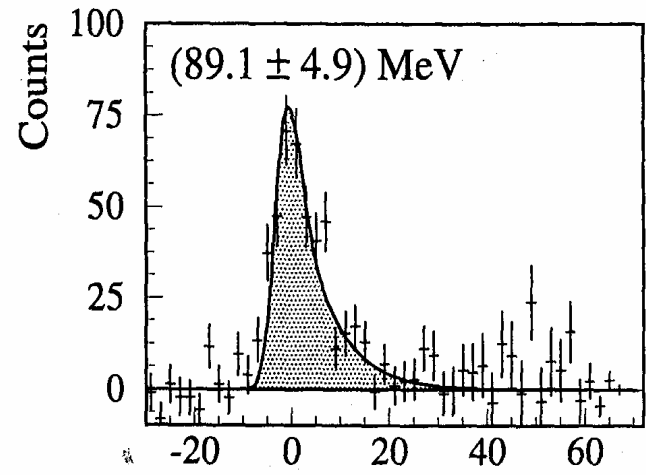
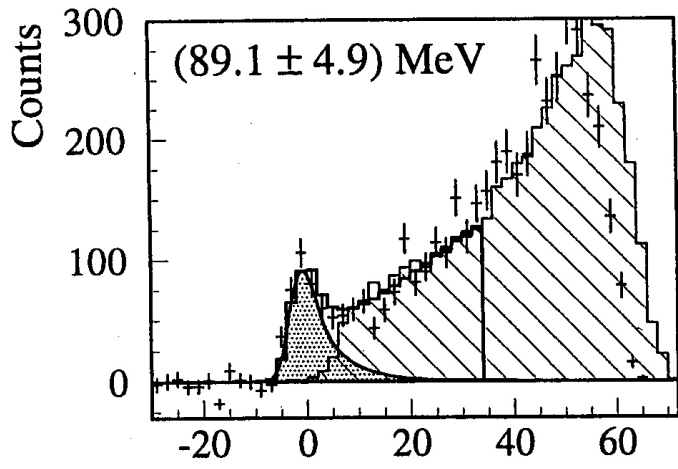


**Born cross section**

$\bar{\alpha} = 9 \cdot 10^{-4} \text{ fm}^3$

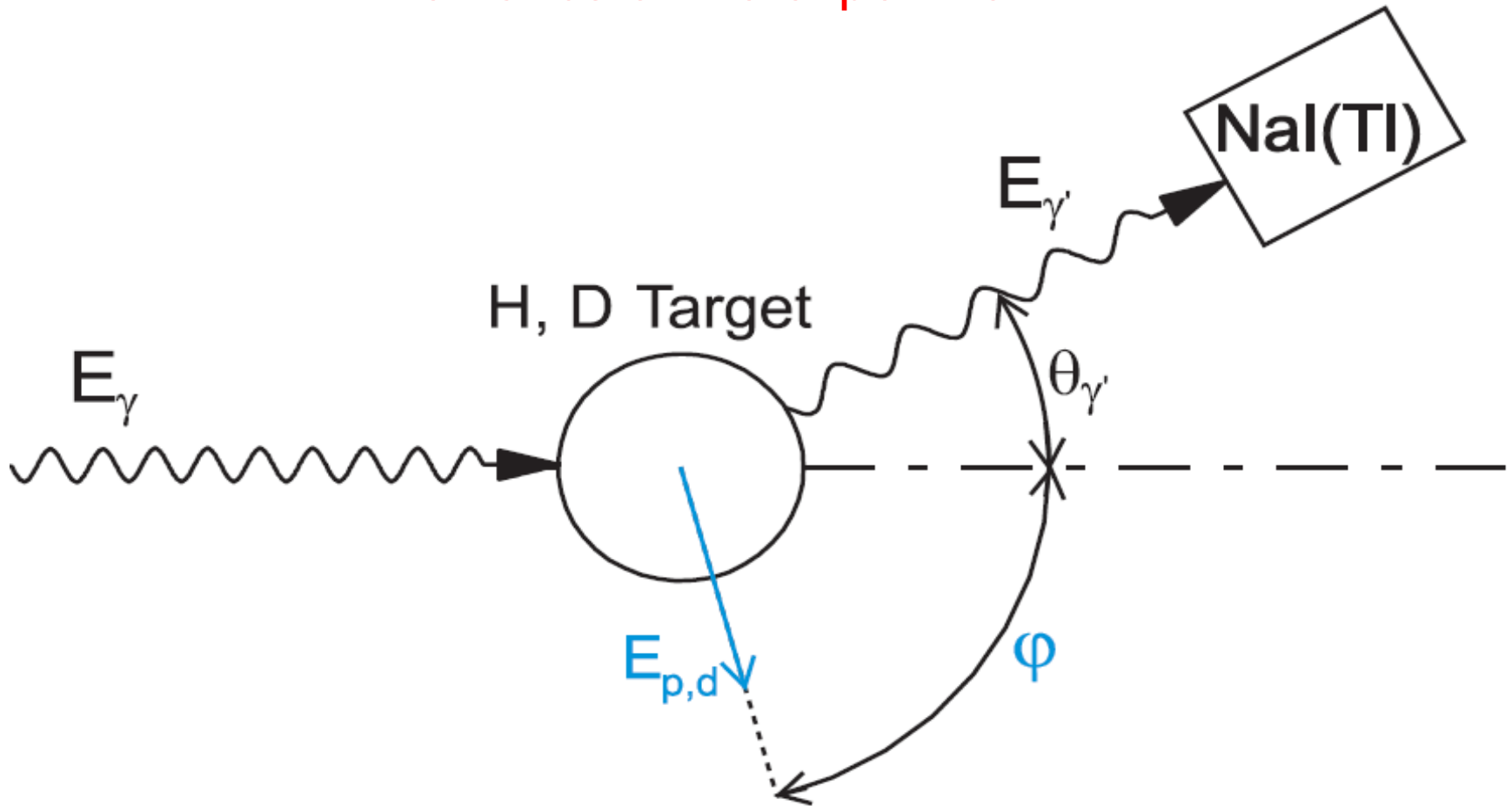
$\bar{\alpha} = 17 \cdot 10^{-4} \text{ fm}^3$

- Urbana, 1991
- SAL, 1995
- TAPS 2001



V. Olmos de Leon et al., Eur. Phys. J. A 10, 207 (2001).

## Kinematics of the experiment

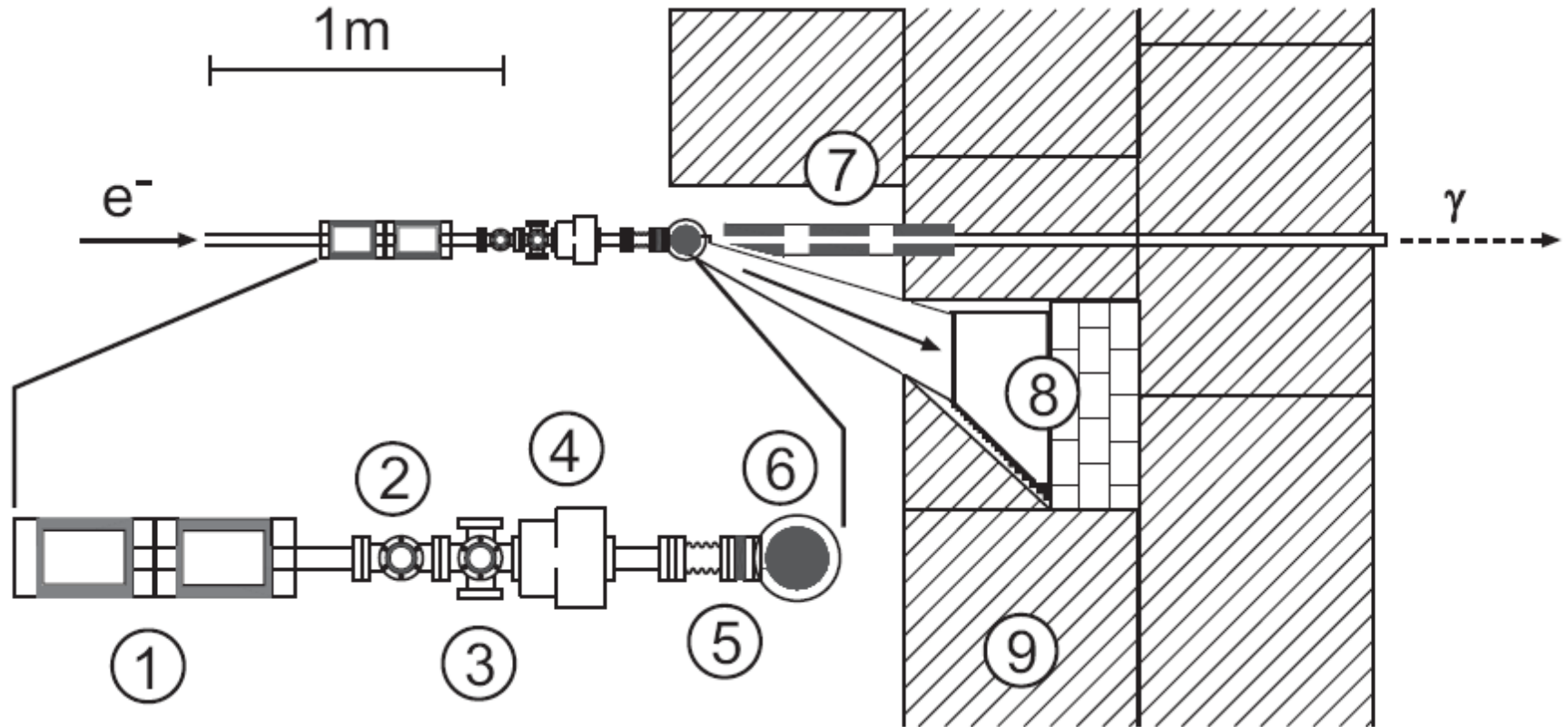


$$\phi \sim 90^\circ - \theta_{\gamma'}/2$$

$E_{p,d}$  is measured with the help of the ionization chambers

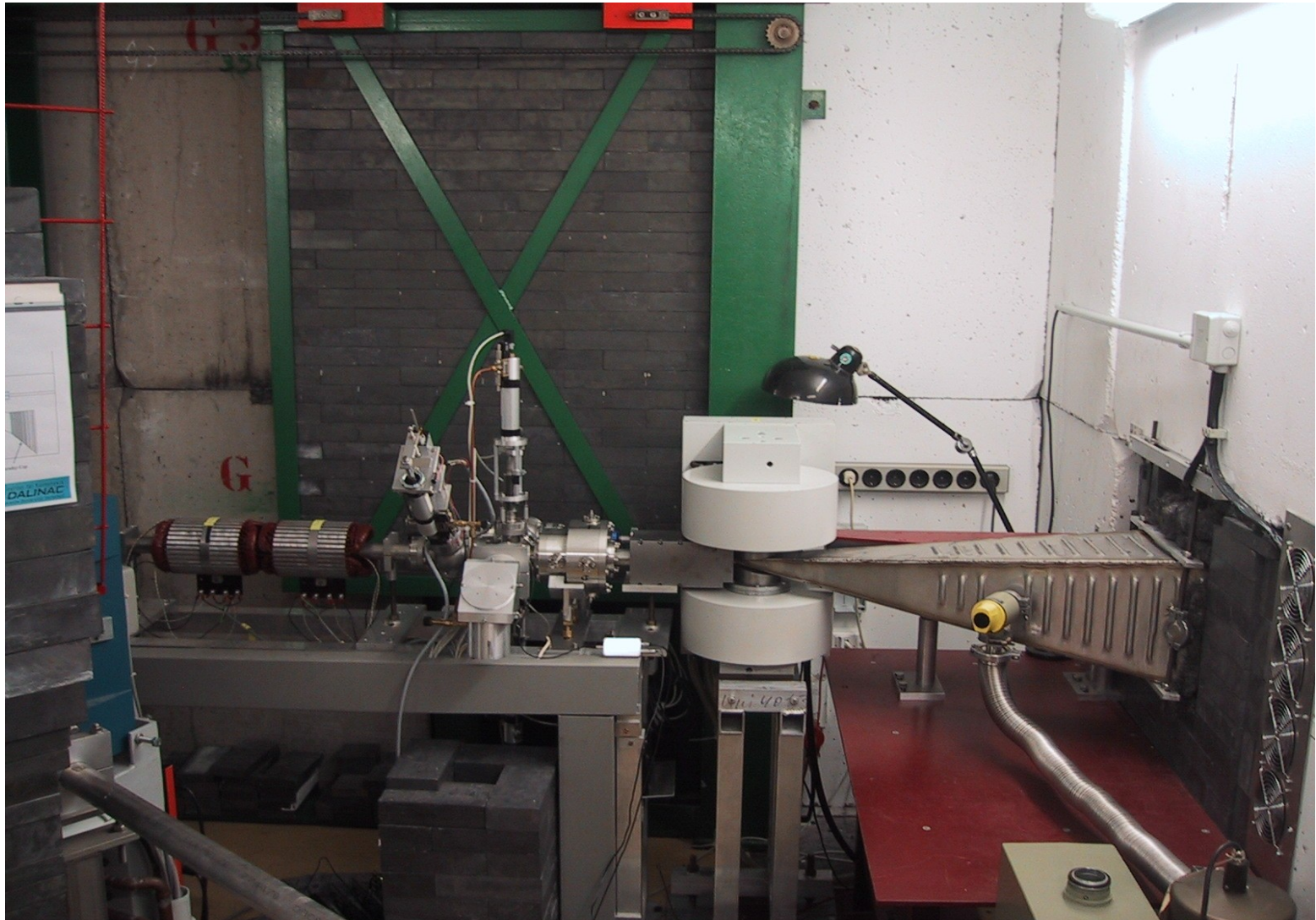


## Schematic view of the bremsstrahlung facility

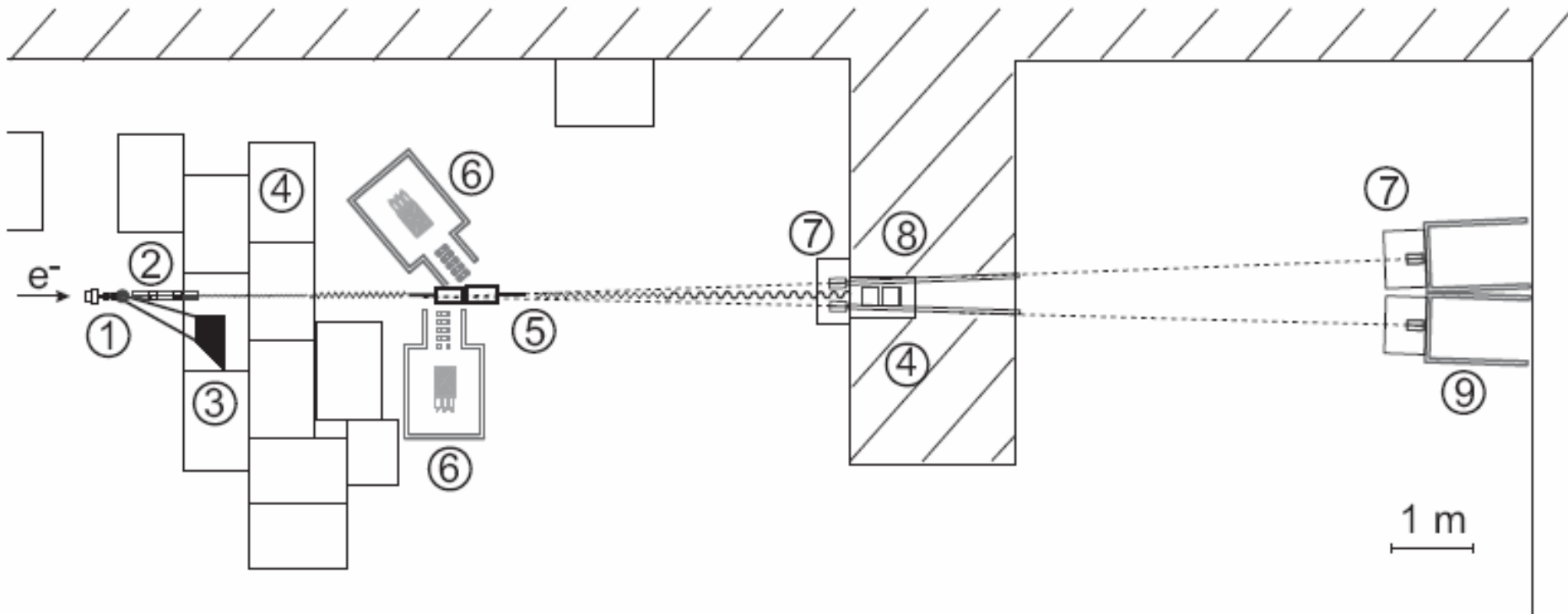


1 – direction correcting magnets, 2 – wire scanner, 3 – targets for beam position control, 4 – beam intensity and position rf monitor, 5 – bremsstrahlung converter target, 6 – cleaning magnet, 7 –  $\gamma$ - beam collimator, 8 – electron beam dump, 9 – concrete shielding

# Bremsstrahlung facility

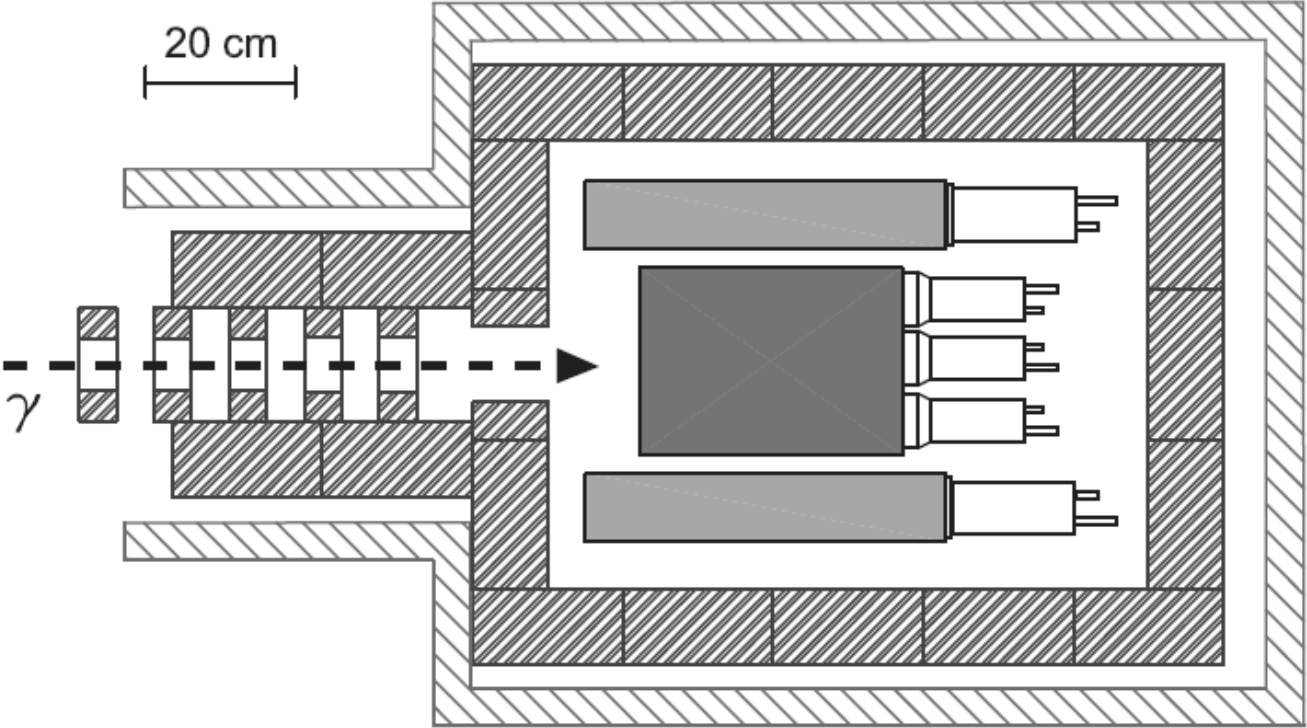


## Schematic view of the experimental setup



1 – bremsstrahlung converter, 2 – collimation system, 3 – electron beam dump, 4 – concrete shielding, 5 – hydrogen-filled ionization chambers, 6 –  $\gamma$  spectrometers, 7 – collimation system, 8 – position sensitive ionization chamber, Gaussian quantometer,  $\gamma$  beam dump, 9 –  $\gamma$  spectrometers

# Schematic view of a 10" x 14" NaI(Tl) spectrometer



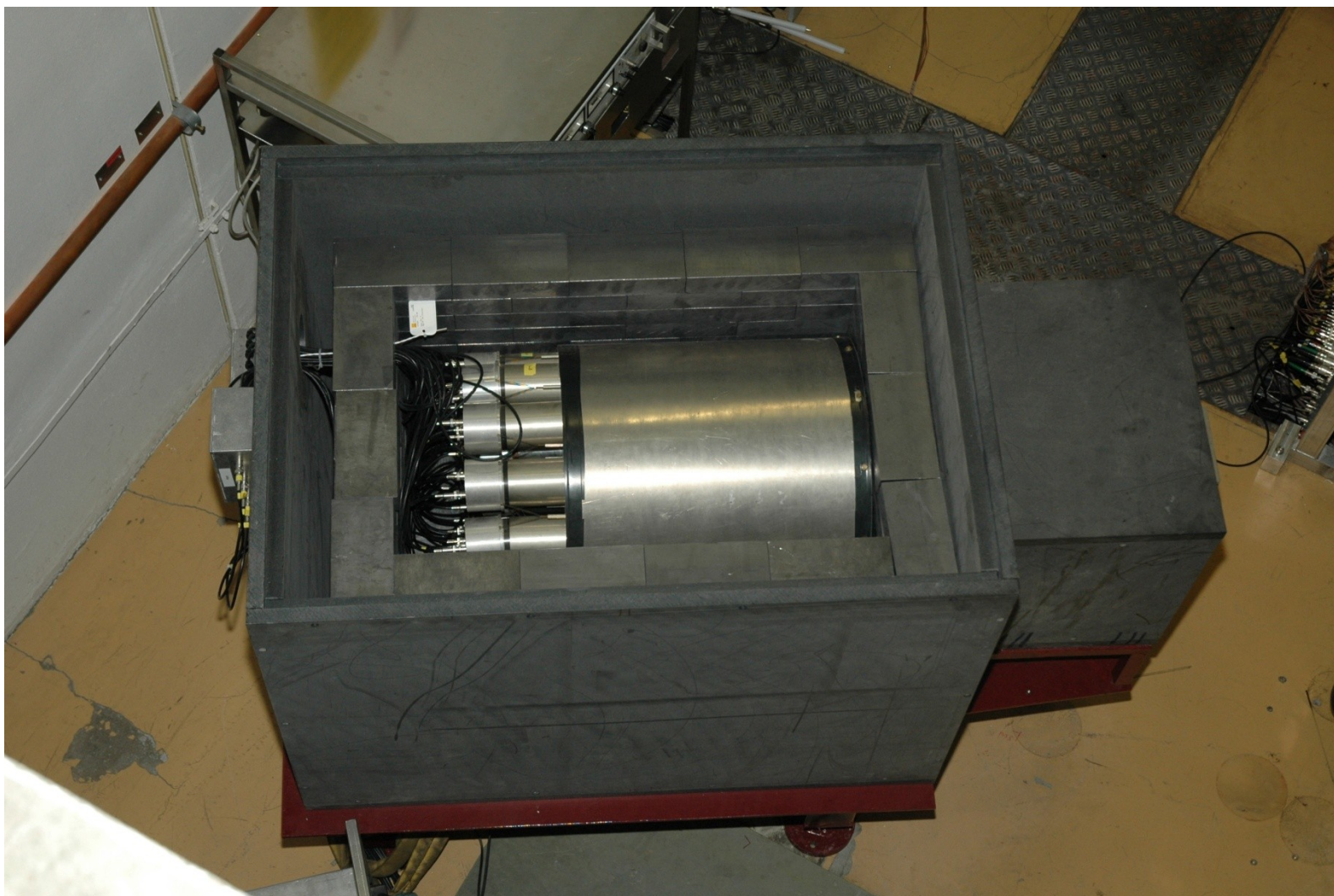
NaI(Tl) Crystal

Lead

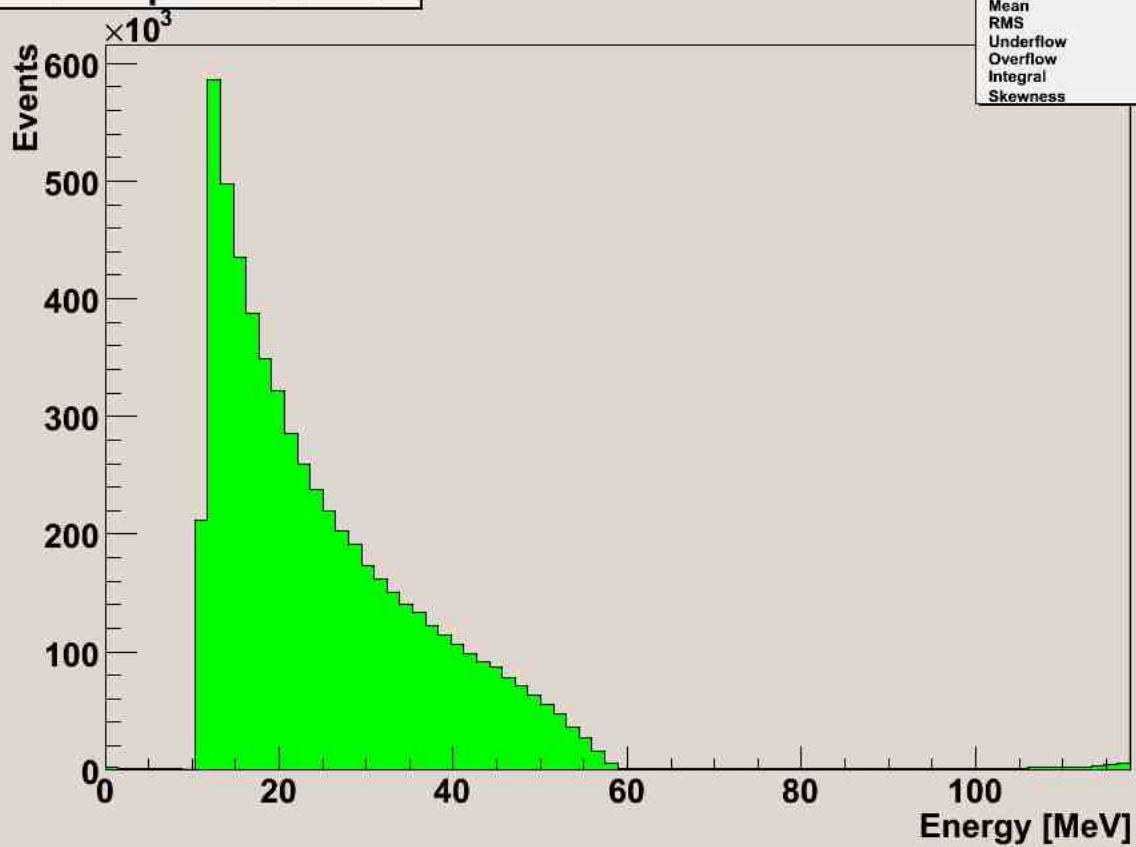
Plastic Scintillator

Boron treated Polyethylene

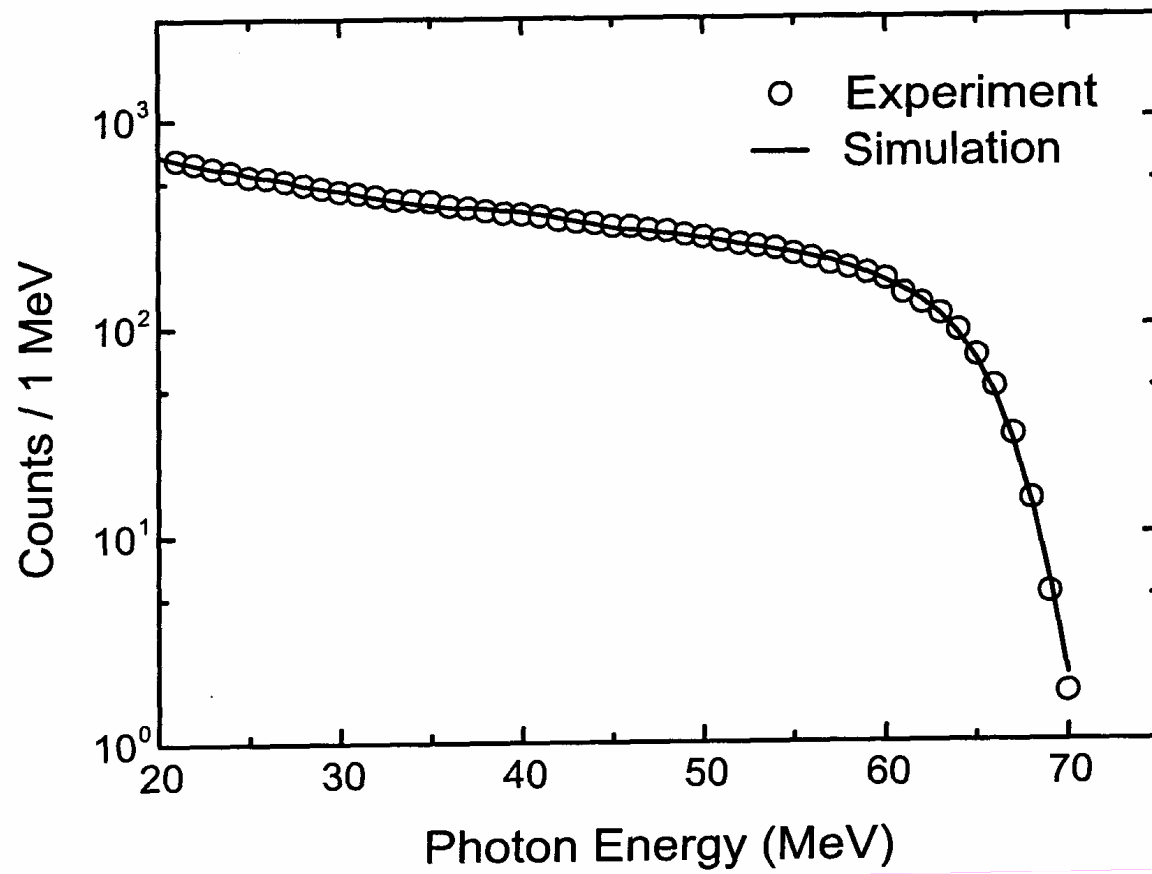
# Nal(Tl) spectrometer



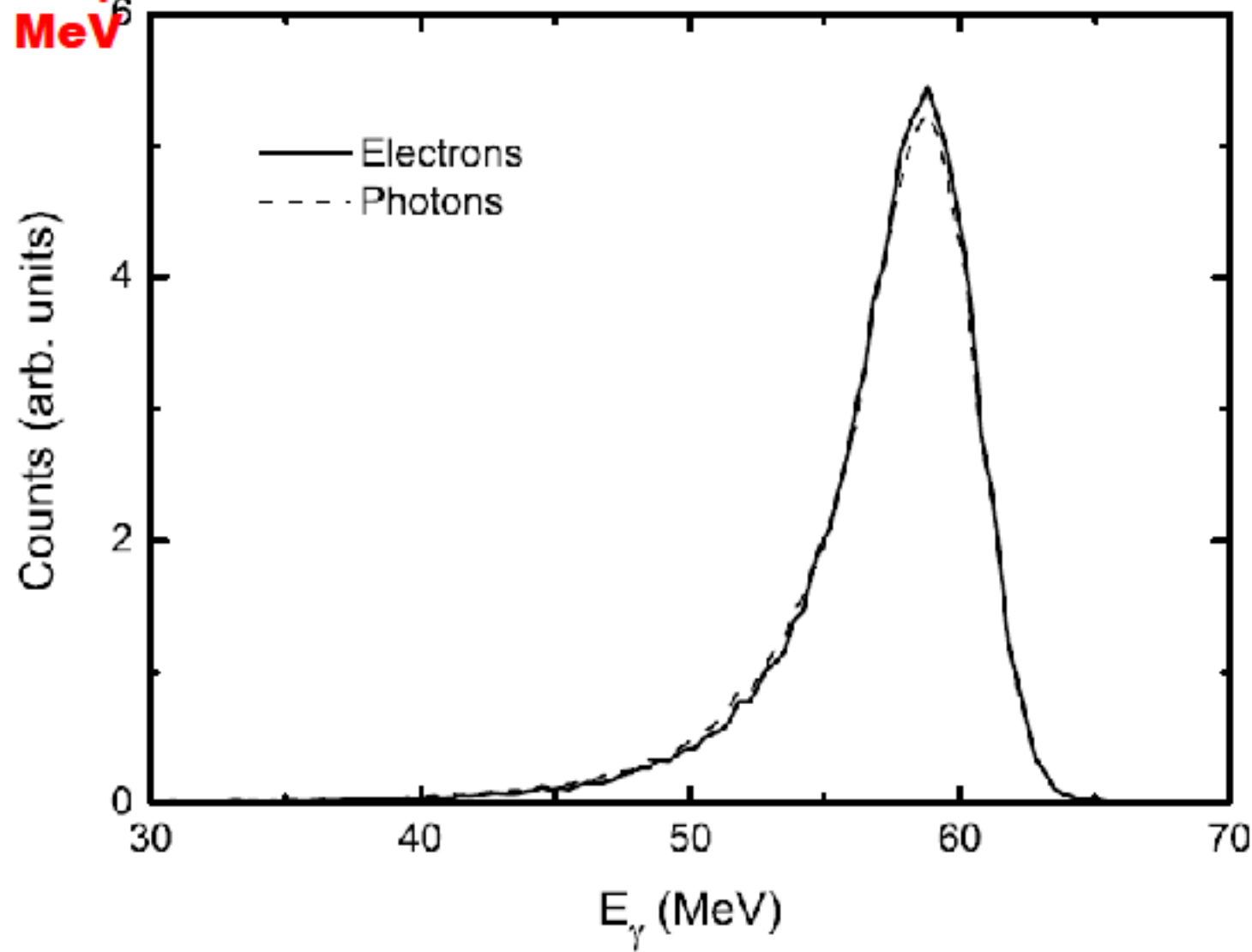
Nal L 2p42 18:52:29



Nal links	
Entries	6064151
Mean	25.3
RMS	13.08
Underflow	0
Overflow	4.588e+04
Integral	6.018e+06
Skewness	2.028

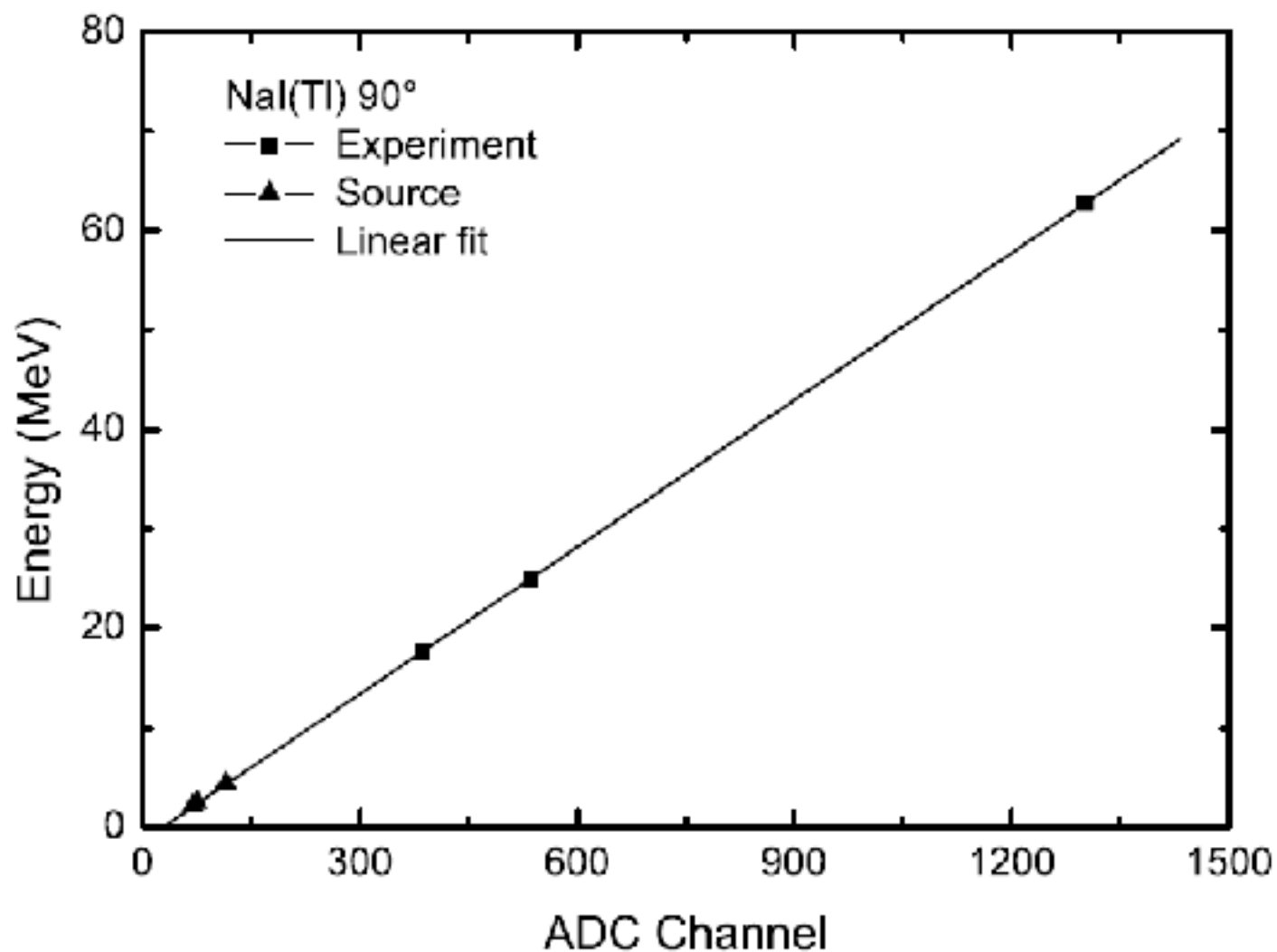


**Response function for a 10" x 14" NaI detector for E = 60 MeV**

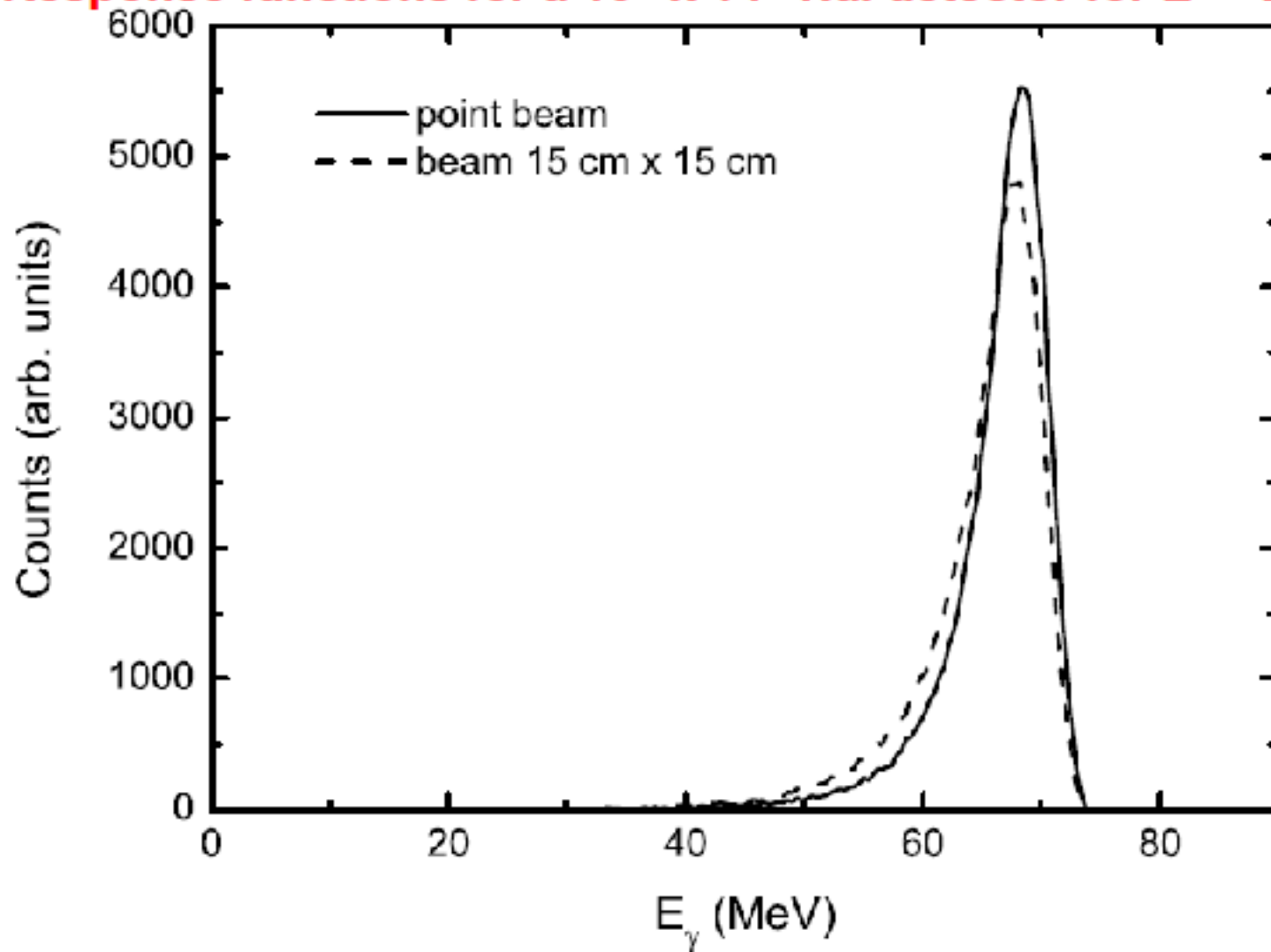




## Energy calibration of one of the NaI spectrometers



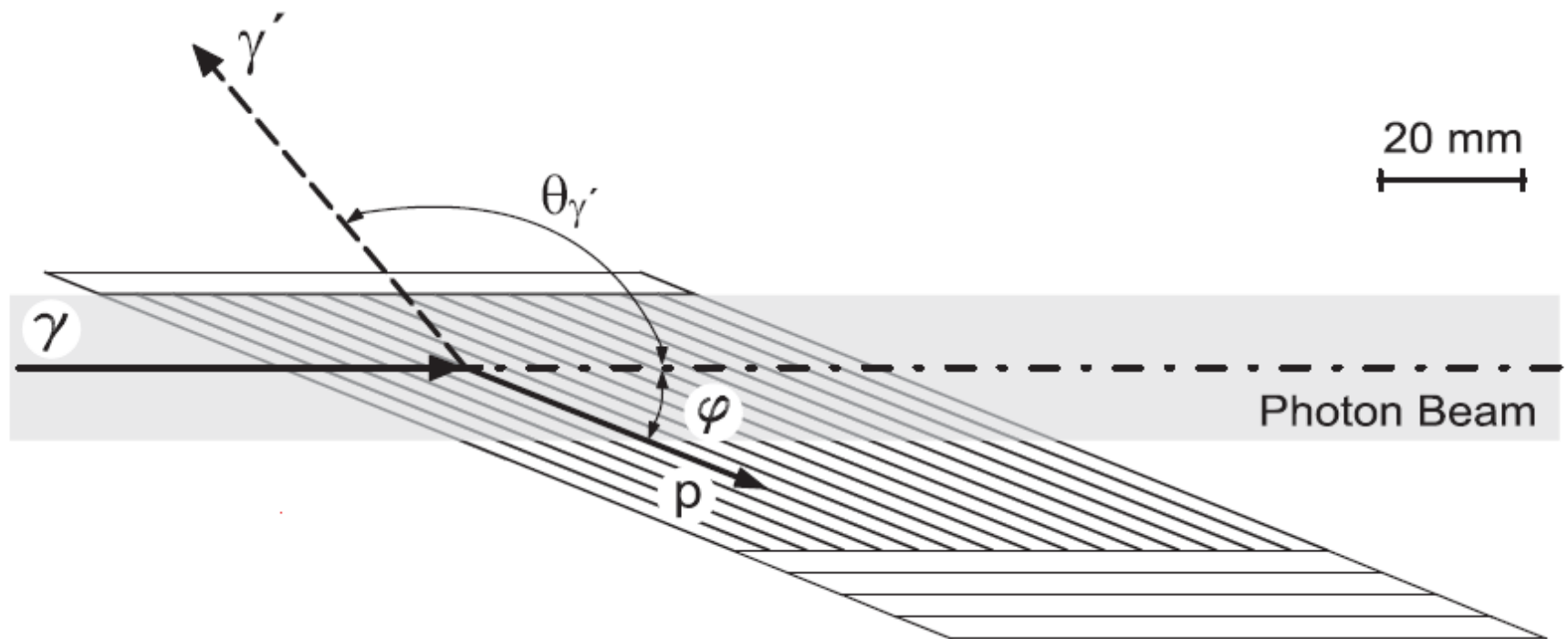
▲ – 60Co (1.3 MeV) and Am-Be (4.4 MeV)  $\gamma$  sources; ■ – calibration with e-A scattering

**Response functions for a 10" x 14" NaI detector for  $E = 70$  MeV**

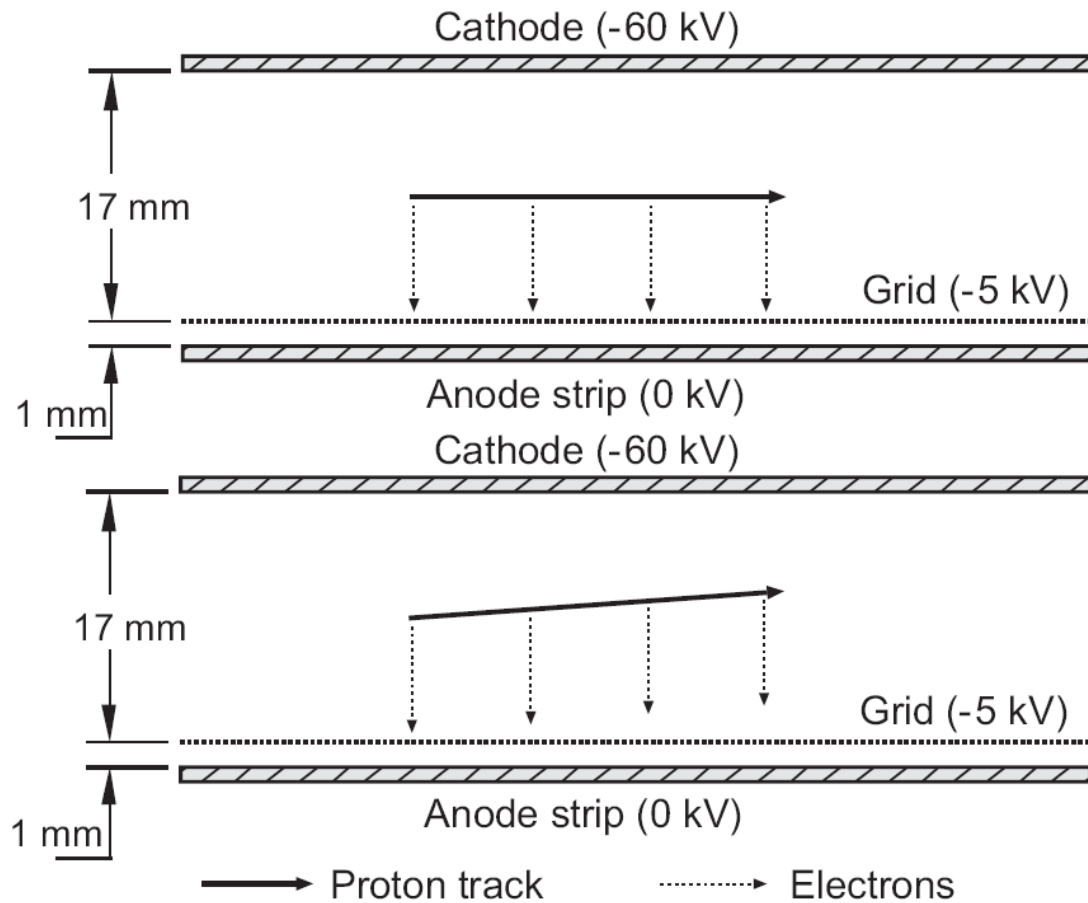
# High-pressure (90 bar) hydrogen-filled ionization chambers at TUD



## Anode-strips geometry (top view)

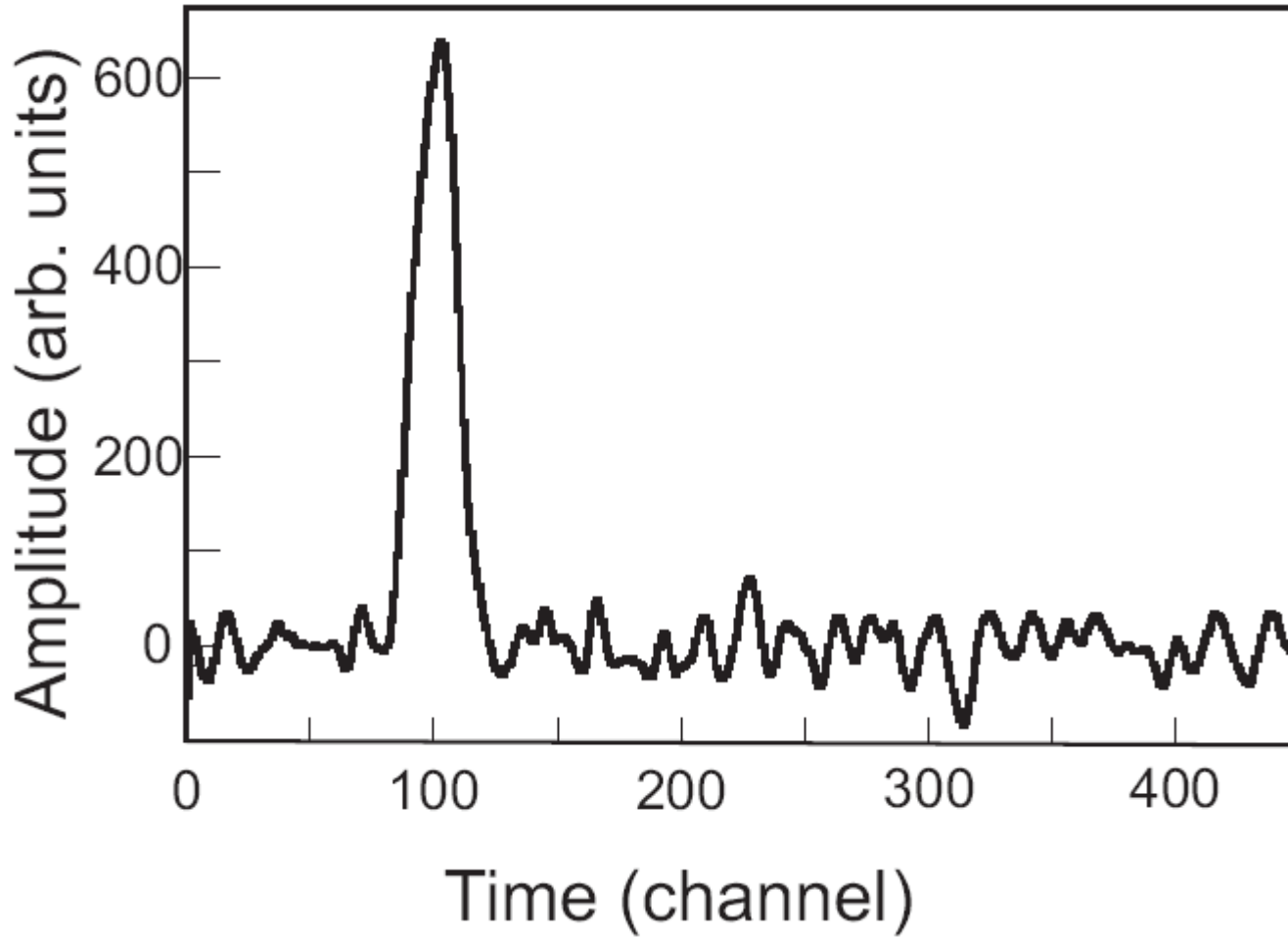


## Cathode-grid-anode geometry of the chambers (side view)

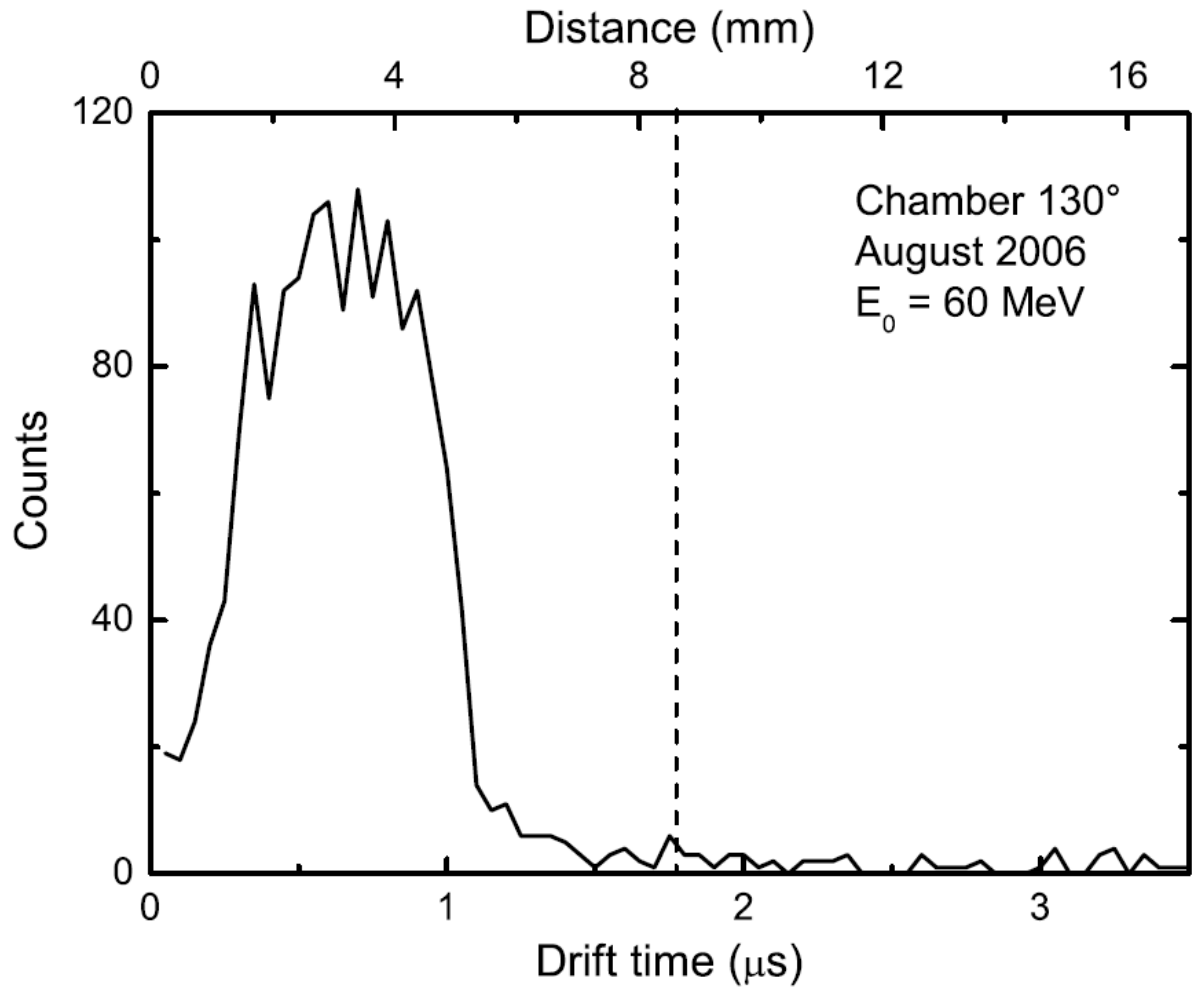


Maximum drift time is  $\sim 3.5 \mu\text{s}$

**A signal on the anode of the ionization chamber from a recoil proton**

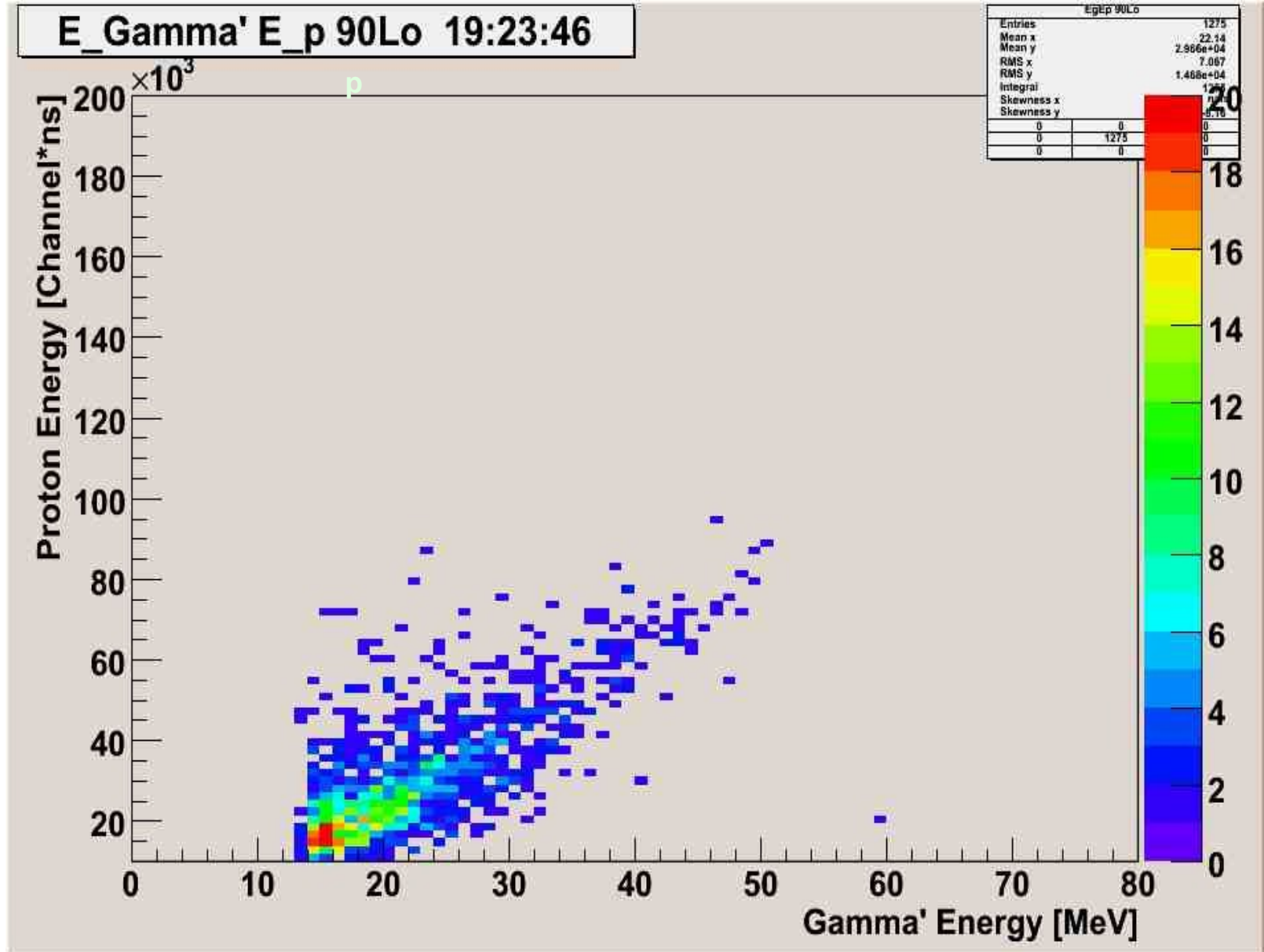


# Drift-time distribution of signals from recoil protons



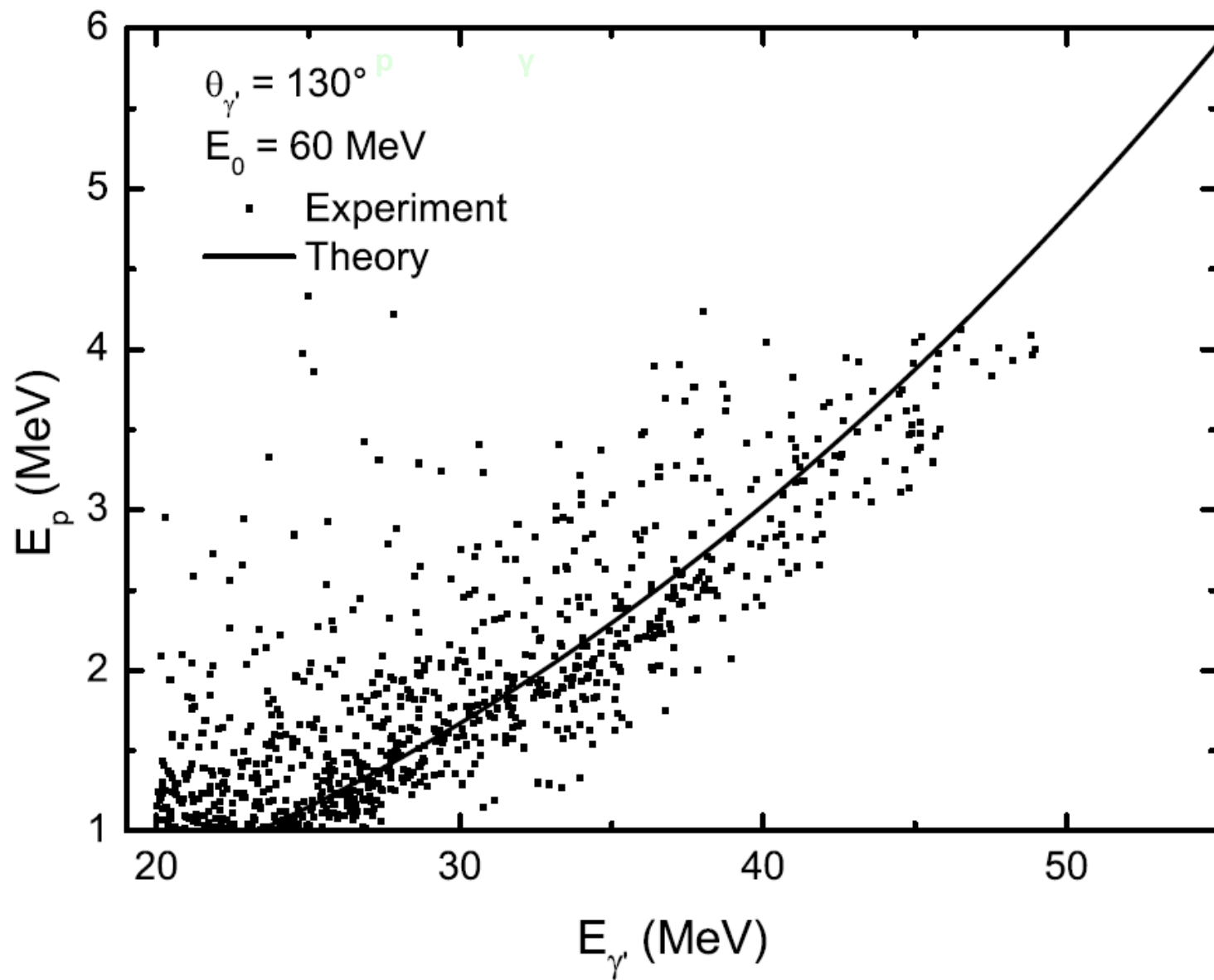
Drift velocity is  $\sim 5 \text{ mm}/\mu\text{s}$

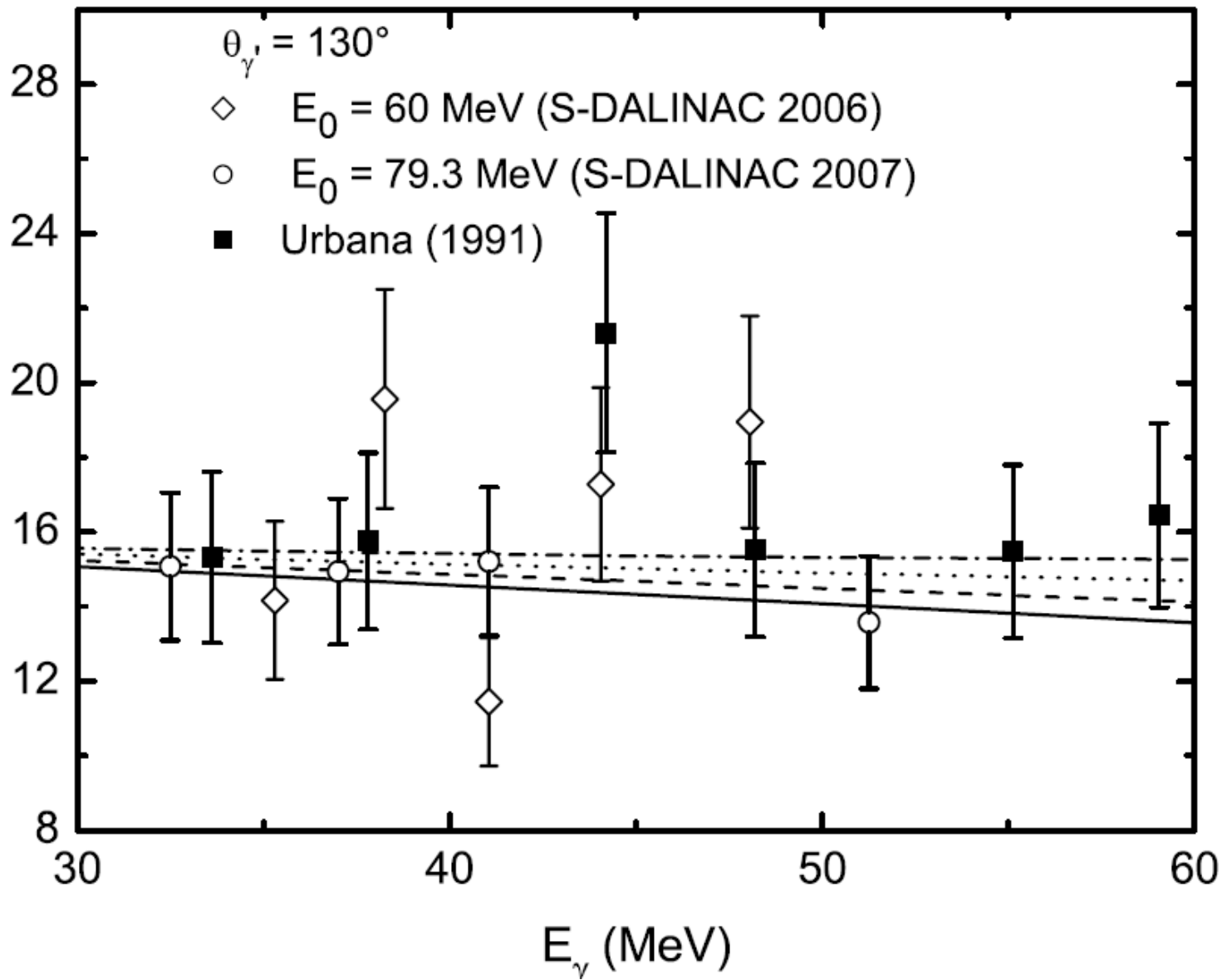
# Ep - Ey correlation





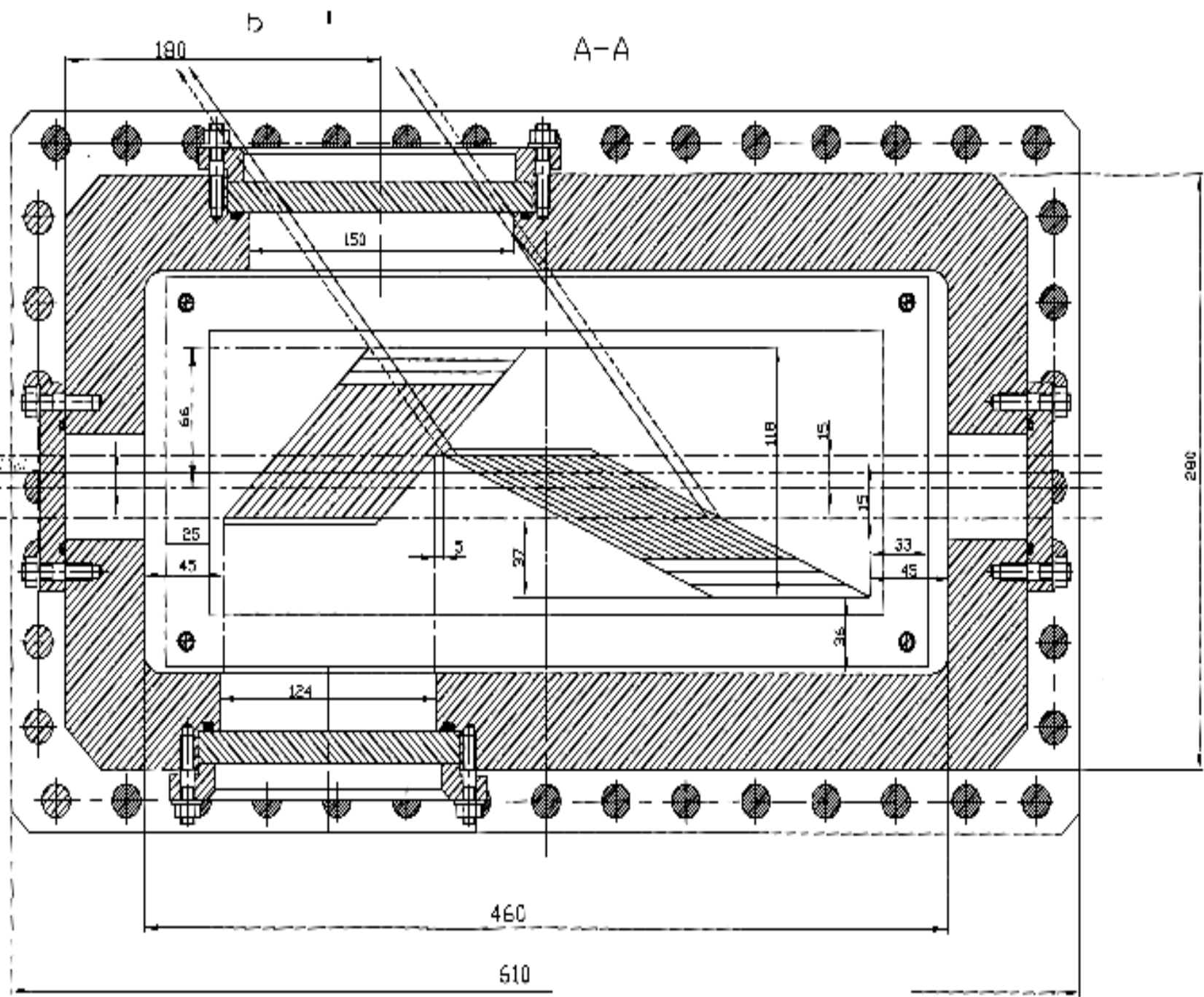
# Ep - E<sub>γ</sub> correlation

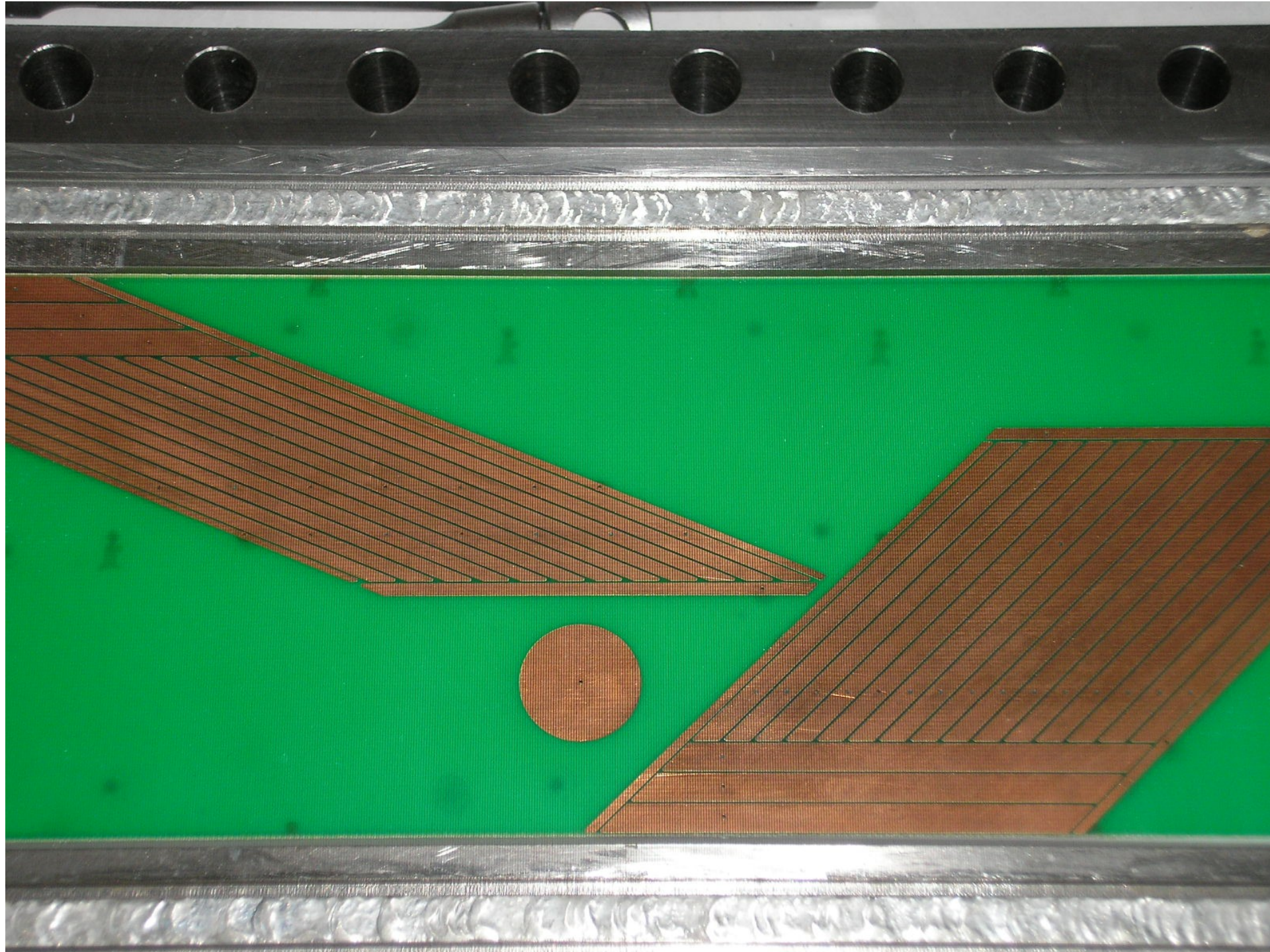


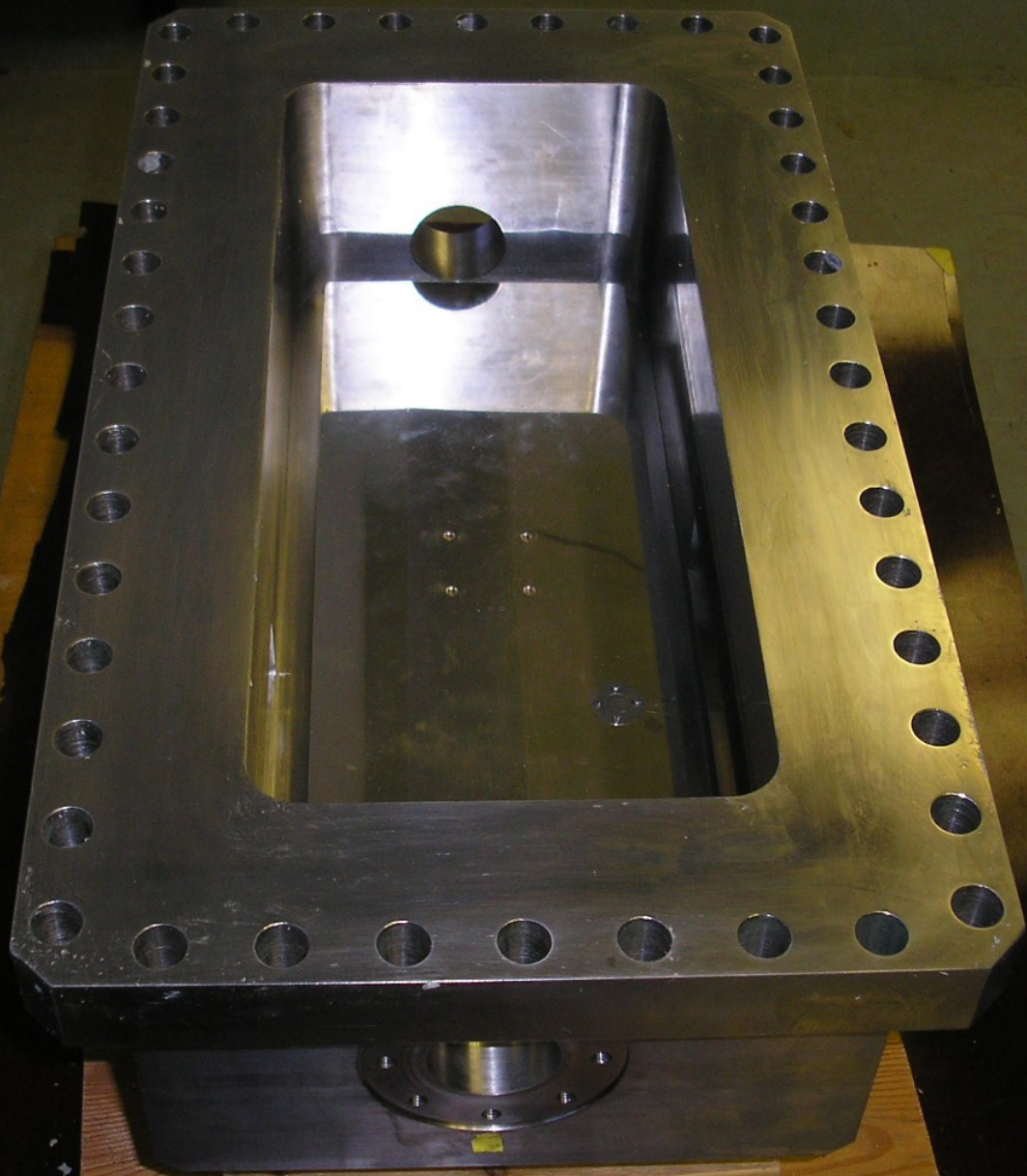


**Differential cross-section  $\gamma p$ - scattering ( $d\sigma/d\Omega$  (nb/sr))**

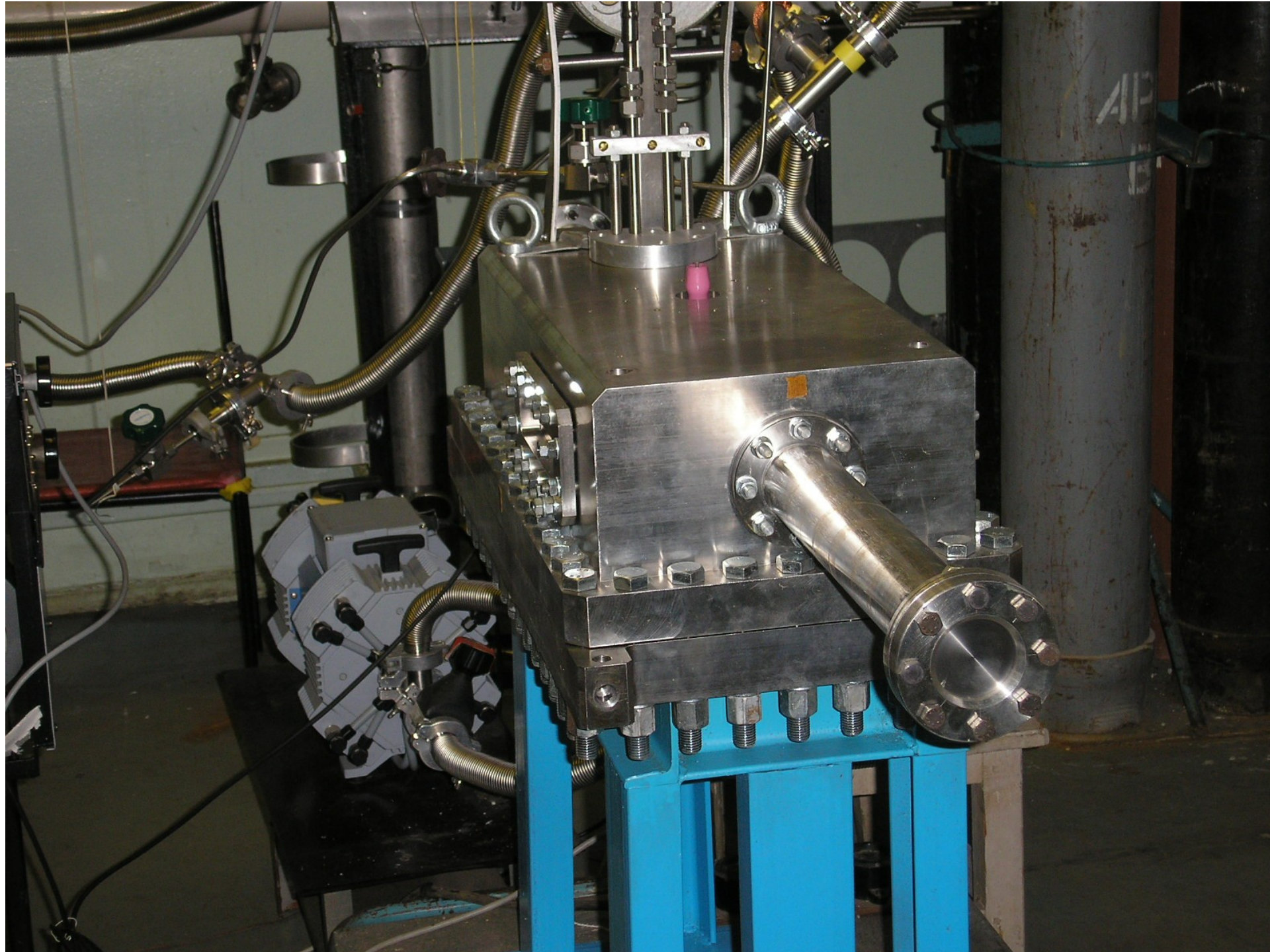
Лента конвейера  
Станок

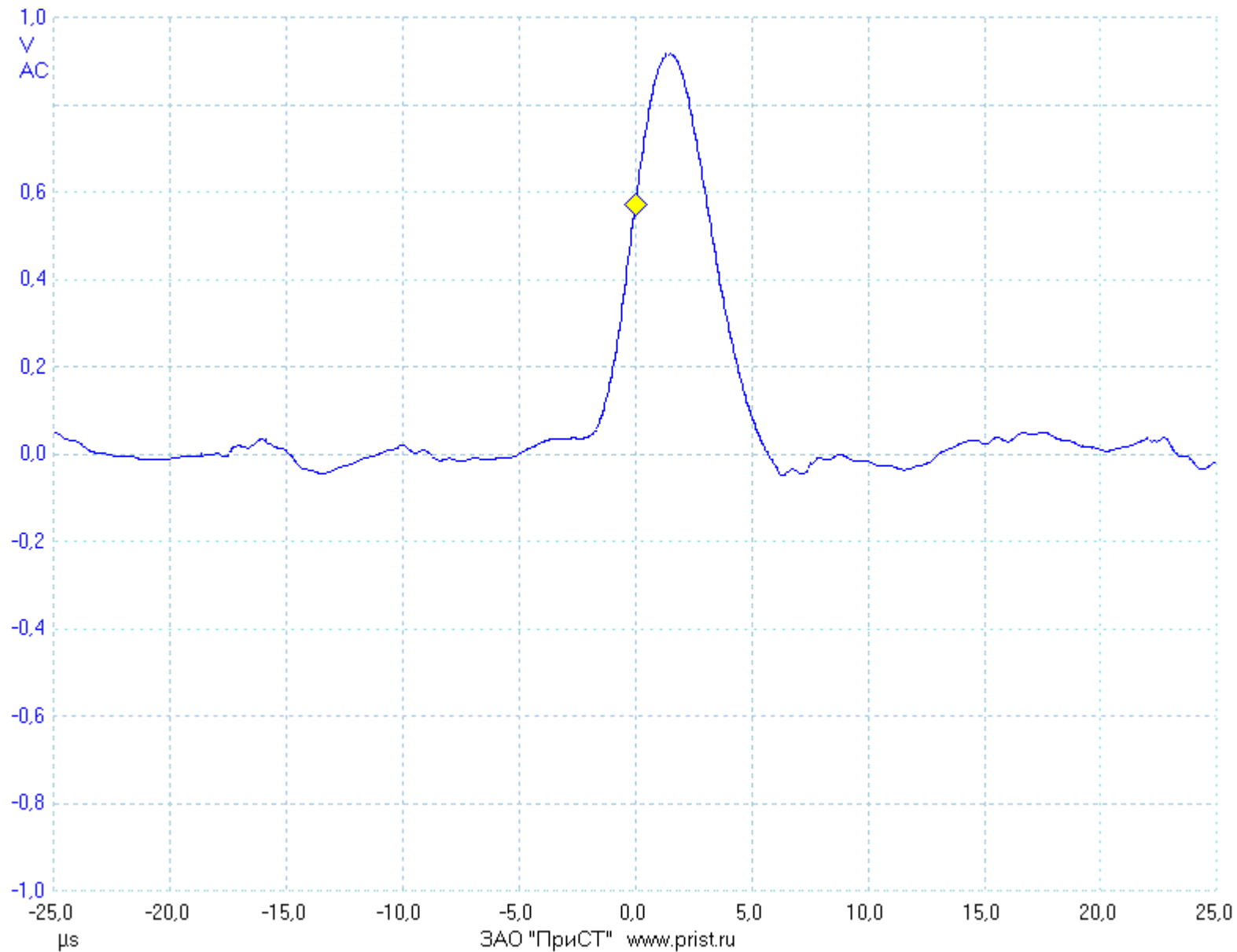












ЗАО "ПриСТ" [www.prist.ru](http://www.prist.ru)

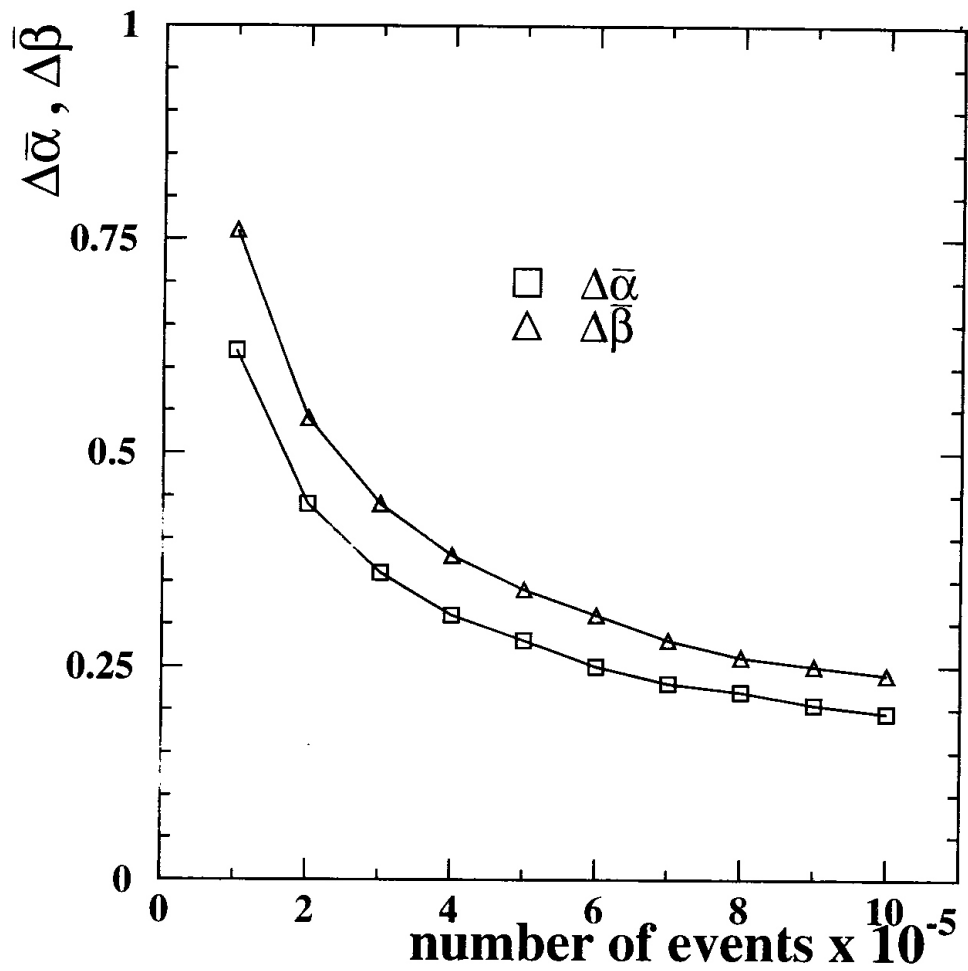


## COUNTING RATE INCREASE WITH THE NEW IC CHAMBER

	<b>NEW IC</b>	<b>OLD IC</b>	<b>COUNTING RATE INCREASE</b>
<b>Target length</b>	<b>90 mm</b>	<b>60 mm</b>	<b>1.5</b>
<b>Target width</b>	<b>30 mm</b>	<b>20 mm</b>	<b>1.5</b>
<b>Target height</b>	<b>15 mm</b>	<b>10 mm</b>	<b>1.5</b>

	<b>NEW NaI-IC geometry</b>	<b>OLD NaI-IC geometry</b>	<b>COUNTING RATE INCREASE</b>
<b>IC to NaI distance</b>	<b>60 cm</b>	<b>110 cm</b>	<b>3.3</b>
<b>Horizont. Be window size</b>	<b>15 cm</b>	<b>10 cm</b>	
<b>Vertical Be window size</b>	<b>34 mm</b>	<b>20 mm</b>	

**TOTAL COUNTING RATE INCREASE ~ 10**



Statistical errors in determination of  $\alpha$  and  $\beta$

## BEAM TIME ESTIMATION

### Minimum scenario:

$I = 3 \mu\text{A}$ ,  $E = 60 \text{ MeV}$ ,  $T = 500 \text{ h}$  (3 weeks)

$N = 50\,000$  events,  $\Delta\alpha \sim 0.8$ ,  $\Delta\beta \sim 1.0$

$\gamma P$

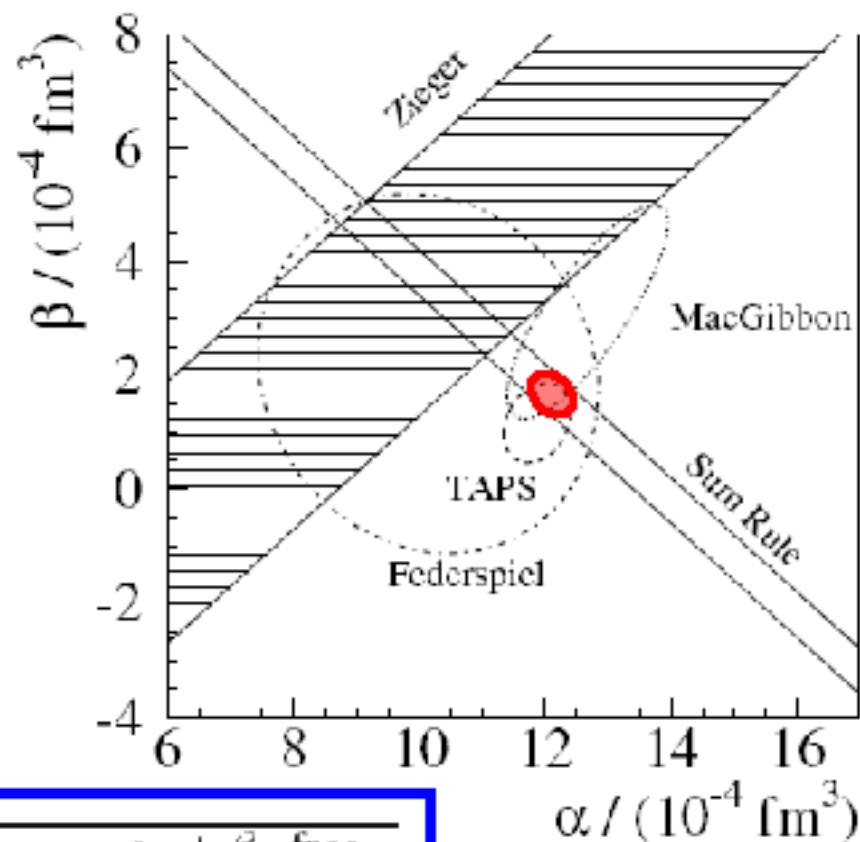
### Maximum scenario:

$I = 5 \mu\text{A}$ ,  $E = 110 \text{ MeV}$ ,  $T = 1000 \text{ h}$  (6 weeks)

$N = 600\,000$  events,  $\Delta\alpha \sim 0.25$ ,  $\Delta\beta \sim 0.35$

$\gamma P$

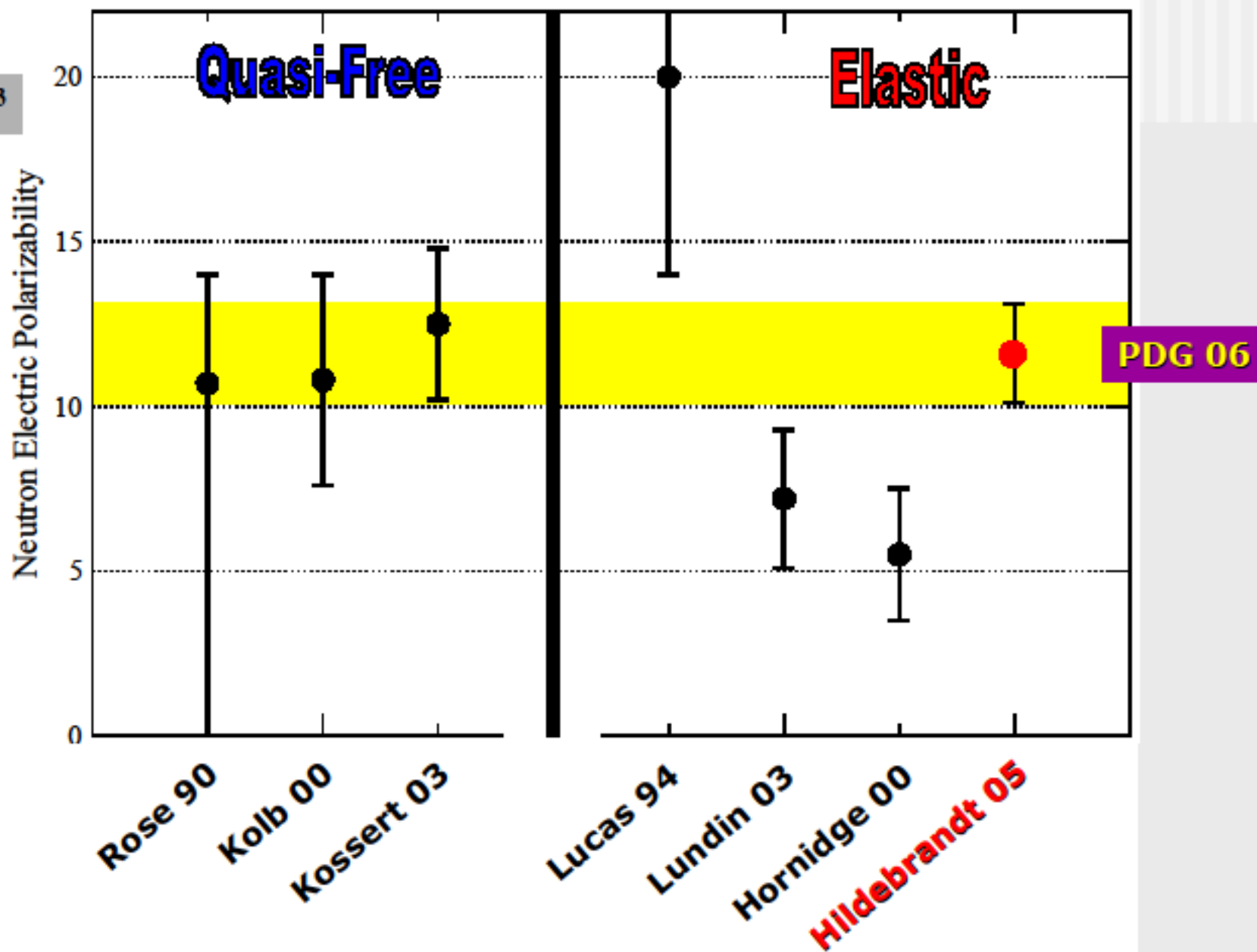
# Proton Polarizability



Data		$\alpha_p - \beta_p$ fixed	$\alpha_p + \beta_p$ free
TAPS Olmos de Leon	$\alpha_p$	$12.1 \pm 0.4 \mp 1.0$	$11.9 \pm 0.5 \mp 1.3$
	$\beta_p$	$1.6 \pm 0.4 \pm 0.8$	$1.2 \pm 0.7 \pm 0.3$
MacGibbon [4]	$\alpha_p$	$11.9 \pm 0.5 \mp 0.8$	$12.6 \pm 1.2 \mp 1.3$
	$\beta_p$	$1.9 \pm 0.5 \pm 0.8$	$3.0 \pm 1.8 \pm 0.1$
Federspiel [3]	$\alpha_p$	$10.8 \pm 2.2 \mp 1.3$	$10.1 \pm 2.6 \mp 2.0$
	$\beta_p$	$3.0 \pm 2.2 \pm 1.3$	$2.0 \pm 3.3 \pm 0.3$
Zieger [6]	$\alpha_p - \beta_p$	$6.4 \pm 2.3 \pm 1.9$	
Global fit	$\alpha_p$	$12.1 \pm 0.3 \mp 0.4$	$11.9 \pm 0.5 \mp 0.5$
	$\beta_p$	$1.6 \pm 0.4 \pm 0.4$	$1.5 \pm 0.6 \pm 0.2$

Olmos de Leon EPJ 01

$\times 10^{-4} \text{ fm}^3$



# Summary of Neutron Results

## ❑ Neutron scattering

- Schmiedmayer (91)

$$\alpha_n = 12.6 \pm 1.5(\text{stat}) \pm 2.0(\text{syst})$$

## ❑ Quasi-free Compton scattering

- Kossert (03)

$$\alpha_n = 12.5 \pm 1.8(\text{stat})^{+1.1}_{-0.6}(\text{syst}) \pm 1.1(\text{model})$$

$$\beta_n = 2.7 \mp 1.8(\text{stat})^{+0.6}_{-1.1}(\text{syst}) \mp 1.1(\text{model})$$

## ❑ Elastic Compton scattering

- data from Lucas (94), Hornidge (00), Lundin (03)
- global fit by Hildebrandt (05)

$$\alpha_n = 11.6 \pm 1.5(\text{stat}) \pm 0.6(\text{Baldin})$$

$$\beta_n = 3.6 \mp 1.5(\text{stat}) \mp 0.6(\text{Baldin})$$

**We can do better . . .**

# Theory (ChPT)

- MuCap( Gp from PCAC)

- $G_p(q^2) = 2M_\mu \cdot M_N \cdot F_a(0) / (M_\pi^2 - q^2)$

$$G_p(q^2) = 8.74 \text{ (LO)} \quad (8.26 \pm 0.23 \text{ (NNLO)})$$

## Polarizabilities ( $\alpha$ , $\beta$ )

$$\alpha_N = C \cdot R_\pi \cdot F_a(0)^2 / (f_\pi)^2, \quad \beta_N = 0.1 \cdot \alpha$$

- $C = 5 / (192\pi), \quad R_\pi = e^2 / (4\pi \cdot M_\pi)$

$$\alpha_N = 12 \text{ (LO)} \quad \beta_N = 1.2 \text{ (LO)}$$

-

# pseudoscalar form factor $g_P$

PCAC:

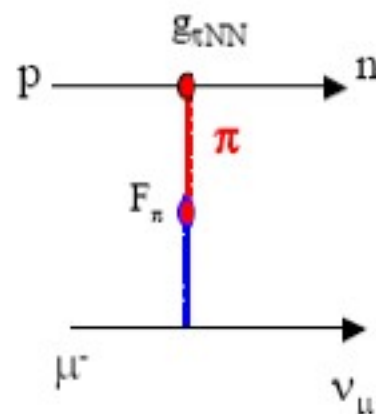
$$g_P(q^2) = \frac{2m_\mu M}{m_\pi^2 - q^2} g_A(0)$$

$$g_P = 8.7$$

heavy baryon chiral perturbation theory:

$$g_P(q^2) = \frac{2m_\mu g_{\pi NN} F_\pi}{m_\pi^2 - q^2} - \frac{1}{3} g_A(0) m_\mu M r_A^2$$

$$g_P = (8.74 \pm 0.23) - (0.48 \pm 0.02) = 8.26 \pm 0.23$$



$\Lambda$  calculations  $O(p^3)$  show good convergence: 100 % 25 % 3 %  
 delta effect small LO NLO NNLO

$g_{\pi NN}$   
 13.31(34)  
 13.0(1)  
 13.05(8)

author	year	$g_P$	$\Lambda_s$	$\Lambda_T$	comment
Primakoff	1959		664(20)	11.9(7)	smaller $g_A$
Opat	1964		634	13.3	smaller $g_A$
Bernard et al	1994	8.44(23)			
Fearing et al	1997	8.21(9)			
Govaerts et al	2000	8.475(76)	688.4(38)	12.01(12)	
Bernard et al	2000/1		687.4 (711*)	12.9	NNLO, small scale
Ando et al	2001		695 (722*)	11.9	NNLO

\*NLO result



## BEAM TIME ESTIMATION

### Minimum scenario:

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$\gamma\text{P}$

### Maximum scenario:

$I = 5 \mu\text{A}$ ,  $E = 110 \text{ MeV}$ ,  $T = 1000 \text{ h}$  (6 weeks)

$N = 600\,000$  events,  $\Delta\alpha \sim 0.25$ ,  $\Delta\beta \sim 0.35$

$\gamma\text{P}$

# Coherent DCS

Three data sets:

$E \sim 50, 70$  MeV (Illinois, Lund)

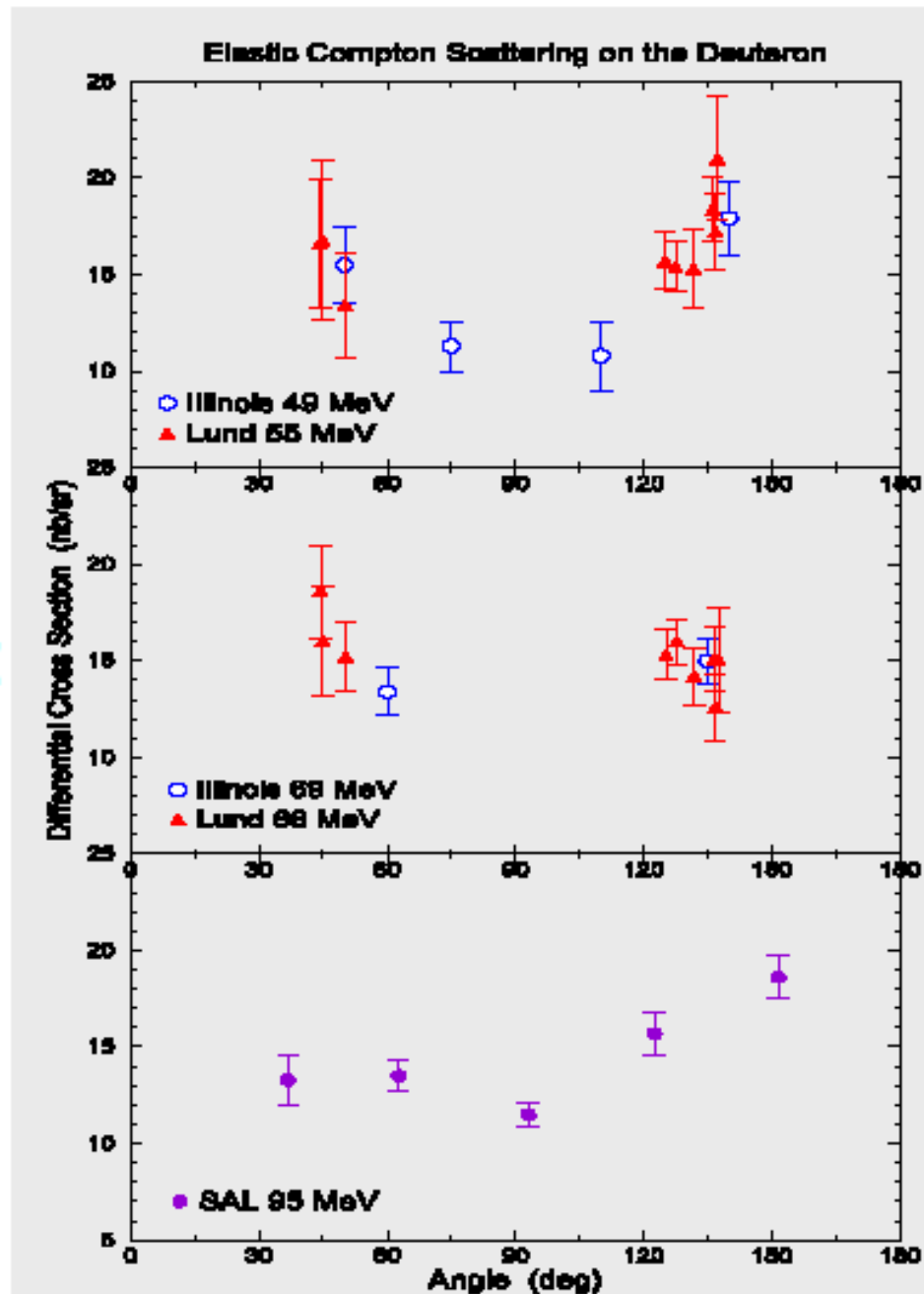
$E = 95$  MeV (SAL)

“Issues” with current data:

Large statistical uncertainties  
(commonly  $> 7\%$ )

Wide energy bins  
( $\Delta E$  is 6 - 20 MeV)

Limited kinematic coverage



Baldin sum rule:

$$\alpha_p + \beta_p = 13.8 \pm 0.4 \quad [10^{-4} \text{ fm}^3]$$

$$\alpha_n + \beta_n = 15.2 \pm 0.5$$

$$\alpha_p = 12.0 \pm 0.6 \quad \beta_p = 1.9 \pm 0.5$$

Scattering of neutrons on lead:  $\alpha_n = 13 \pm 6$  ;  $\alpha_n = 0.6 \pm 5$

Quasi-free Compton scattering from the deuteron:

$$\alpha_n = 7.6 - 14 \quad \beta_n = 1.2 - 7.6$$

$$\text{Mainz: } \alpha_n - \beta_n = 9.8 \pm 4.5$$